

A Systematic First-Principles Investigation of Mixed Transition Metal Olivine Phosphates $\text{LiM}_{1-y}\text{M}'_y\text{PO}_4$ (M/M'=Mn, Fe, Co) As Cathode Materials

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Supplementary material includes 9 figures, 3 tables for a total of 17 pages.

Figure S1: Variations of the unit cell parameters and volume of $\text{LiFe}_{1-y}\text{Mn}_y\text{PO}_4$ as a function of the composition parameter y

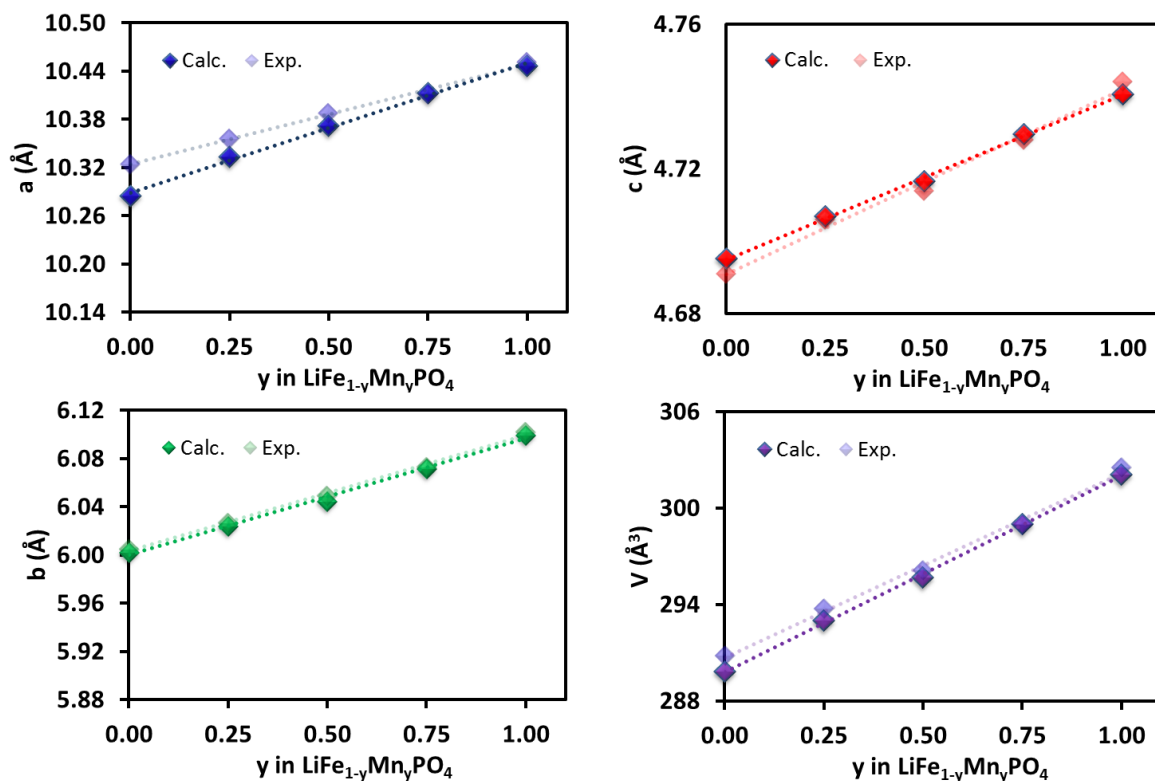


Figure S2: Variations of the unit cell parameters and volume of $\text{LiMn}_{1-y}\text{Co}_y\text{PO}_4$ as a function of the composition parameter y

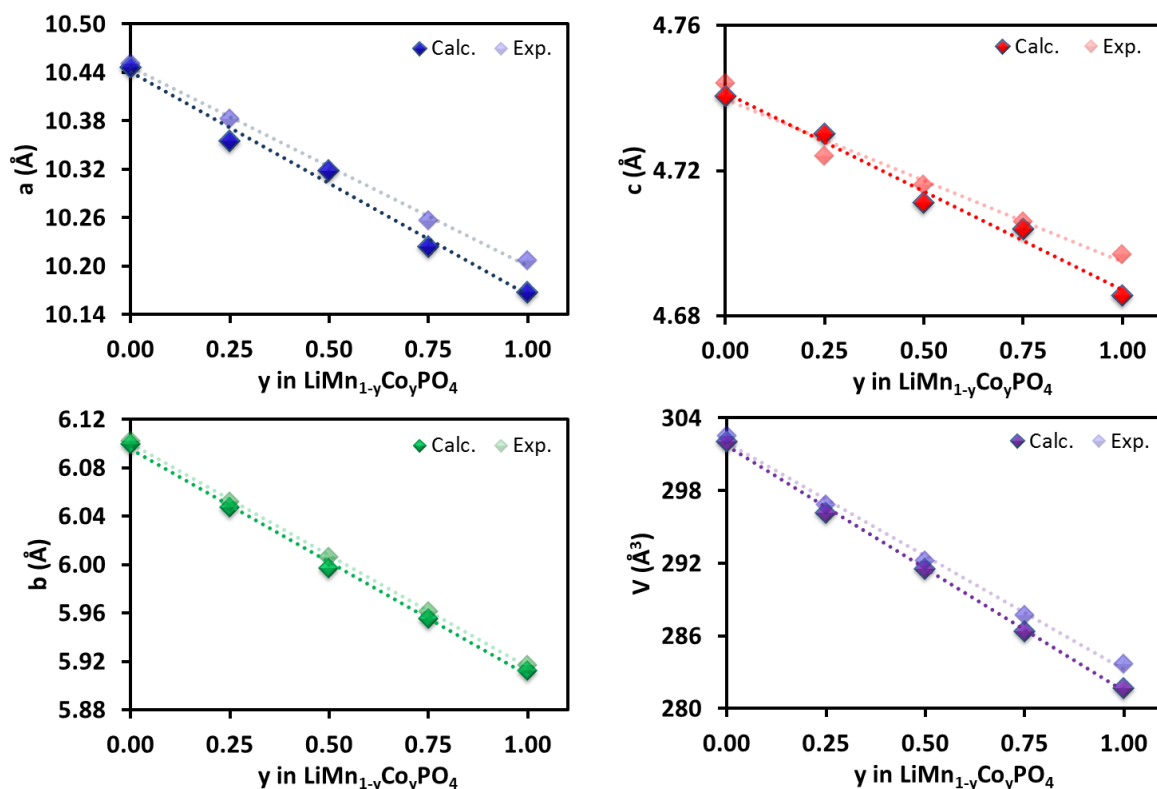


Figure S3: Variations of the unit cell parameters and volume of $\text{LiFe}_{1-y}\text{Co}_y\text{PO}_4$ as a function of the composition parameter y

