



The sensitivity of ocean-bottom gravimeters at deep waters to mass changes in a synthetic hydrocarbon reservoir

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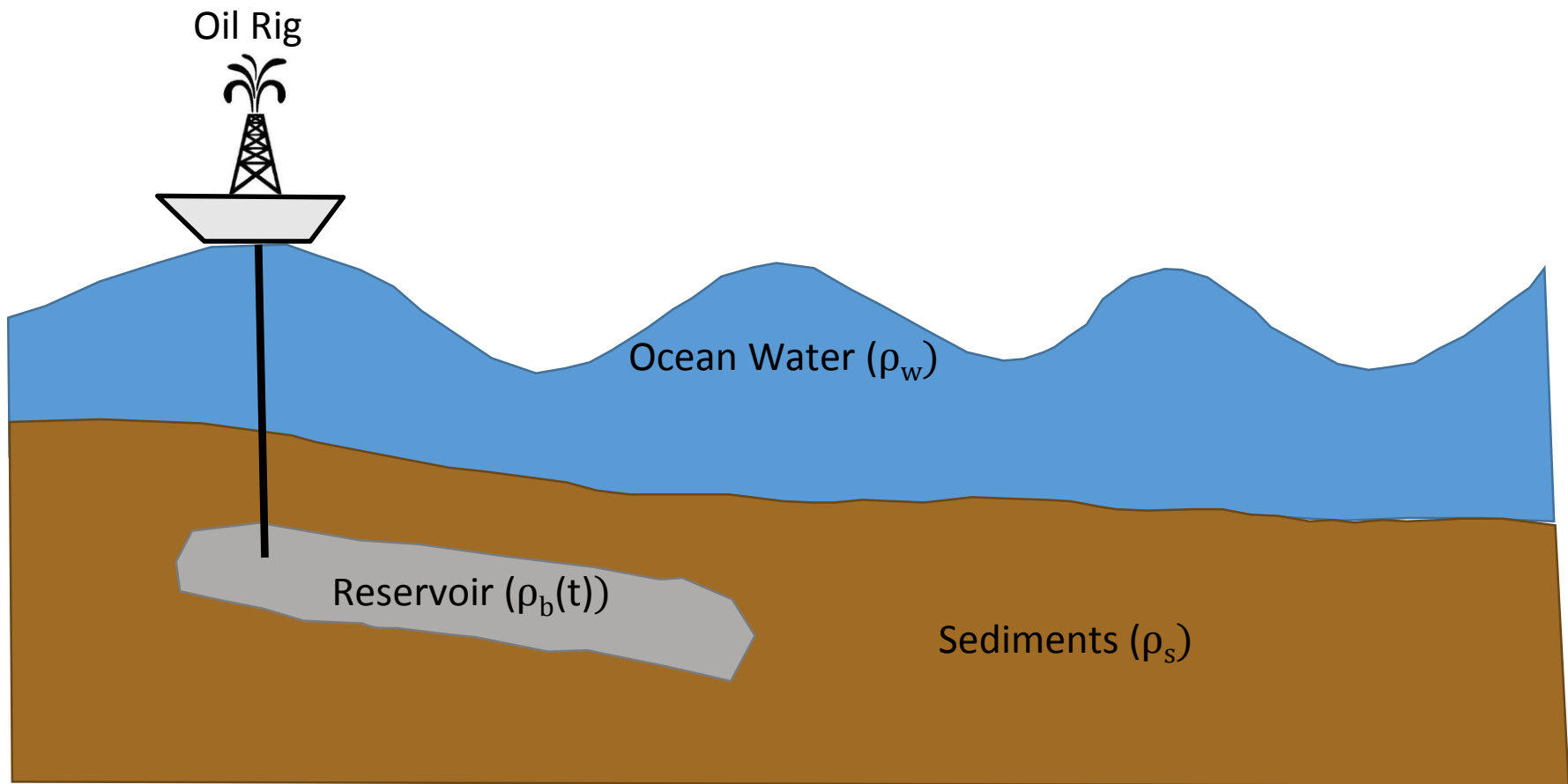
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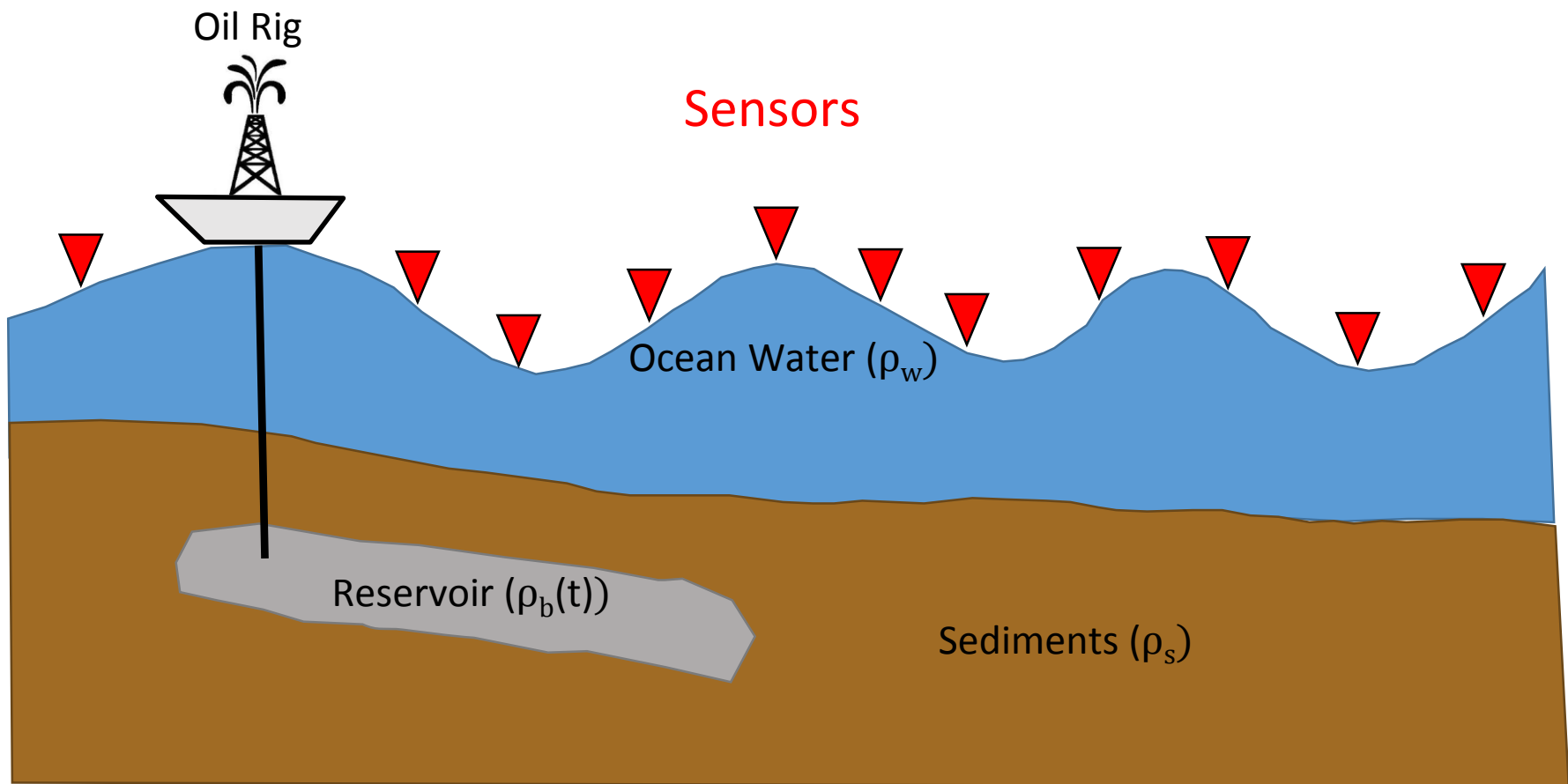
Summary

