

Rural Postman (RPP)

Input: Undirected graph $G = (V, E)$ with edge lengths and a set $R \subseteq E$ of required edges.

Find: Shortest tour containing all required edges.

Solution structure

If the graph $G \langle R \rangle$ consisting only of edges in R and incident vertices has

- c connected components and
- b odd-degree vertices,

then an optimal tour visits

$$d \geq \max\{c, b/2\}$$

edges additionally to those in R .

Theoretical results

Theorem 1. RPP cannot be polynomial-time reduced to instances of size $d^{O(1)}$, unless $\text{coNP} \subseteq \text{NP/poly}$.

Theorem 2. Given $\varepsilon > 0$, any RPP instance I can be reduced to an instance I' in $O(|V|^3)$ time such that

- I' has $2b + O(c/\varepsilon)$ vertices, and
- α -approximate solutions for I' yield $\alpha(1 + \varepsilon)$ -approximate solutions for I , for any $\alpha \geq 1$.

On approximate data reduction for the Rural Postman Problem

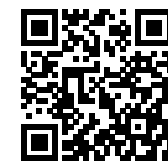
R. van Bevern, T. Fluschnik, and O. Yu. Tsidulko, *Networks*, in press.

Experiments show that

vertex count decreases to 60 %

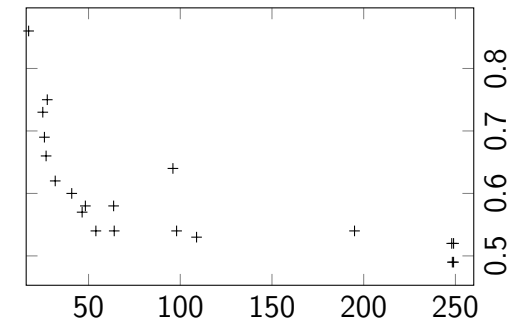
solution cost increases by 1 %

on instances with few components of required edges.



Experimental results

Average component size of $G \langle R \rangle$ vs fraction of remaining vertices:



Example: before and after