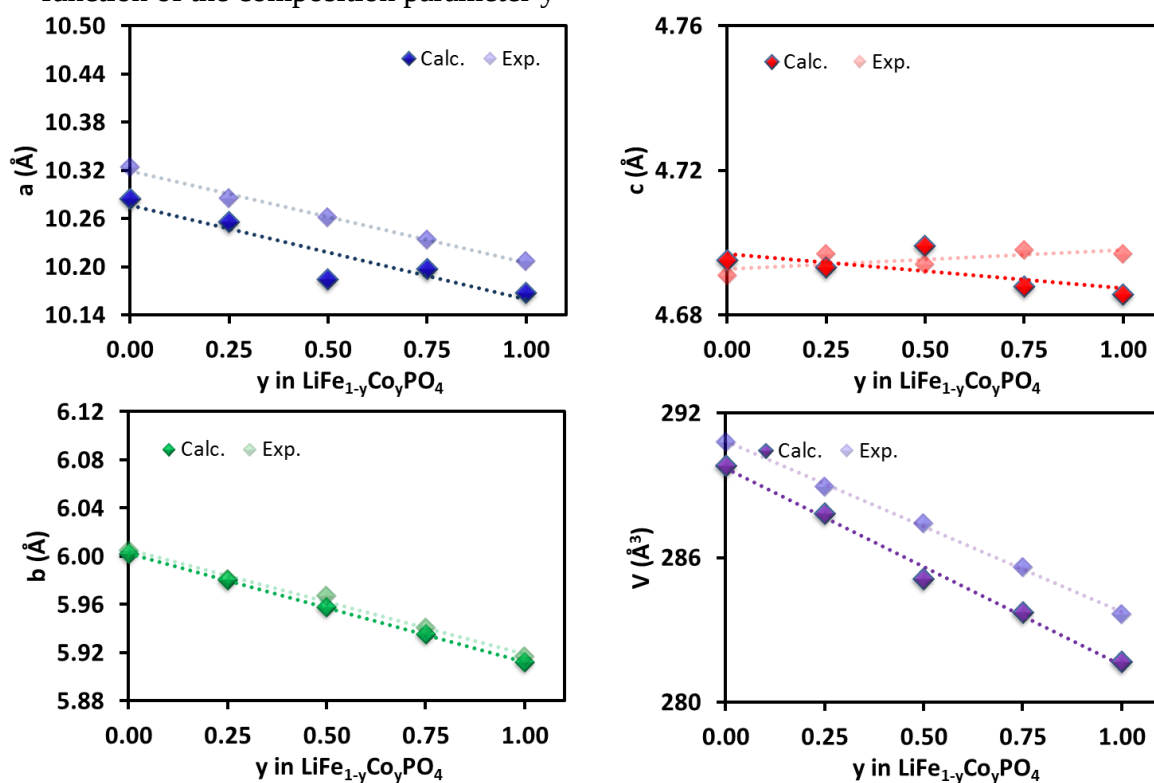
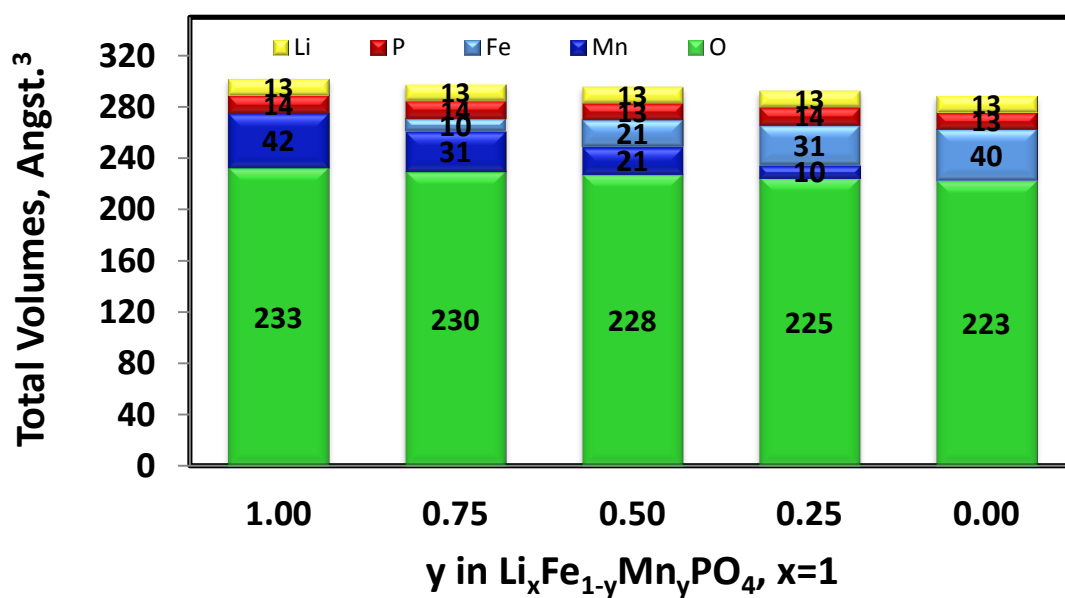
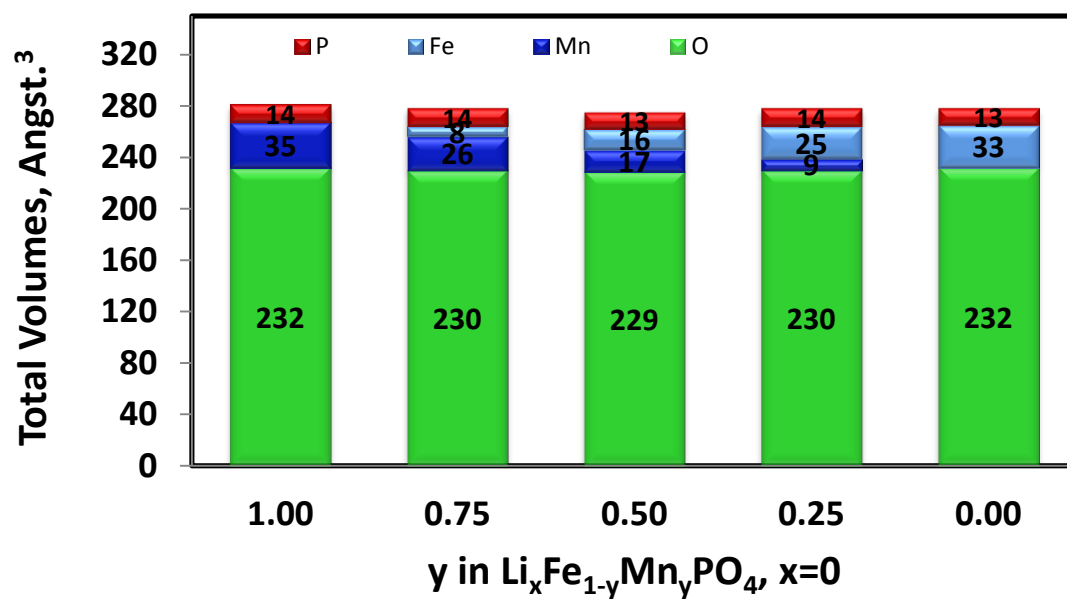