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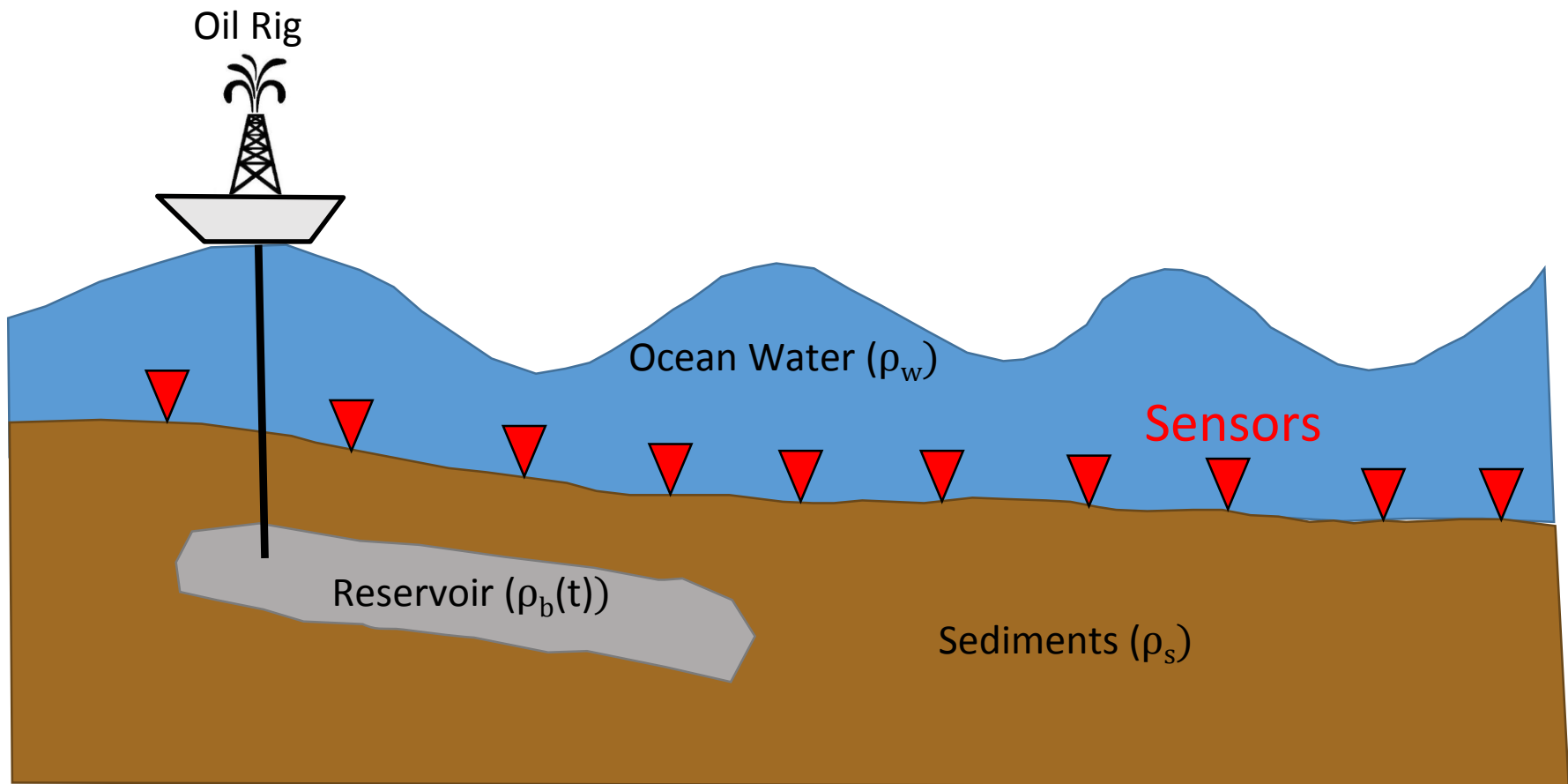
Introduction



