Supporting information for: Frozen Density Embedding with External Orthogonality in Delocalized Covalent Systems

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1 System Geometries

	subsys	stem I			subsy	stem II	
atom	x	y	z	atom	x	y	z
0	-1.4626	0.0000	0.0000	0	1.4626	0.0000	0.0000
Η	-1.7312	0.9302	0.0000	Η	1.9309	0.3579	0.7697
Н	-0.4844	0.0275	0.0000	Η	1.9309	0.3579	-0.7697

Table S1: Water dimer geometry (in Å).

Table S2: FHF⁻ geometry (in Å).

FH subsystem				F^- subsystem				
atom	x	y	z	atom	x	y	z	
F	0.0000	0.0000	1.1587	F	0.0000	0.0000	-1.1587	
Η	0.0000	0.0000	0.0000					

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Table S3: BH_3NH_3 geometry (in Å).

	BH_3 su	lbsystem		$\rm NH_3~subsystem$				
atom	x	y	z	atom	x	y	z	
В	0.0000	0.0000	0.8382	Ν	0.0000	0.0000	-0.8158	
Н	-0.5864	-1.0157	1.1548	Η	0.4765	-0.8252	-1.1862	
Η	-0.5864	1.0157	1.1548	Η	0.4765	0.8252	-1.1862	
Η	1.1728	0.0000	1.1548	Η	-0.9529	0.0000	-1.1862	

Table S4: C_2H_6 geometry (in Å).

CH_3^+ su	ıbsystem		CH_3^- subsystem				
x	y	z	atom	x	y	z	
0.0000	0.0000	0.7651	С	0.0000	0.0000	-0.7651	
0.0000	-1.0222	1.1666	Η	0.8853	-0.5111	-1.1666	
-0.8853	0.5111	1.1666	Η	0.0000	1.0222	-1.1666	
0.8853	0.5111	1.1666	Η	-0.8853	-0.5111	-1.1666	
	$\begin{array}{c} {\rm CH}^+_3 {\rm su}\\ \hline x\\ \hline 0.0000\\ 0.0000\\ 0.8853\\ 0.8853\end{array}$	$\begin{array}{c c} \mathrm{CH}_3^+ \text{ subsystem} \\ \hline x & y \\ \hline 0.0000 & 0.0000 \\ 0.0000 & -1.0222 \\ 0.8853 & 0.5111 \\ 0.8853 & 0.5111 \\ \end{array}$	$\begin{array}{c cccc} {\rm CH}_3^+ \mbox{ subsystem} & \\ \hline x & y & z \\ \hline 0.0000 & 0.0000 & 0.7651 \\ 0.0000 & -1.0222 & 1.1666 \\ 0.8853 & 0.5111 & 1.1666 \\ 0.8853 & 0.5111 & 1.1666 \\ \hline \end{array}$	CH_3^+ subsystem x y z $atom$ 0.0000 0.0000 0.7651 C 0.0000 -1.0222 1.1666 H 0.8853 0.5111 1.1666 H 0.8853 0.5111 1.1666 H	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	

Table S5: C_6H_{12} geometry (in Å).

atom x y z atom x y z	z
C = 31505 + 0.3535 + 0.0351 + C = 0.6165 + 0.2504 + 0.040	_
0 -3.1333 -0.3333 0.0331 0 0.0103 0.2334 -0.040)
Н -3.1754 -1.1510 -0.7229 Н 0.7222 1.3357 -0.232	3
H -4.0780 0.2386 -0.0819 C 1.9083 -0.5197 0.109	7
Н -3.1945 -0.8346 1.0241 Н 1.9381 -1.3285 -0.638	3
C -1.9086 0.5199 -0.1096 H 1.9250 -1.0195 1.092	1
H -1.9408 1.3297 0.6377 C 3.1600 0.3521 -0.036	7
Н -1.9241 1.0183 -1.0928 Н 4.0779 -0.2418 0.074	4
C -0.6166 -0.2579 0.0421 H 3.1807 1.1466 0.724	5
H -0.7219 -1.3344 0.2335 H 3.1915 0.8372 -1.023	9