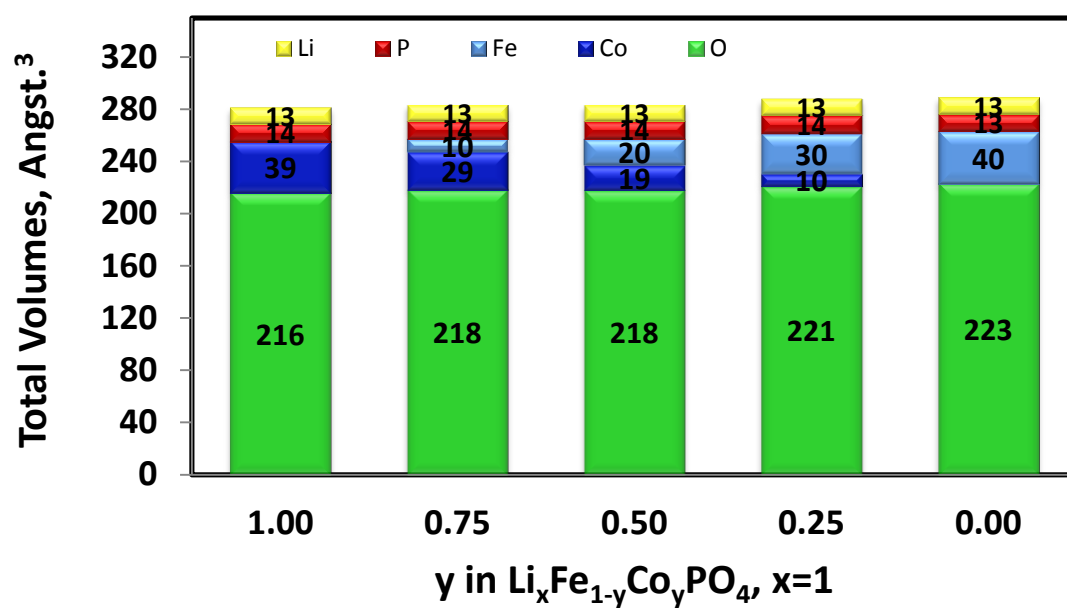
Figure S4: Bader volumes population evolution for mixed $\text{Li}_x\text{M}_{1-y}\text{M}_y\text{PO}_4$ olivines. (M=Co, Fe, Mn, $x=1$ and 0): (a) $\text{Li}_x\text{Fe}_{1-y}\text{Mn}_y\text{PO}_4$; (b) $\text{Li}_x\text{Fe}_{1-y}\text{Co}_y\text{PO}_4$; (c) $\text{Li}_x\text{Mn}_{1-y}\text{Co}_y\text{PO}_4$

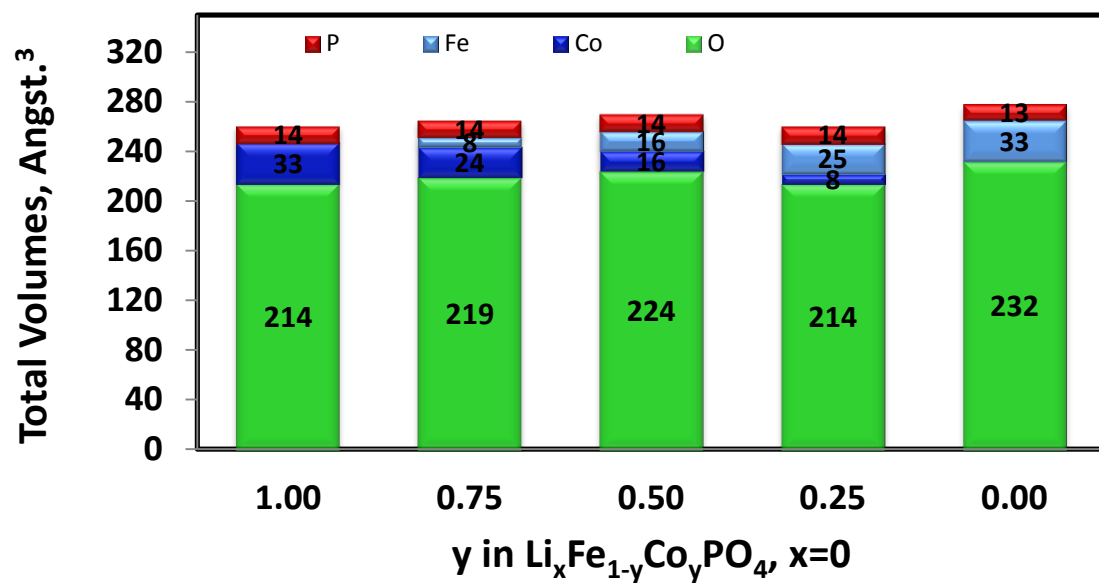
(a)



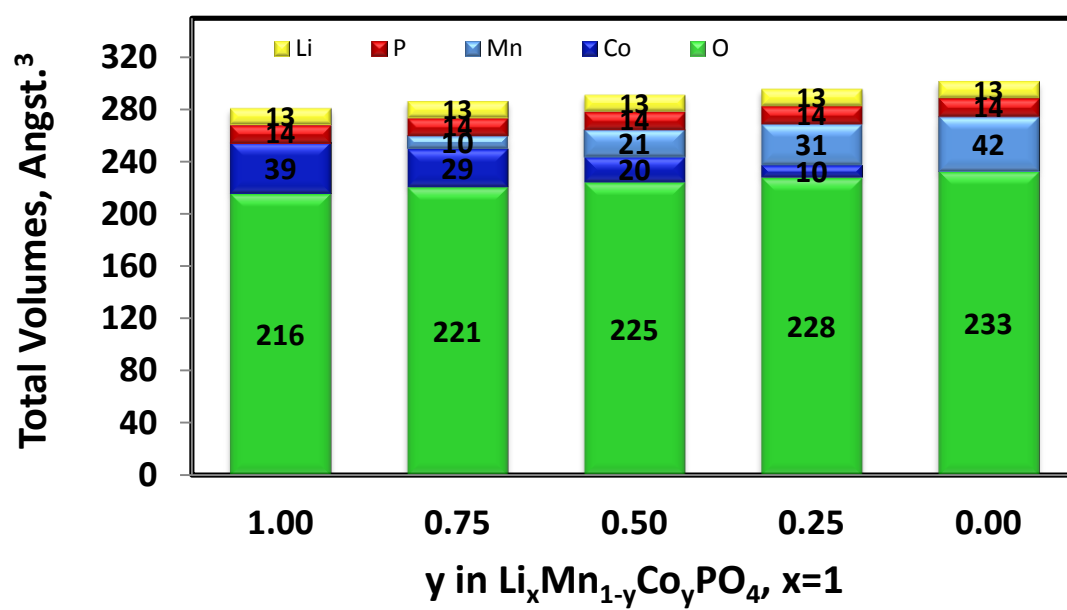


(b)