Introduction

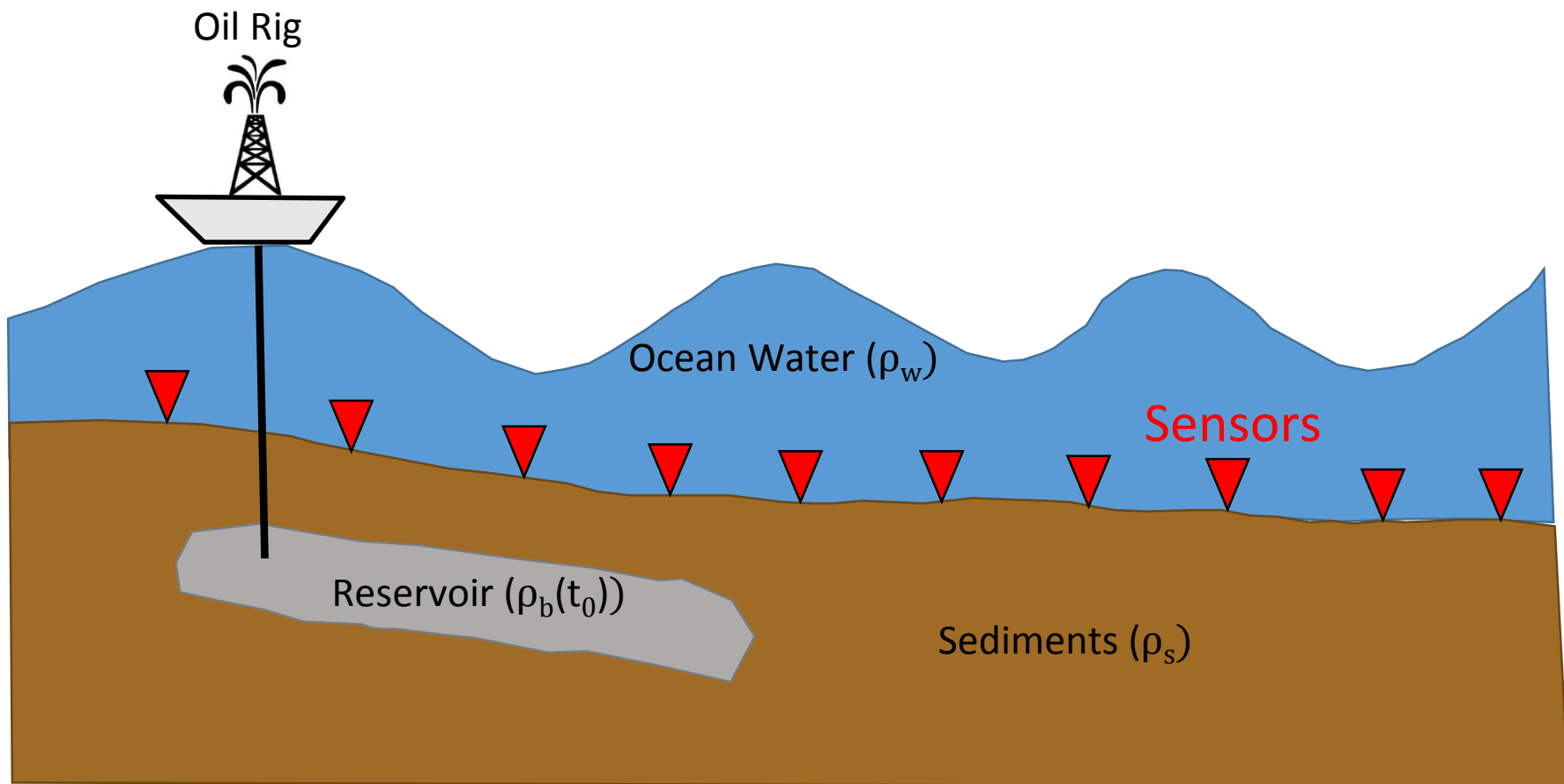


Introduction

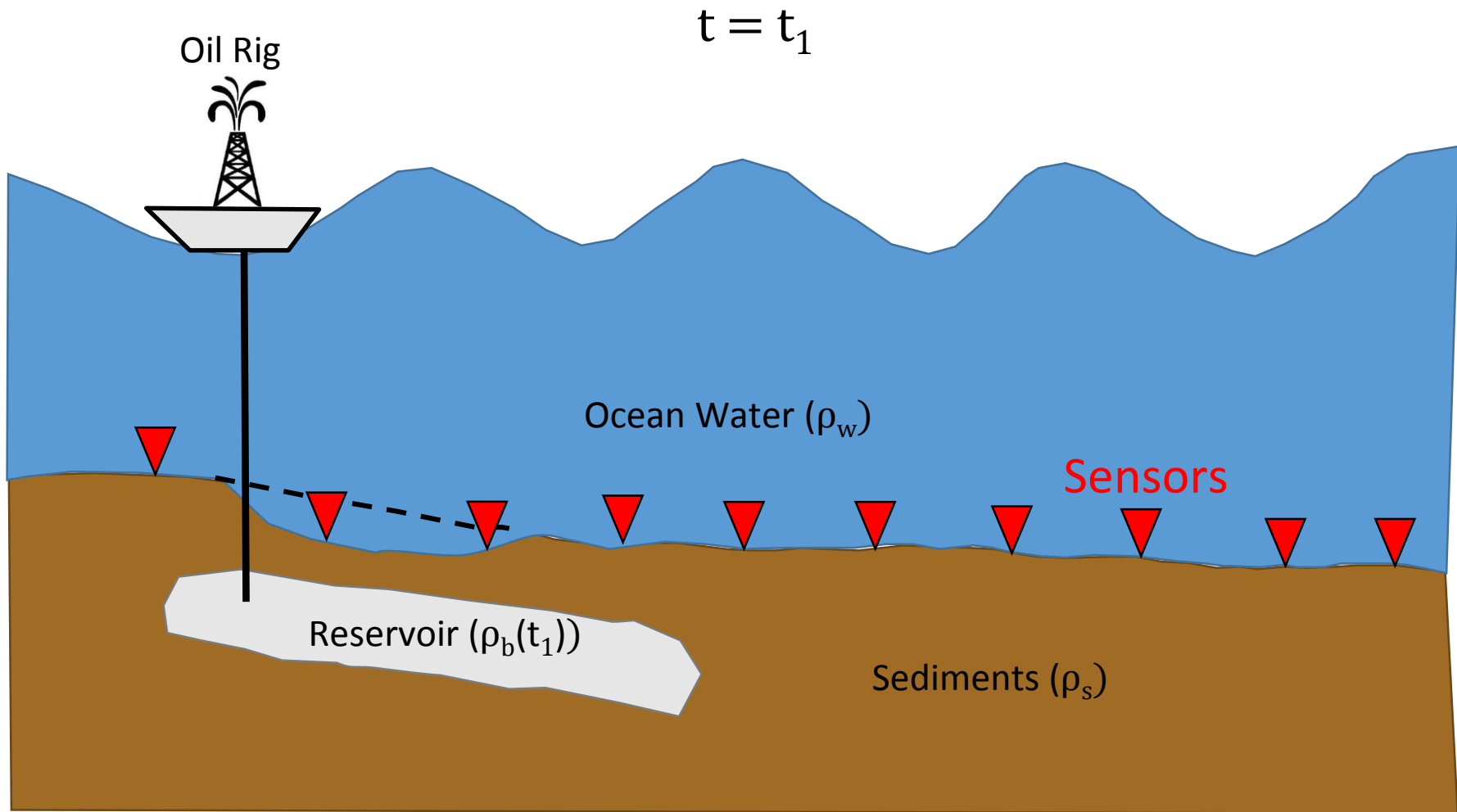


Introduction

$$t = t_0$$



Introduction



Objectives

Main Objective