	subsy	v stem I		subsystem II				
atom	x	y	z	atom	x	y	z	
С	-0.5764	-0.0196	-4.2325	С	0.6473	-0.3793	0.5416	
Η	-1.4640	0.3376	-4.7742	Η	0.6756	-1.4674	0.3942	
Η	-0.5526	-1.1169	-4.3182	С	0.6194	0.0918	1.9688	
Η	0.3123	0.3729	-4.7505	Η	0.6127	1.1936	1.9948	
\mathbf{C}	-0.6019	0.4206	-2.7654	Η	1.5461	-0.2279	2.4798	
Η	-1.5144	0.0423	-2.2761	С	-0.5819	-0.4528	2.7648	
Η	-0.6578	1.5208	-2.7097	Η	-0.5780	-1.5546	2.7114	
С	0.6257	-0.0595	-1.9677	Η	-1.5127	-0.1257	2.2730	
Η	1.5348	0.3101	-2.4767	С	-0.5836	-0.0086	4.2309	
Η	0.6783	-1.1600	-1.9944	Η	-1.4521	-0.4117	4.7713	
С	0.6257	0.4116	-0.5402	Η	-0.6190	1.0886	4.3135	
Η	0.5927	1.4996	-0.3924	Η	0.3236	-0.3513	4.7521	

Table S6: C_8H_{16} geometry (in Å).

Table S7: $C_{10}H_{20}$ geometry (in Å).

	subsy	vstem I		subsystem II				
atom	x	y	z	atom	x	y	z	
С	0.0855	0.7963	-5.0878	С	0.6551	-0.3168	0.5133	
Η	1.1425	0.6724	-4.8099	Η	0.8182	-1.3865	0.3246	
Н	-0.1514	1.8703	-5.0274	С	0.5973	0.0963	1.9579	
Н	-0.0142	0.4921	-6.1401	Η	1.5590	-0.1463	2.4425	
\mathbf{C}	-0.8452	-0.0226	-4.1845	Η	0.4764	1.1898	2.0253	
Н	-1.8796	0.0812	-4.5506	С	-0.5445	-0.5967	2.7292	
Η	-0.5976	-1.0945	-4.2743	Η	-0.4254	-1.6914	2.6431	
С	-0.8134	0.3794	-2.7005	Η	-1.4963	-0.3522	2.2300	
Η	-1.6203	-0.1476	-2.1655	С	-0.6397	-0.2132	4.2150	
Н	-1.0386	1.4570	-2.6108	Η	-1.5758	-0.6287	4.6225	
С	0.5180	0.0813	-1.9814	Η	-0.7327	0.8834	4.3007	
Η	1.3356	0.6078	-2.5036	С	0.5342	-0.6972	5.0755	
Η	0.7407	-0.9960	-2.0508	Η	1.4888	-0.2535	4.7565	
С	0.5039	0.5014	-0.5377	Η	0.6399	-1.7920	5.0177	
Η	0.3363	1.5704	-0.3490	Η	0.3870	-0.4324	6.1328	
				_				

	subsy	v stem I		subsystem II				
atom	x	y	z	atom	x	y	z	
С	-0.0185	1.9689	-5.3535	С	0.5329	-0.3242	0.5389	
Η	0.7078	2.3769	-6.0718	Η	0.6786	-1.4049	0.4054	
Η	0.0983	2.5311	-4.4149	С	0.4734	0.1618	1.9608	
Η	-1.0273	2.1795	-5.7429	Η	1.4386	-0.0496	2.4538	
С	0.1907	0.4628	-5.1500	Η	0.3485	1.2569	1.9725	
Η	0.1421	-0.0403	-6.1298	С	-0.6596	-0.4973	2.7728	
Η	1.2107	0.2810	-4.7724	Η	-0.5347	-1.5930	2.7429	
С	-0.8384	-0.2018	-4.2170	Η	-1.6162	-0.2904	2.2656	
Η	-0.6756	-1.2933	-4.2288	С	-0.7606	-0.0187	4.2321	
Η	-1.8466	-0.0407	-4.6364	Η	-1.6753	-0.4474	4.6771	
С	-0.8374	0.2806	-2.7555	Η	-0.9053	1.0754	4.2356	
Η	-1.6875	-0.1833	-2.2290	С	0.4333	-0.3632	5.1415	
Η	-1.0182	1.3683	-2.7174	Η	0.2707	0.1181	6.1200	
С	0.4524	-0.0438	-1.9753	Η	1.3544	0.0884	4.7370	
Η	1.3109	0.4211	-2.4912	С	0.6527	-1.8662	5.3570	
Η	0.6297	-1.1316	-1.9890	Η	1.4814	-2.0495	6.0565	
С	0.4131	0.4437	-0.5533	Η	0.8961	-2.3854	4.4179	
Н	0.2638	1.5238	-0.4192	Н	-0.2486	-2.3421	5.7752	