(c)



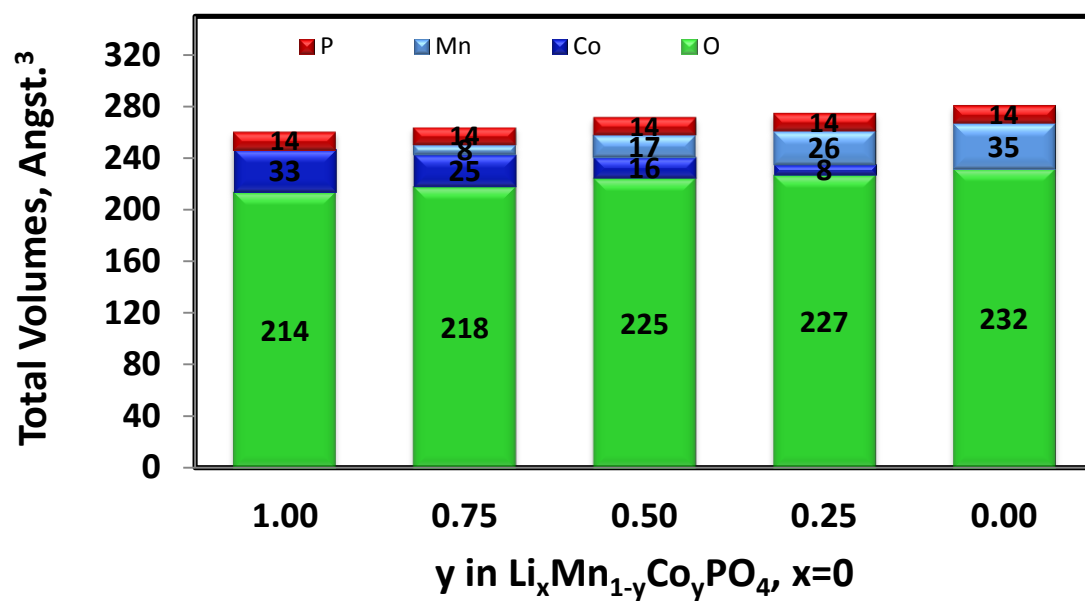


Figure S5: Schematic view of the octahedral $\text{M}(\text{H}_2\text{O})_6^{2+}$ complex. The transition metal ion M (M=Co, Fe, Mn) is enclosed in octahedra of O linked by H

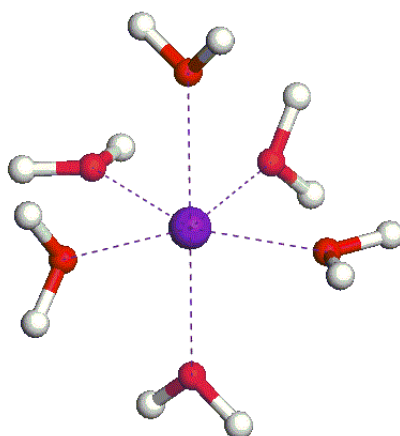


Figure S6: Spatial representation of HOMO orbitals of $\text{M}(\text{H}_2\text{O})_6^{2+}$ complexes (a) M=Co (b) M=Fe (c) M= Mn

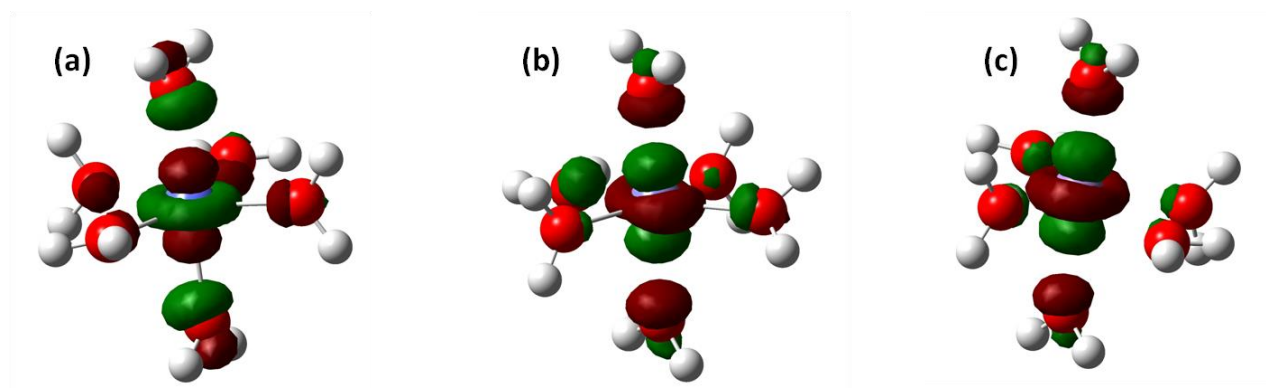
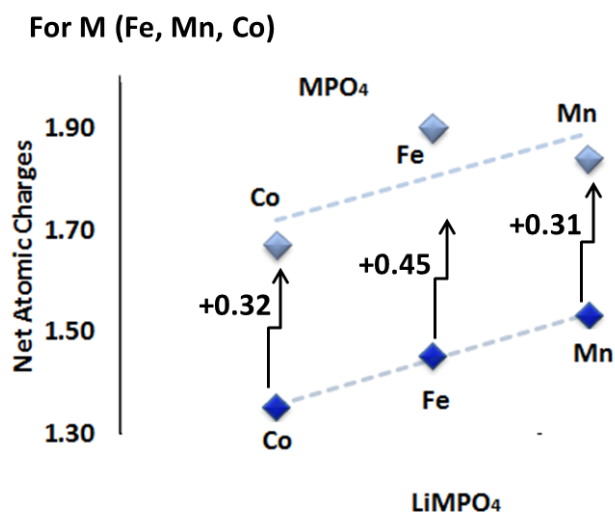
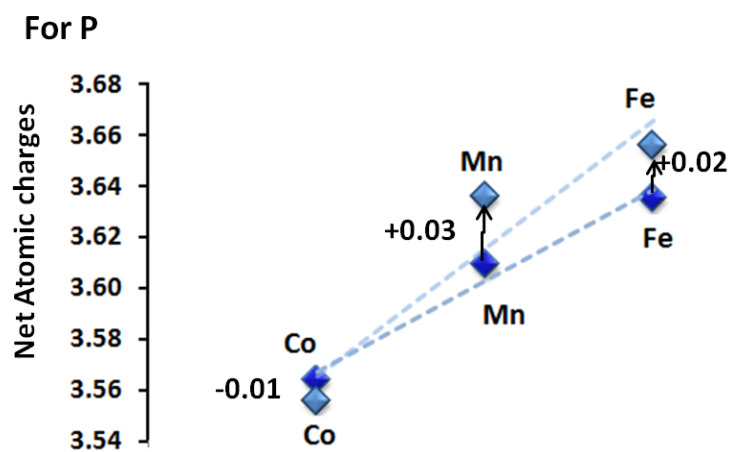