Study the parameter sensitivity ($3 \mu\text{Gal}$) of a 4D ocean-bottom gravity acquisition via forward modelling.

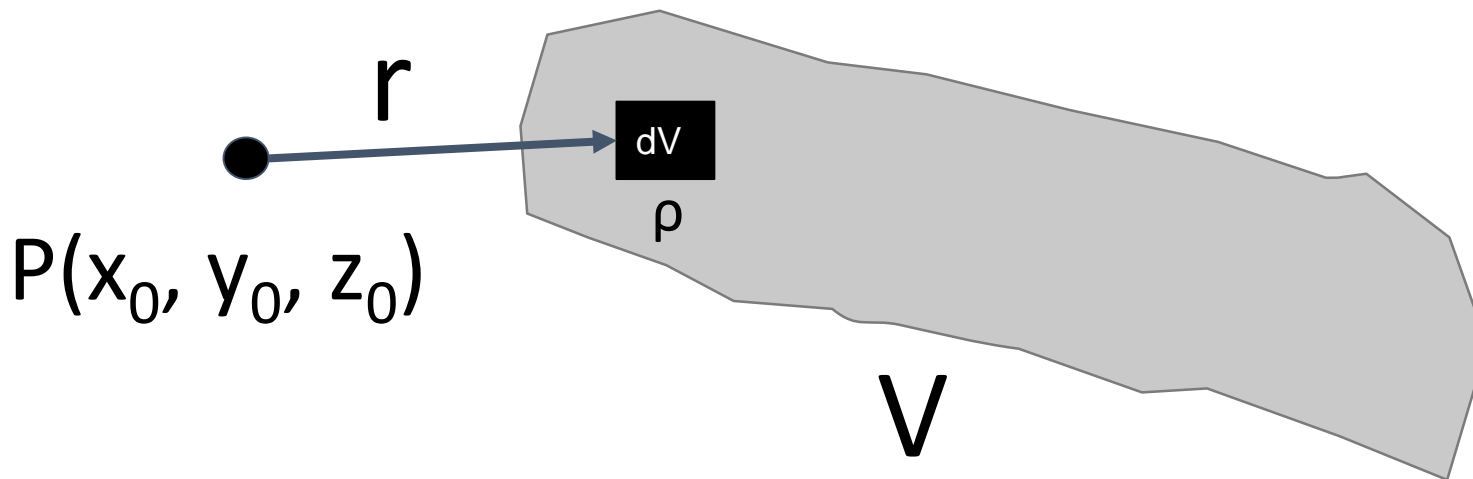
Studied Parameters:

Water thickness

Ocean-bottom subsidence

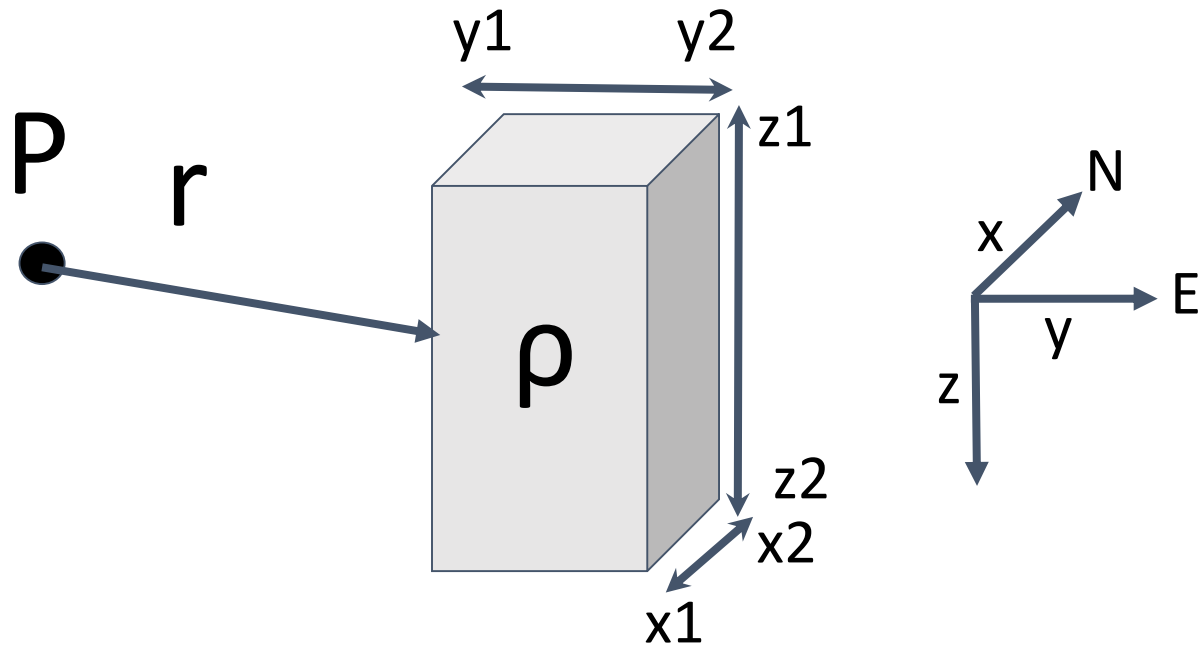
Reservoir fluid substitution

Methodology



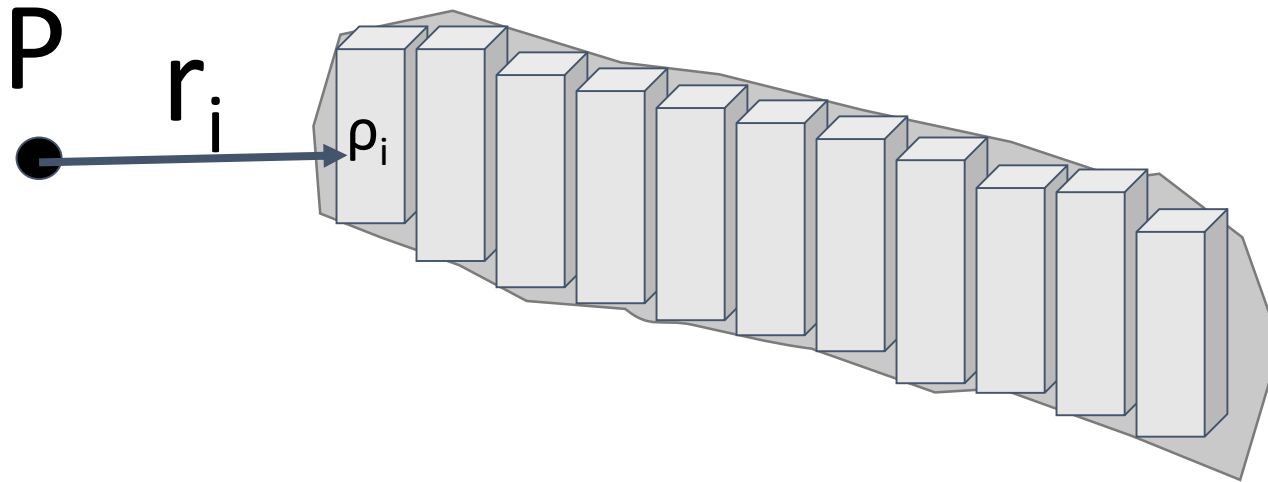
$$g_z(P) = \gamma \rho \int \int \int_V \frac{z - z_0}{r^3} dV$$

Methodology



$$g_z(P) = \gamma \rho \left[x \ln(y + r) + y \ln(x + r) - z \tan^{-1} \left(\frac{xy}{zr} \right) \right]_{x_1}^{x_2} \Big|_{y_1}^{y_2} \Big|_{z_1}^{z_2}$$

Methodology

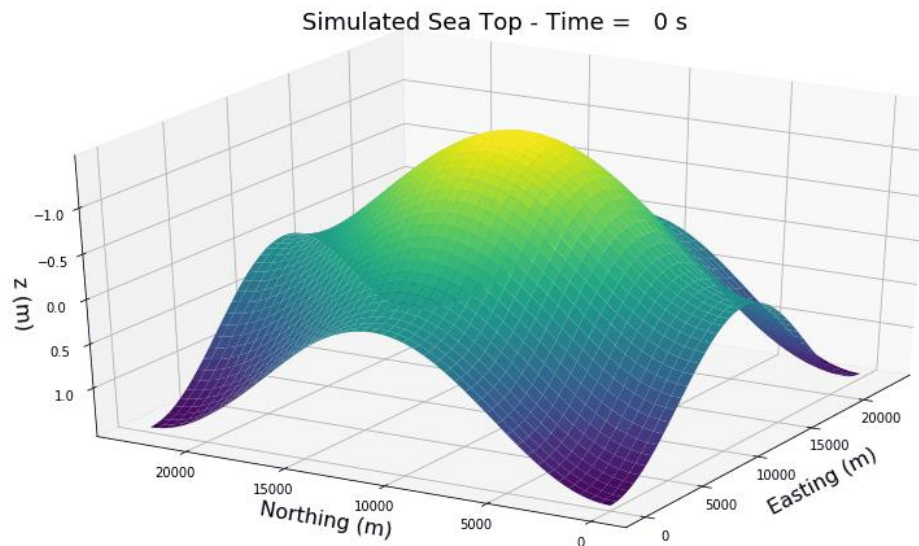


$$g_z(P) = \gamma \sum_{i=1}^N \rho_i \left[x \ln(y + r_i) + y \ln(x + r_i) - z \tan^{-1} \left(\frac{xy}{zr_i} \right) \right] \begin{vmatrix} x_{2i} & y_{2i} & z_{2i} \\ x_{1i} & y_{1i} & z_{1i} \end{vmatrix}$$