Table S8: $C_{12}H_{24}$ geometry (in Å).

			-	-	· · · /				
	subsy	vstem I		subsystem II					
atom	x	y	z	atom	x	y	z		
С	0.6824	2.2735	-6.4294	С	0.5178	-0.3216	0.5731		
Η	1.7278	2.2052	-6.0905	Η	0.6394	-1.4122	0.5234		
Η	0.4567	3.3362	-6.5997	С	0.5068	0.2784	1.9520		
Η	0.6152	1.7576	-7.3998	Η	1.4752	0.0726	2.4408		
С	-0.2723	1.6525	-5.4035	Η	0.4193	1.3748	1.8779		
Η	-0.2055	2.2196	-4.4603	С	-0.6291	-0.2715	2.8375		
Η	-1.3137	1.7638	-5.7535	Н	-0.5512	-1.3712	2.8820		
С	0.0115	0.1666	-5.1401	Η	-1.5903	-0.0587	2.3413		
Η	-0.0306	-0.3753	-6.1009	С	-0.6676	0.3107	4.2617		
Η	1.0495	0.0540	-4.7814	Η	-1.5858	-0.0430	4.7586		
С	-0.9609	-0.5106	-4.1576	Н	-0.7703	1.4075	4.1934		
Η	-0.7491	-1.5934	-4.1374	С	0.5484	-0.0078	5.1537		
Η	-1.9860	-0.4102	-4.5531	Н	0.4107	0.5069	6.1207		
С	-0.9412	0.0234	-2.7138	Н	1.4550	0.4339	4.7081		
Η	-1.7663	-0.4416	-2.1500	С	0.8087	-1.5012	5.4252		
Η	-1.1495	1.1065	-2.7116	Н	1.7426	-1.5883	6.0048		
С	0.3743	-0.2385	-1.9532	Н	0.9986	-2.0260	4.4738		
Η	1.2136	0.1865	-2.5312	С	-0.3173	-2.2150	6.1845		
Η	0.5550	-1.3239	-1.8895	Н	-0.0503	-3.2603	6.3992		
С	0.3817	0.3591	-0.5734	Н	-1.2560	-2.2279	5.6108		
Η	0.2548	1.4490	-0.5220	Н	-0.5229	-1.7191	7.1466		

Table S9: $C_{14}H_{28}$ geometry (in Å).

Table S10: C_6H_8 geometry (in Å).

	subsy	vstem I		subsystem II			
atom	x	y	z	atom	x	y	z
С	-3.0670	-0.3214	-0.0670	С	0.5943	0.3283	0.0291
Η	-4.0109	0.2224	-0.0697	Η	0.5913	1.4238	0.0304
Η	-3.1172	-1.4114	-0.1095	С	1.8844	-0.3239	0.0331
С	-1.8842	0.3233	-0.0025	Η	1.8786	-1.4183	0.0662
Η	-1.8776	1.4175	0.0391	С	3.0673	0.3233	-0.0025
С	-0.5947	-0.3299	0.0151	Η	3.1159	1.4135	-0.0379
Н	-0.5919	-1.4255	0.0088	Н	4.0122	-0.2187	0.0088

	subsy	vstem I			subsy	rstem II	
atom	x	y	z	atom	x	y	z
С	-4.4159	0.3378	0.0131	С	0.5969	0.3298	-0.0130
Н	-4.3294	1.4325	0.0247	Η	0.5956	1.4252	-0.0124
Н	-4.9997	0.0306	0.8963	С	1.8847	-0.3224	-0.0036
Н	-5.0147	0.0496	-0.8665	Η	1.8804	-1.4188	-0.0018
\mathbf{C}	-3.0719	-0.3224	-0.0036	С	3.0739	0.3214	0.0049
Н	-3.0636	-1.4184	-0.0046	Η	3.0711	1.4174	0.0004
С	-1.8855	0.3265	-0.0106	С	4.4144	-0.3461	0.0209
Η	-1.8851	1.4230	-0.0095	Η	5.0130	-0.0636	-0.8607
\mathbf{C}	-0.5963	-0.3228	-0.0157	Η	4.3219	-1.4402	0.0358
Η	-0.5939	-1.4182	-0.0137	Η	5.0016	-0.0403	0.9023