Figure S7: (a-c) Net atomic charges of M, P and O in LiMPO_4 and MPO_4 (M= Fe, Co, Mn), calculated by the Bader approach.

(a)



(b)



(c)

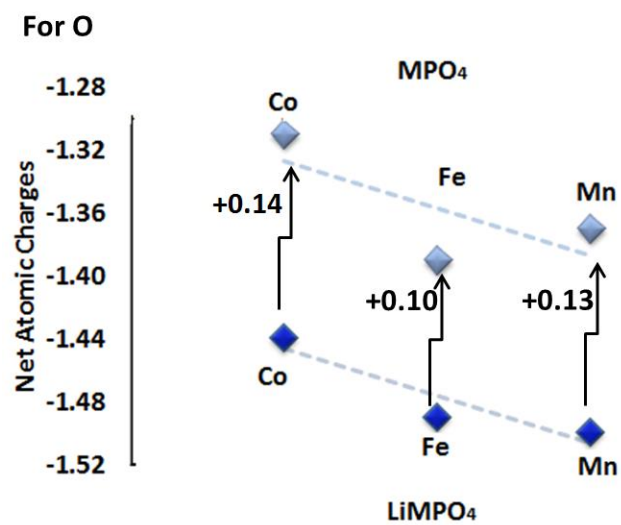
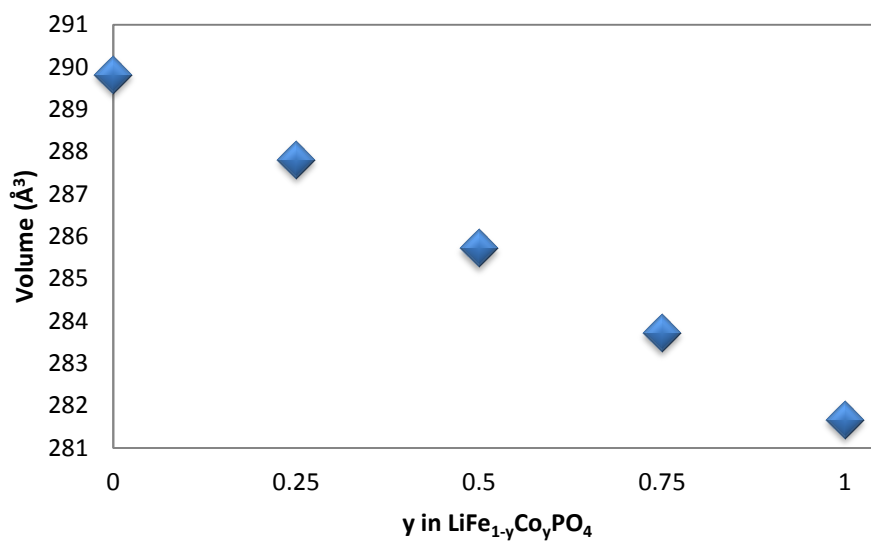
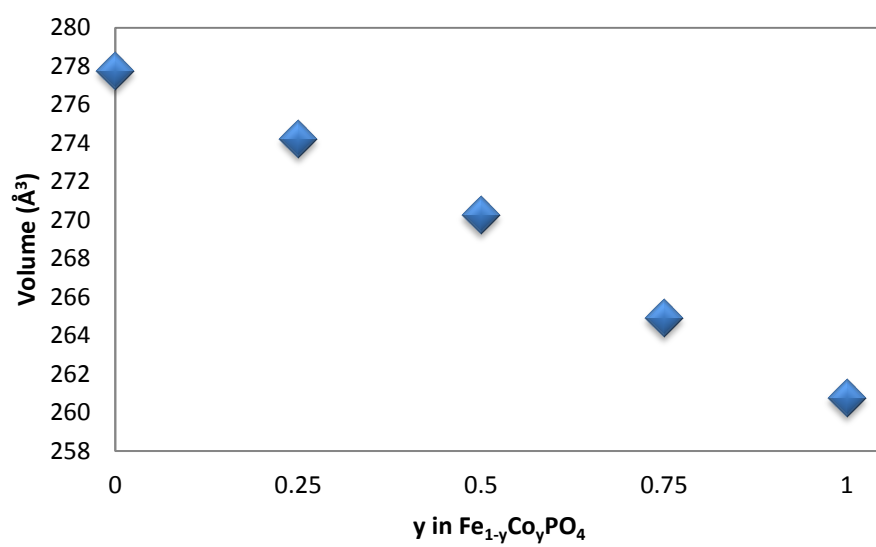


Figure S8: (a,b) Volume changes in lithiated (a) and delithiated (b) mixed iron cobalt olivines

(a)



(b)



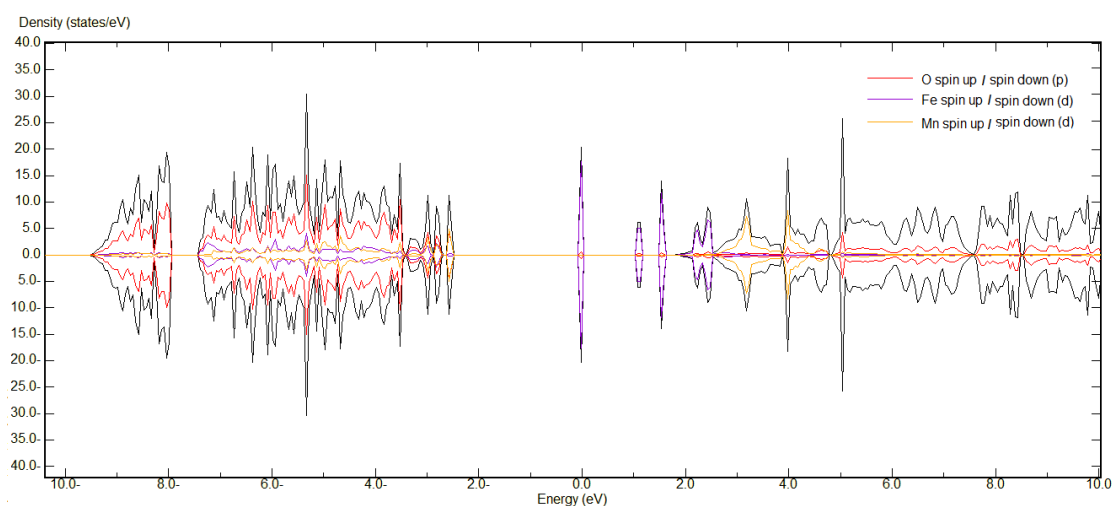
Redox active electrons and density of states