Methodology - Water Top

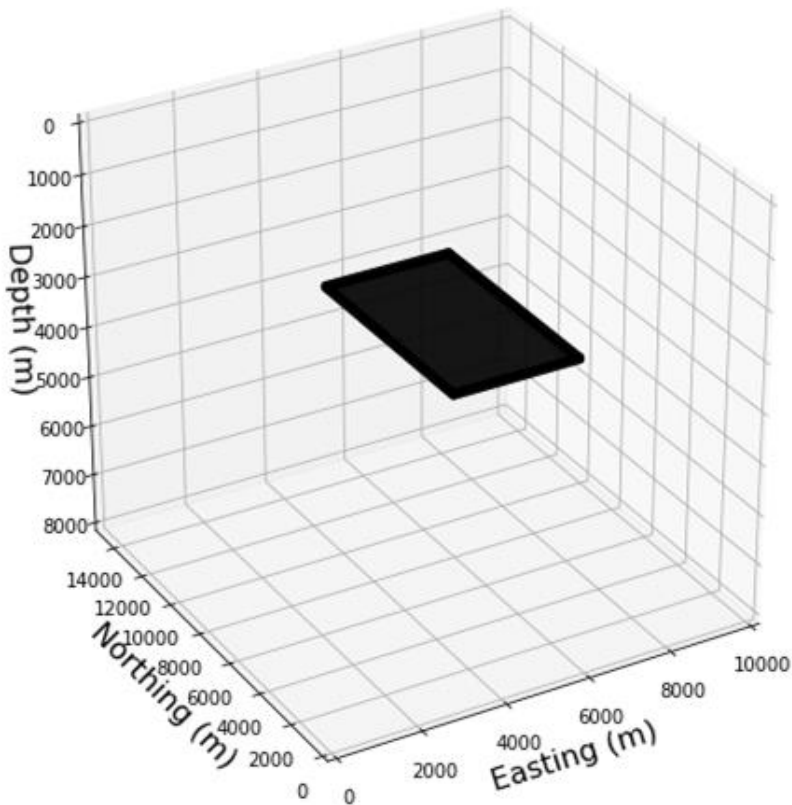
$$z_w(x, y, t) = \frac{A}{2} \left\{ \cos \left(\frac{2\pi}{L_x} x + \frac{2\pi}{T} t \right) + \cos \left(\frac{2\pi}{L_y} y + \frac{2\pi}{T} t \right) \right\}$$

- A: amplitude;
- L_x : Model size in x;
- L_y : model size in y;
- T: period.



Methodology - Fluid Substitution

$$\rho_b(t) = \phi[\alpha(t)\rho_f + (1 - \alpha(t))\rho_o] + (1 - \phi)\rho_r$$



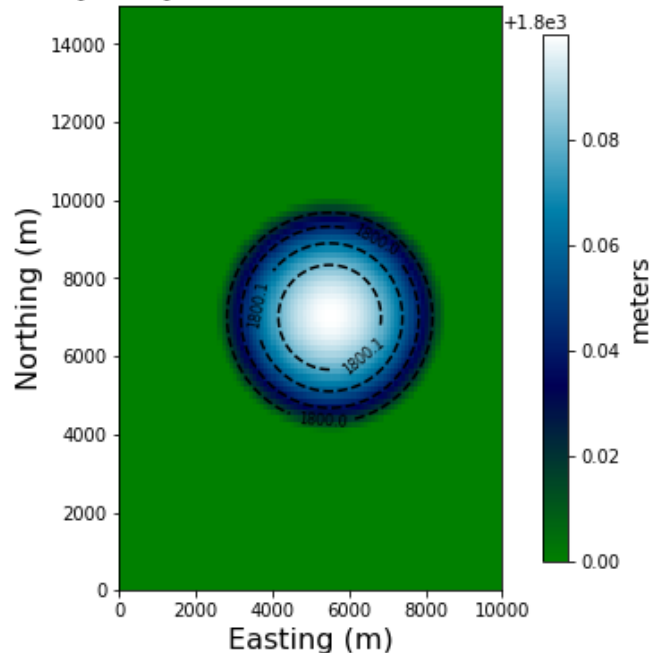
- $\rho_b(t)$: bulk density;
- ϕ : porosity;
- $\alpha(t)$: fluid substitution percentage;
- ρ_f : fluid density;
- ρ_o : oil density;
- ρ_r : rock density.

Methodology - Subsidence

$$z(t_1) = -\left[\frac{(x - x_c)^2}{a^2} + \frac{(y - y_c)^2}{b^2}\right] + z_{max}$$

$$a = \frac{-R_x}{\sqrt{z_{max} - z(t_0)}} \quad b = \frac{-R_y}{\sqrt{z_{max} - z(t_0)}}$$

Bathymetry with Subsidence of 0.1 meter

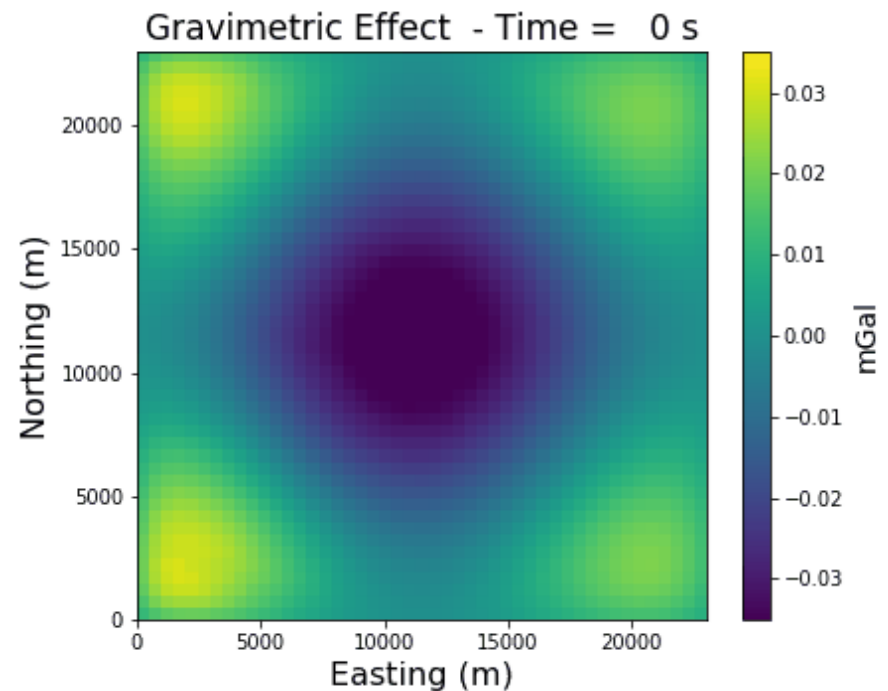
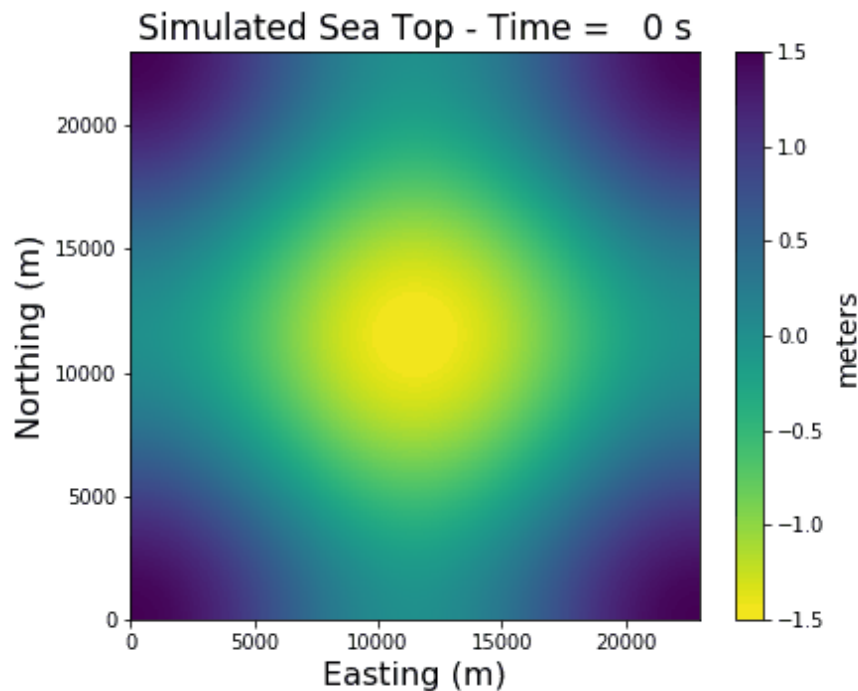