Table S11: C_8H_{12} geometry (in Å).

Table S12: $C_{10}H_{12}$ geometry (in Å).

	subsy	vstem I			subsy	vstem II	
atom	x	y	z	atom	x	y	z
С	-5.5488	-0.2968	0.0080	С	0.6003	0.3120	-0.0192
Н	-6.4845	0.2609	0.0127	Η	0.5937	1.4070	-0.0160
Н	-5.6162	-1.3867	0.0227	С	1.8776	-0.3314	-0.0154
\mathbf{C}	-4.3525	0.3311	-0.0094	Η	1.8868	-1.4266	-0.0116
Н	-4.3293	1.4260	-0.0203	С	3.0716	0.3311	-0.0094
\mathbf{C}	-3.0762	-0.3389	-0.0147	Η	3.0632	1.4265	-0.0123
Η	-3.0869	-1.4340	-0.0223	С	4.3597	-0.3139	0.0196
С	-1.8731	0.3068	-0.0099	Η	4.3592	-1.4090	0.0154
Н	-1.8708	1.4021	0.0058	С	5.5419	0.3397	0.0609
С	-0.5998	-0.3448	-0.0195	Η	5.5851	1.4308	0.0706
Η	-0.5965	-1.4394	-0.0270	Н	6.4892	-0.1975	0.0876

	subsy	vstem I		subsystem II				
atom	x	y	z	atom	x	y	z	
С	-6.8885	0.3419	-0.0728	С	0.6022	0.3258	0.0897	
Η	-6.7995	1.4363	-0.0737	Η	0.5997	1.4208	0.0908	
Η	-7.5116	0.0473	0.7876	С	1.8769	-0.3224	0.0686	
Η	-7.4495	0.0431	-0.9736	Η	1.8794	-1.4177	0.0714	
С	-5.5482	-0.3224	-0.0249	С	3.0765	0.3298	0.0271	
Η	-5.5434	-1.4184	-0.0241	Η	3.0752	1.4249	0.0216	
С	-4.3582	0.3232	0.0145	С	4.3585	-0.3224	-0.0249	
Η	-4.3546	1.4197	0.0148	Η	4.3552	-1.4188	-0.0166	
С	-3.0757	-0.3291	0.0515	С	5.5475	0.3229	-0.0922	
Η	-3.0747	-1.4242	0.0484	Η	5.5427	1.4188	-0.1023	
С	-1.8755	0.3225	0.0785	С	6.8860	-0.3431	-0.1607	
Η	-1.8771	1.4178	0.0798	Η	7.4280	-0.0548	-1.0765	
С	-0.6010	-0.3263	0.0903	Η	6.7961	-1.4373	-0.1479	
Н	-0.5991	-1.4213	0.0871	Н	7.5274	-0.0395	0.6831	

Table S13: $C_{12}H_{16}$ geometry (in Å).

Table S14: $C_{14}H_{16}$ geometry (in Å).