Based on the discussion on page 20-21 in the main manuscript, it is expected that in the mixed $\text{LiM}_{1-y}\text{M}'_y\text{PO}_4$ compounds the redox active electron (i.e. the top of the valence band) should belong to the metal with the highest d-band energy. The mixed electronic DOS of both $\text{LiFe}_{0.5}\text{Mn}_{0.5}\text{PO}_4$ and $\text{LiFe}_{0.5}\text{Co}_{0.5}\text{PO}_4$ indicate that the top of the valence band belongs to the d-states of the iron, indicated in cyan, Figure S9a and s9b, in qualitative agreement with the computed and experimental redox potentials (Figure 6a and 6b). However, for the $\text{LiMn}_{0.5}\text{Co}_{0.5}\text{PO}_4$ compound we did not succeed in reproducing the correct d-band ordering resulting in the Co d-electrons populating the top of the valence band (Figure S9c).

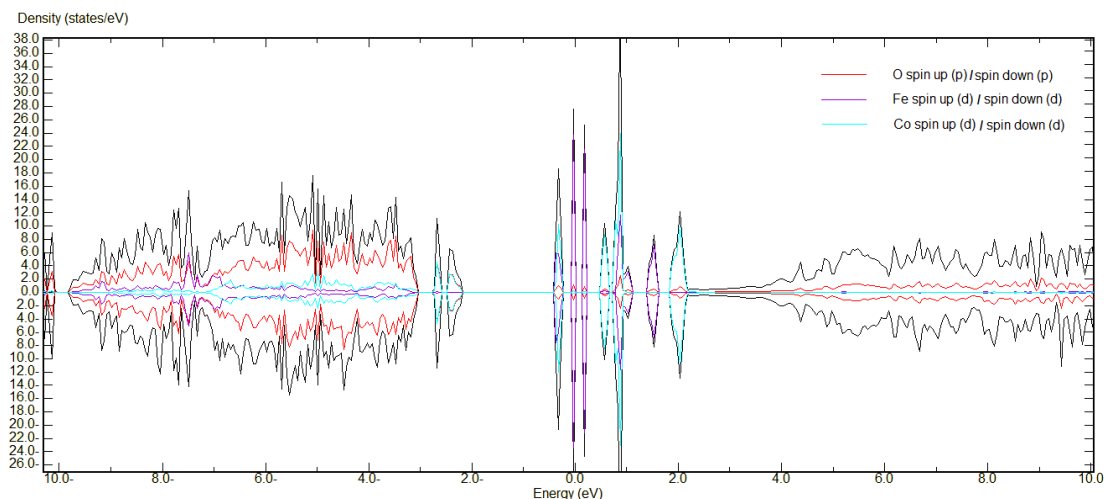
Figure S9: Calculated density of states for (a) $\text{LiFe}_{0.5}\text{Mn}_{0.5}\text{PO}_4$; (b) $\text{LiFe}_{0.5}\text{Co}_{0.5}\text{PO}_4$;

(c) $\text{LiMn}_{0.5}\text{Co}_{0.5}\text{PO}_4$

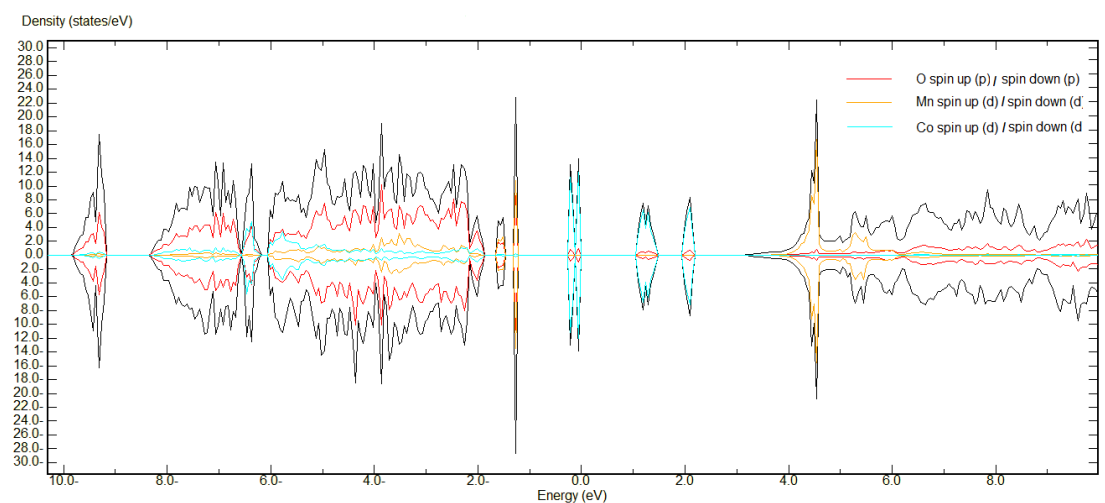
(a)



(b)



(c)



However, a recent study by Johannes et. al.¹ suggests that the GGA+U level might not be sufficiently accurate to describe the fine electronic structure details such as the composition of the top of the valence band, as compared to a hybrid functional such as HSE06. See Table 1 in the aforementioned reference and the discussion therein. On the other hand, the scheme developed by Ceder et. al.² for computing the voltage of these compounds is based on total energy calculations with suitable Hubbard

parameters, thus resulting in a good agreement with the experimental findings at the GGA+U level of theory.