- $z(t_1)$: bathymetry after subsidence.
- x_c : central point in x;
- y_c : central point in y;
- z_{max} : maximum subsidence;
- R_x : subsidence radius in x;
- R_y : subsidence radius in y;
- $z(t_0)$: original bathymetry.

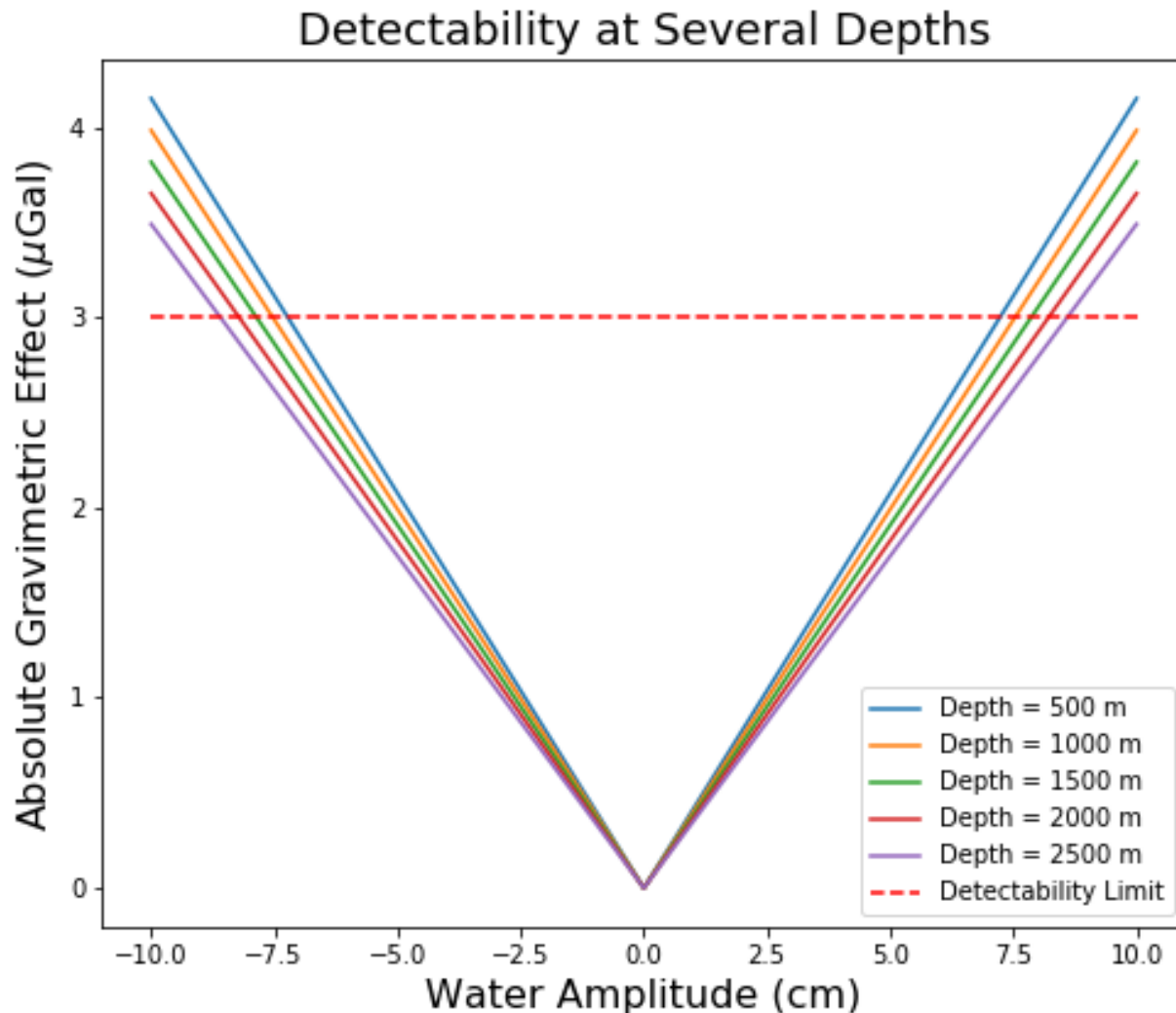
Results - Water Effect

$$z_w(x, y, t) = \frac{A}{2} \left\{ \cos \left(\frac{2\pi}{L_x} x + \frac{2\pi}{T} t \right) + \cos \left(\frac{2\pi}{L_y} y + \frac{2\pi}{T} t \right) \right\}$$