	subsy	vstem I			vstem II		
atom	x	y	z	atom	x	y	z
С	-8.0253	-0.2506	0.0699	С	0.6022	0.2962	-0.1200
Η	-8.1149	-1.3381	0.0308	Η	0.5907	1.3911	-0.1146
Н	-8.9487	0.3255	0.1139	С	1.8755	-0.3407	-0.0986
С	-6.8164	0.3542	0.0654	Η	1.8897	-1.4359	-0.0947
Η	-6.7729	1.4477	0.1064	С	3.0732	0.3271	-0.0592
С	-5.5529	-0.3348	0.0076	Η	3.0583	1.4218	-0.0605
Η	-5.5795	-1.4291	-0.0212	С	4.3496	-0.3085	0.0046
С	-4.3402	0.2958	-0.0161	Η	4.3615	-1.4036	0.0148
Η	-4.3249	1.3907	0.0093	С	5.5439	0.3542	0.0654
С	-3.0774	-0.3675	-0.0706	Η	5.5395	1.4493	0.0547
Η	-3.0834	-1.4621	-0.0853	С	6.8256	-0.2976	0.1464
С	-1.8693	0.2818	-0.0961	Η	6.8159	-1.3924	0.1682
Η	-1.8707	1.3767	-0.0834	С	8.0135	0.3456	0.1949
С	-0.6011	-0.3651	-0.1221	Η	8.0685	1.4359	0.1754
Η	-0.5940	-1.4597	-0.1265	Н	8.9542	-0.2006	0.2523

	subsy	stem I		subsystem II					
atom	x	y	z	atom	x	y	z		
С	-9.2739	-0.3141	0.5769	С	0.6156	-0.3666	-0.5073		
Η	-9.6805	-0.0164	1.5577	Η	0.6172	-1.4616	-0.4963		
Η	-9.1981	-1.4092	0.5584	С	1.8778	0.2893	-0.4390		
Η	-10.0232	-0.0062	-0.1707	Η	1.8726	1.3844	-0.4526		
С	-7.9513	0.3380	0.3230	С	3.0836	-0.3516	-0.3041		
Η	-7.9327	1.4336	0.3380	Η	3.0905	-1.4463	-0.2790		
С	-6.7888	-0.3194	0.0923	С	4.3356	0.3134	-0.1383		
Η	-6.7986	-1.4155	0.0777	Η	4.3254	1.4084	-0.1649		
С	-5.5170	0.3208	-0.1095	С	5.5261	-0.3194	0.0923		
Η	-5.5033	1.4158	-0.0938	Η	5.5380	-1.4139	0.1247		
С	-4.3332	-0.3422	-0.2836	С	6.7726	0.3561	0.3342		
Η	-4.3460	-1.4373	-0.2962	Η	6.7551	1.4519	0.3010		
С	-3.0630	0.2963	-0.4097	С	7.9421	-0.2664	0.6191		
Η	-3.0515	1.3912	-0.3970	Η	7.9520	-1.3618	0.6511		
С	-1.8626	-0.3629	-0.4958	С	9.2368	0.4255	0.9096		
Η	-1.8689	-1.4581	-0.4976	Η	9.6140	0.1569	1.9103		
С	-0.5941	0.2833	-0.5294	Η	9.1327	1.5177	0.8674		
Н	-0.5922	1.3785	-0.5293	Н	10.0216	0.1246	0.1963		

Table S15: $C_{16}H_{20}$ geometry (in Å).

	subsy	stem I		subsystem II				
atom	x	y	z	atom	x	y	z	
С	-10.4842	0.2977	-0.2389	С	0.6032	-0.3477	0.2105	
Η	-11.4160	-0.2626	-0.3026	Η	0.5890	-1.4422	0.2122	
Η	-10.5549	1.3873	-0.2340	С	1.8718	0.2885	0.1794	
\mathbf{C}	-9.2872	-0.3277	-0.1683	Η	1.8836	1.3838	0.1770	
Η	-9.2614	-1.4226	-0.1738	С	3.0765	-0.3738	0.1330	
\mathbf{C}	-8.0167	0.3437	-0.0835	Η	3.0690	-1.4685	0.1325	
Η	-8.0288	1.4389	-0.0807	С	4.3406	0.2730	0.0721	
С	-6.8124	-0.3001	-0.0061	Η	4.3407	1.3683	0.0738	
Η	-6.8081	-1.3954	-0.0057	С	5.5498	-0.3737	-0.0013	
\mathbf{C}	-5.5472	0.3537	0.0707	Η	5.5582	-1.4682	-0.0055	
Η	-5.5465	1.4484	0.0749	С	6.8067	0.2952	-0.0845	
\mathbf{C}	-4.3417	-0.3011	0.1300	Η	6.7859	1.3902	-0.0878	
Η	-4.3464	-1.3960	0.1241	С	8.0216	-0.3277	-0.1683	
\mathbf{C}	-3.0750	0.3426	0.1797	Η	8.0561	-1.4225	-0.1685	
Η	-3.0660	1.4371	0.1788	С	9.2761	0.3722	-0.2625	
\mathbf{C}	-1.8698	-0.3194	0.2090	Η	9.2227	1.4662	-0.2724	
Η	-1.8815	-1.4144	0.2090	С	10.4887	-0.2217	-0.3354	
\mathbf{C}	-0.6009	0.3183	0.2198	Η	10.5880	-1.3090	-0.3312	
Н	-0.5873	1.4134	0.2209	Н	11.4048	0.3630	-0.4028	