Table S1: Calculated and experimental cell parameters of the olivine structures in the lithiated state, as well as discrepancy between the theoretical and experimental values

system	x	Calculated (GGA+U)				Experimental				% (Calc. vs Exp.)			
		a(Å)	b(Å)	c(Å)	V (Å ³)	a(Å)	b(Å)	c(Å)	V(Å ³)	a(Å)	b(Å)	c(Å)	V(Å ³)
LiFe _{1-x} Mn _x PO ₄	1.00	10.447	6.099	4.741	302.060	10.451	6.102	4.744	302.530	0.042	0.043	0.070	0.155
	0.75	10.412	6.072	4.730	299.000	10.412	6.073	4.728	298.960	0.001	0.022	0.032	0.013
	0.50	10.372	6.044	4.717	295.690	10.388	6.049	4.714	296.100	0.155	0.078	0.056	0.138
	0.25	10.333	6.024	4.707	292.980	10.356	6.027	4.706	293.730	0.224	0.050	0.019	0.255
	0.00	10.285	6.002	4.695	289.830	10.324	6.005	4.691	290.820	0.380	0.047	0.086	0.340
LiMn _{1-x} Co _x PO ₄	1.00	10.168	5.912	4.686	281.680	10.207	5.917	4.697	283.670	0.385	0.080	0.240	0.702
	0.75	10.224	5.955	4.704	286.370	10.257	5.961	4.706	287.730	0.322	0.101	0.042	0.473
	0.50	10.318	5.997	4.711	291.530	10.318	6.006	4.716	292.250	-0.001	0.149	0.100	0.246
	0.25	10.355	6.047	4.730	296.210	10.383	6.052	4.724	296.840	0.270	0.076	0.130	0.212
	0.00	10.447	6.099	4.741	302.060	10.451	6.102	4.744	302.530	0.042	0.043	0.070	0.155
LiFe _{1-x} Co _x PO ₄	1.00	10.168	5.912	4.686	281.680	10.207	5.917	4.697	283.670	0.385	0.080	0.240	0.702
	0.75	10.198	5.935	4.688	283.730	10.234	5.941	4.698	285.630	0.356	0.099	0.215	0.665
	0.50	10.184	5.958	4.699	285.130	10.262	5.967	4.694	287.420	0.756	0.154	0.109	0.797
	0.25	10.255	5.980	4.693	287.820	10.286	5.981	4.697	288.960	0.298	0.015	0.083	0.395
	0.00	10.285	6.002	4.695	289.830	10.324	6.005	4.691	290.820	0.380	0.047	0.086	0.340

Table S2: Calculated average metal-O (MO_6 octahedra) bond lengths in $\text{Li}_x\text{M}_{1-y}\text{PO}_4$ olivines (M = Fe, Co, Mn; y=1, 0.75, 0.5, 0.25, 0 and x=1, y, 0)
(a)

	y	Mn-O(Å)						Co-O(Å)					
		O1	O2	O3	O3	O ₃ '	O ₃ '	O1	O2	O3	O3	O ₃ '	O ₃ '
$\text{LiMn}_{1-y}\text{Co}_y\text{PO}_4$	1							2.110	2.072	2.177	2.177	2.054	2.054
	0.75	2.210	2.126	2.251	2.251	2.112	2.112	2.120	2.066	2.170	2.170	2.072	2.072
	0.5	2.236	2.142	2.249	2.249	2.115	2.115	2.110	2.068	2.189	2.189	2.072	2.072
	0.25	2.228	2.136	2.255	2.255	2.123	2.123	2.142	2.050	2.167	2.167	2.113	2.113
	0	2.237	2.144	2.264	2.264	2.132	2.132						
$\text{Mn}_{1-y}\text{Co}_y\text{PO}_4$	1							1.917	1.911	2.144	2.144	1.943	1.943
	0.75	1.901	1.884	2.056	2.056	1.985	1.985	1.898	1.916	2.131	2.131	2.020	2.020
	0.5	1.879	1.889	1.992	1.992	2.280	2.280	1.852	1.848	2.089	2.089	2.081	2.081
	0.25	1.891	1.880	2.270	2.270	2.003	2.003	1.863	1.843	2.140	2.140	2.049	2.049
	0	1.889	1.883	2.310	2.310	1.996	1.996						
$\text{Li}_{x=y}\text{Mn}_{1-y}\text{Co}_y\text{PO}_4$	0.75	1.938	1.915	2.251	2.096	2.087	1.974	2.203	2.009	2.291	2.233	2.034	2.011
	0.25	1.927	1.882	2.337	2.272	2.016	1.965	2.026	1.964	2.196	2.161	2.128	2.082
	0.5	1.939	1.887	2.296	2.265	2.024	1.964	2.041	2.028	2.296	2.115	2.136	2.041

(b)

	y	Fe-O(Å)						Co-O(Å)					
		O1	O2	O3	O3	O ₃ '	O ₃ '	O1	O2	O3	O3	O ₃ '	O ₃ '
LiFe _{1-y} Co _y PO ₄	1							2.110	2.072	2.177	2.177	2.054	2.054
	0.75	2.099	2.168	2.223	2.223	2.055	2.055	2.074	2.115	2.182	2.182	2.056	2.056
	0.5	2.094	2.176	2.230	2.230	2.057	2.057	2.086	2.117	2.184	2.184	2.055	2.055
	0.25	2.102	2.180	2.232	2.232	2.059	2.059	2.079	2.121	2.193	2.193	2.058	2.058
	0	2.103	2.185	2.236	2.236	2.059	2.059						
Fe _{1-y} Co _y PO ₄	1							1.917	1.911	2.144	2.144	1.943	1.943
	0.75	1.918	1.905	2.140	2.140	2.021	2.021	1.910	1.895	2.121	2.121	1.982	1.982
	0.5	1.941	1.927	2.117	2.117	2.018	2.018	1.909	1.907	2.170	2.170	1.958	1.958
	0.25	1.931	1.917	2.121	2.121	2.039	2.039	1.865	1.855	2.113	2.113	2.060	2.060
	0	1.932	1.921	2.129	2.129	2.041	2.041						
Li _{x-y} Fe _{1-y} Co _y PO ₄	0.75	1.990	1.966	2.086	2.055	2.044	2.019	2.156	2.008	2.241	2.195	2.062	2.038
	0.5	1.996	1.901	2.133	2.109	2.071	2.012	2.089	2.036	2.298	2.105	2.087	2.022
	0.25	1.992	1.923	2.141	2.111	2.041	1.997	2.050	1.957	2.165	2.163	2.117	2.094

(c)

	y	Fe-O(Å)						Mn-O(Å)					
		O1	O2	O3	O3	O ₃ '	O ₃ '	O1	O2	O3	O3	O ₃ '	O ₃ '
LiFe _{1-y} Mn _y PO ₄	1							2.237	2.144	2.264	2.264	2.132	2.132
	0.75	2.200	2.108	2.236	2.236	2.077	2.077	2.236	2.140	2.263	2.263	2.126	2.126
	0.5	2.182	2.095	2.243	2.243	2.070	2.070	2.246	2.148	2.251	2.251	2.118	2.118
	0.25	2.191	2.106	2.236	2.236	2.065	2.065	2.229	2.133	2.260	2.260	2.116	2.116
	0	2.185	2.103	2.236	2.236	2.059	2.059						
Fe _{1-y} Mn _y PO ₄	1							1.889	1.883	2.310	2.310	1.996	1.996
	0.75	1.925	1.912	2.157	2.157	2.034	2.034	1.897	1.880	2.291	2.291	2.003	2.003
	0.5	1.935	1.922	2.160	2.160	2.117	2.117	1.932	1.906	2.377	2.377	2.002	2.002
	0.25	1.926	1.925	2.135	2.135	2.038	2.038	1.907	1.875	2.273	2.273	2.009	2.009
	0	1.932	1.921	2.129	2.129	2.041	2.041						
Li _{1-x-y} Fe _x Mn _y PO ₄	0.75	2.215	2.107	2.272	2.234	2.140	2.128	1.997	1.925	2.180	2.134	2.127	2.028
	0.25	2.139	2.102	2.268	2.255	2.168	2.097	2.001	1.966	2.143	2.067	2.068	2.000
	0.5	2.137	2.133	2.319	2.289	2.101	2.045	1.992	2.062	2.117	2.056	1.958	2.048

Table S3: The FFT grid specification and Bader charge and volume analysis for LiMPO₄ (M=Co, Fe, Mn) systems.

LiCoPO₄

Atom Name	FFT grid							
	NGX=40 NGY = 24 NGZ = 18 NGXF=80 NGYF=48 NGZF= 6		NGX =80 NGY =48 NGZ =36 NGXF= 160 NGYF=96 NGZF=72		NGX =120 NGY =72 NGZ =54 NGXF=240 NGYF=160 NGZF=108		NGX =80 NGY =72 NGZ =54 NGXF=320 NGYF=192 NGZF=144	
	Average charge	Total volume	Average charge	Total volume	Average charge	Total volume	Average charge	Total volume
Li	0.87	12.76	0.87	12.52	0.87	12.49	0.87	12.47
O	-1.42	212.66	-1.47	217.28	-1.48	217.97	-1.48	218.21
P	3.48	15.14	3.64	13.38	3.67	12.91	3.68	12.74
Co	1.31	41.12	1.36	38.49	1.36	38.31	1.36	38.26

CoPO₄

Atom Name	FFT grid							
	NGX=36 NGY = 24 NGZ = 18 NGXF=72 NGYF=42 NGZF=3 6		NGX =72 NGY =42 NGZ =36 NGXF= 144 NGYF=84 NGZF=72		NGX =72 NGY =24 NGZ =18 NGXF=216 NGYF=126 NGZF=108		NGX =72 NGY =42 NGZ =36 NGXF=288 NGYF=168 NGZF=144	
	Average charge	Total volume	Average charge	Total volume	Average charge	Total volume	Average charge	Total volume
O	-1.28	212.46	-1.33	214.80	-1.33	214.68	-1.34	215.94
P	3.50	14.70	3.63	13.53	3.67	12.70	3.69	12.72
Co	1.63	32.43	1.67	32.43	1.65	33.39	1.68	32.12

LiFePO₄

Atom Name	FFT grid							
	NGX=40 NGY = 24 NGZ = 18 NGXF=80 NGYF=48 NGZF=3 6		NGX =80 NGY =48 NGZ =36 NGXF= 160 NGYF=96 NGZF=72		NGX =120 NGY =72 NGZ =54 NGXF=240 NGYF=160 NGZF=108		NGX =80 NGY =96 NGZ =72 NGXF=320 NGYF=192 NGZF=144	
	Average charge	Total volume	Average charge	Total volume	Average charge	Total volume	Average charge	Total volume
Li	0.87	12.87	0.87	12.76	0.87	12.69	0.87	12.68
O	-1.44	218.95	-1.49	223.06	-1.50	223.82	-1.50	224.06
P	3.48	15.09	3.63	13.48	3.67	12.92	3.68	12.75
Fe	1.40	42.92	1.45	40.52	1.45	40.40	1.45	40.35

FePO₄

Atom Name	FFT grid			
	NGX=36 NGY = 21 NGZ = 18	NGX =72 NGY =42 NGZ =36	NGX =72 NGY =64 NGZ =54	NGX =72 NGY =96 NGZ =72

	NGXF=72 NGYF=42 NGZF=3 6		NGXF= 144 NGYF=84 NGZF=72		NGXF=216 NGYF=126 NGZF=108		NGXF=288 NGYF=168 NGZF=144	
	Average charge	Total volume	Average charge	Total volume	Average charge	Total volume	Average charge	Total volume
O	-1.34	227.49	-1.38	231.10	-1.40	232.31	-1.40	232.46
P	3.52	14.74	3.62	13.70	3.69	14.74	3.70	12.74
Fe	1.84	35.51	1.90	32.94	1.90	35.51	1.91	32.55

LiMnPO₄

Atom Name	FFT grid							
	NGX=40 NGY = 24 NGZ = 18 NGXF=80 NGYF=48 NGZF=3 6		NGX =80 NGY =48 NGZ =36 NGXF= 160 NGYF=96 NGZF=72		NGX =80 NGY =48 NGZ =36 NGXF=240 NGYF=160 NGZF=108		NGX =80 NGY =48 NGZ =36 NGXF=320 NGYF=192 NGZF=144	
	Average charge	Total volume	Average charge	Total volume	Average charge	Total volume	Average charge	Total volume
Li	0.85	14.22	0.87	12.93	0.87	12.85	0.87	12.84
O	-1.45	227.30	-1.51	233.26	-1.52	234.08	-1.52	234.31
P	3.44	15.94	3.62	13.65	3.66	13.09	3.68	12.90
Mn	1.49	44.55	1.53	42.16	1.53	41.97	1.53	41.94

MnPO₄

Atom Name	FFT grid							
	NGX=36 NGY = 21 NGZ = 18 NGXF=72 NGYF=42 NGZF=3 6		NGX =72 NGY =48 NGZ =36 NGXF= 144 NGYF=96 NGZF=72		NGX =72 NGY =48 NGZ =36 NGXF=216 NGYF=144 NGZF=108		NGX =80 NGY =96 NGZ =72 NGXF=320 NGYF=192 NGZF=144	
	Average charge	Total volume	Average charge	Total volume	Average charge	Total volume	Average charge	Total volume
O	-1.32	228.37	-1.37	231.61	-1.38	232.50	-1.39	232.84
P	3.46	16.00	3.63	13.66	3.69	12.94	3.71	12.67
Mn	1.82	36.02	1.84	35.13	1.85	34.95	1.85	34.88

References:

1. Johannes, M.; Hoang, K.; Allen, J.; Gaskell, K. Hole polaron formation and migration in olivine phosphate materials. *Physical Review B* **2012**, *85*, 115106.
2. Aydinol, M. K.; Kohan, A. F.; Ceder, G.; Cho, K.; Joannopoulos, J. Ab initio study of lithium intercalation in metal oxides and metal dichalcogenides. *Phys. Rev. B* **1997**, *56*, 1354-1365.