Table S16: $C_{18}H_{20}$ geometry (in Å).

	subsy	stem I		subsystem II				
atom	x	y	z	atom	x	y	z	
С	-10.2566	-0.1748	-3.1129	С	0.5891	-0.2332	2.1222	
Н	-10.0833	0.0411	-4.1805	Η	0.5318	-1.3270	2.1221	
Н	-11.2821	0.1660	-2.8952	С	1.8798	0.3468	1.9709	
Н	-10.2181	-1.2635	-2.9764	Η	1.9426	1.4401	1.9681	
С	-9.2521	0.5277	-2.2536	С	3.0186	-0.3732	1.6858	
Η	-9.2055	1.6187	-2.3451	Η	2.9429	-1.4654	1.6617	
С	-8.3897	-0.0834	-1.4044	С	4.2567	0.1963	1.2729	
Η	-8.4265	-1.1758	-1.3177	Η	4.3384	1.2881	1.2883	
С	-7.3770	0.5939	-0.6388	С	5.2966	-0.5265	0.7373	
Η	-7.3376	1.6852	-0.7218	Η	5.2009	-1.6168	0.6987	
С	-6.4258	-0.0404	0.1145	С	6.4415	0.0456	0.1047	
Η	-6.4641	-1.1332	0.1815	Η	6.5363	1.1362	0.1345	
С	-5.3167	0.6091	0.7362	С	7.3603	-0.6664	-0.6190	
Η	-5.2722	1.7008	0.6644	Η	7.2586	-1.7559	-0.6638	
С	-4.2528	-0.0525	1.3023	С	8.4120	-0.0796	-1.4057	
Η	-4.2947	-1.1459	1.3504	Η	8.5123	1.0114	-1.3646	
С	-3.0338	0.5680	1.6992	С	9.2367	-0.7764	-2.2259	
Η	-2.9868	1.6608	1.6459	Η	9.1253	-1.8658	-2.2696	
С	-1.8789	-0.1206	1.9974	С	10.2815	-0.1748	-3.1129	
Η	-1.9260	-1.2144	2.0250	Η	10.0903	-0.4214	-4.1708	
С	-0.5928	0.4753	2.1195	Η	11.2834	-0.5728	-2.8833	
Н	-0.5405	1.5690	2.0927	Н	10.3141	0.9187	-3.0199	

Table S17: $C_{20}H_{24}$ geometry (in Å).

2 Energy, Density, and Dipole Differences

Sys	tem	100	01	റി	03	01	05	06	07	08	-0	o10
n	d	111	er	ez	69	64	60	eo	er	60	69	610
6	1	-2784	-517	-12	2							
0	3	-1173	-851	-63	1							
8	1	-2703	-636	-152	-7	1						
0	3	-2234	-600	-144	-52	3						
10	1	-2827	-757	-313	-65	-3	2					
10	5	5354^{\dagger}	-623	-220	-84	-45	1					
19	1	-2882	-749	-376	-112	-5	2	2				
12	5	5409^{\dagger}	-654	-358	-150	-55	-22	4				
1/	1	-2951	-782	-405	-201	-1	2	2	2			
14	7	121986^{\dagger}	-723	-332	-165	-83	-40	-10	2			
16	7	202558^{\dagger}	-689	-349	-233	-154	-77	-36	-38	-4		
18	9	529592^{\dagger}	-678	-338	-249	-559	-86	-51	-24	-2	6	
20	9	-2157.706	-654	-342	-250	-147	-143	$-1\overline{27}$	-45	-28	-4	8

Table S18: Energy difference (ΔE , in mE_h) between the KS-DFT and FDE(EO,5ft) methods with different levels of basis set overlap.

n - number of carbon atoms; d - number of conjugated double bonds. [†]One or more SCF cycles failed to converge during the freeze-and-thaw iterations.

Sys	tem		1	0	ŋ	4	۲	C	-	0	0	10
n	d	m	el	e2	e3	e4	eə	eb	eí	eð	e9	e10
6	1	4.74	2.23	0.11	0.00							
0	3	6.98	2.54	0.61	0.00							
8	1	5.65	2.29	0.93	0.08	0.00						
	3	6.56	2.40	1.17	0.58	0.00						
10	1	6.00	2.72	2.00	0.66	0.06	0.00					
	5	16.00^{\dagger}	2.54	1.66	0.95	0.44	0.00					
19	1	6.65	2.65	2.21	0.87	0.10	0.00	0.00				
12	5	18.26^{\dagger}	2.72	2.44	1.47	0.69	0.37	0.00				
14	1	6.82	2.77	2.23	1.47	0.12	0.01	0.00	0.00			
14	7	44.99^{\dagger}	2.76	2.47	1.66	1.05	0.64	0.26	0.00			
16	7	54.41^{\dagger}	2.86	2.54	2.45	1.76	1.04	0.46	0.55	0.01		
18	9	67.99^{\dagger}	2.92	2.56	2.54	3.14	1.27	0.83	0.50	0.20	0.00	
20	9	6.37	2.98	2.61	2.59	1.91	1.88	1.59	0.80	0.40	0.20	0.00

Table S19: Integrated absolute density difference (Δ^{abs} , in e) for the FDE(EO,5ft) method with different levels of basis set overlap.

n - number of carbon atoms; d - number of conjugated double bonds. [†]One or more SCF cycles failed to converge during the freeze-and-thaw iterations.

Table S20: Absolute dipole difference $(|\Delta \mu|, \text{ in } D)$ for the FDE(EO,5ft) method with different levels of basis set overlap.

Sys	tem	722	01	<u></u>	02	04	05	26	07	08	o 0	o10
n	d	111	er	ez	eə	e 4	eo	eo	er	eo	69	ero
6	1	17.32	9.14	0.06	0.00							
0	3	39.09	7.80	3.08	0.00							
8	1	26.34	9.27	2.16	0.20	0.00						
0	3	46.78	16.14	6.18	3.35	0.00						
10	1	30.73	11.94	7.28	1.76	0.14	0.00					
10	5	106.17^{\dagger}	22.49	12.19	7.23	0.08	0.01					
19	1	43.31	12.41	9.49	1.16	0.21	0.00	0.00				
12	5	121.73^{\dagger}	26.32	22.88	11.34	5.20	3.10	0.01				
1/	1	46.25	13.60	9.75	3.34	0.23	0.00	0.00	0.00			
14	7	272.74^{\dagger}	33.11	29.84	16.62	10.39	6.54	2.70	0.00			
16	7	311.68^{\dagger}	35.45	31.80	30.20	18.65	10.21	4.06	5.88	0.05		
18	9	407.66^{\dagger}	43.75	38.98	38.28	10.28	15.44	10.15	6.25	2.60	0.01	
$\overline{20}$	9	64.86	41.79	37.43	36.98	23.31	23.19	18.78	8.87	3.72	$2.\overline{54}$	0.04

n - number of carbon atoms; d - number of conjugated double bonds.

[†]One or more SCF cycles failed to converge during the freeze-and-thaw iterations.

3 Extended Monomer Truncation



Figure S1: $|\Delta \mu|$ for the FDE(EO,5ft) method with different levels of basis set overlap for (a) alkane-like systems, and (b) conjugated alkenes. The dashed line is the dipole difference threshold of 0.25 D.

4 DZP-Truncated Basis Data



Figure S2: Number of basis functions for the fragments of the conjugated alkenes in the supermolecular basis (sup.), the DZP truncated basis (DZP), and the largest extended monomer basis truncation (exp.).



Figure S3: Computation time (on 8 processors) for the KS-DFT method, and various levels of basis set truncations of the FDE(EO) method. FDE(EO,e) represents the largest extended monomer basis truncation.