- $A = 1.5 \text{ m}$
- $L_x = L_y = 23,000 \text{ m}$
- $T = 7,500 \text{ s}$



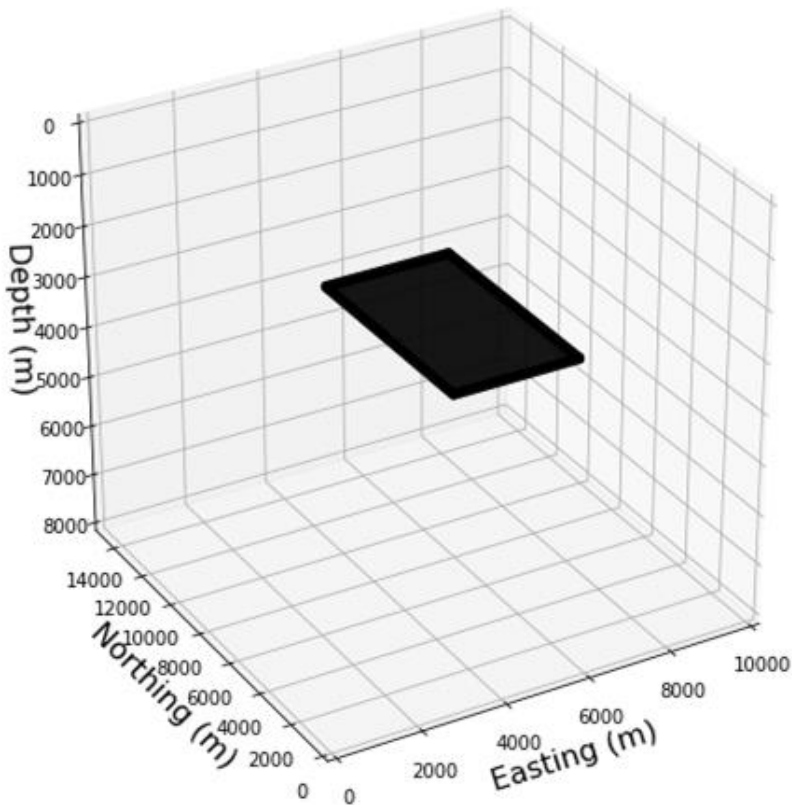
Results - Water Effect



- $x = y = 11,700$ m
- $L_x = L_y = 23,000$ m
- $T = 7,500$ s

Results - Density Changes in Reservoir

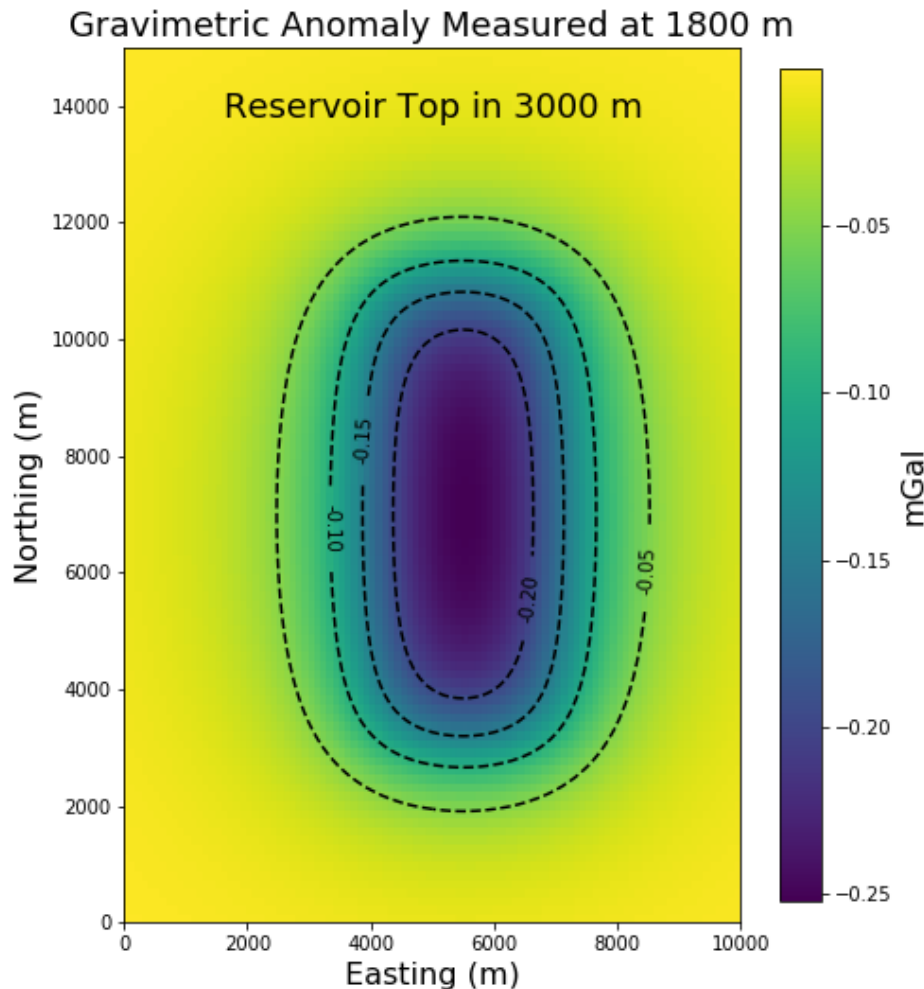
$$\rho_b(t) = \phi[\alpha(t)\rho_f + (1 - \alpha(t))\rho_o] + (1 - \phi)\rho_r$$



- ϕ : 20%
- $\alpha(t_0)$: 0% (before production)
- ρ_f : 1060 kg/m³ (brine)
- ρ_o : 850 kg/m³ (oil)
- ρ_r : 2350 kg/m³ (sandstone)
- $\rho_b(t_0)$: 2050 kg/m³

Results - Density Changes in Reservoir

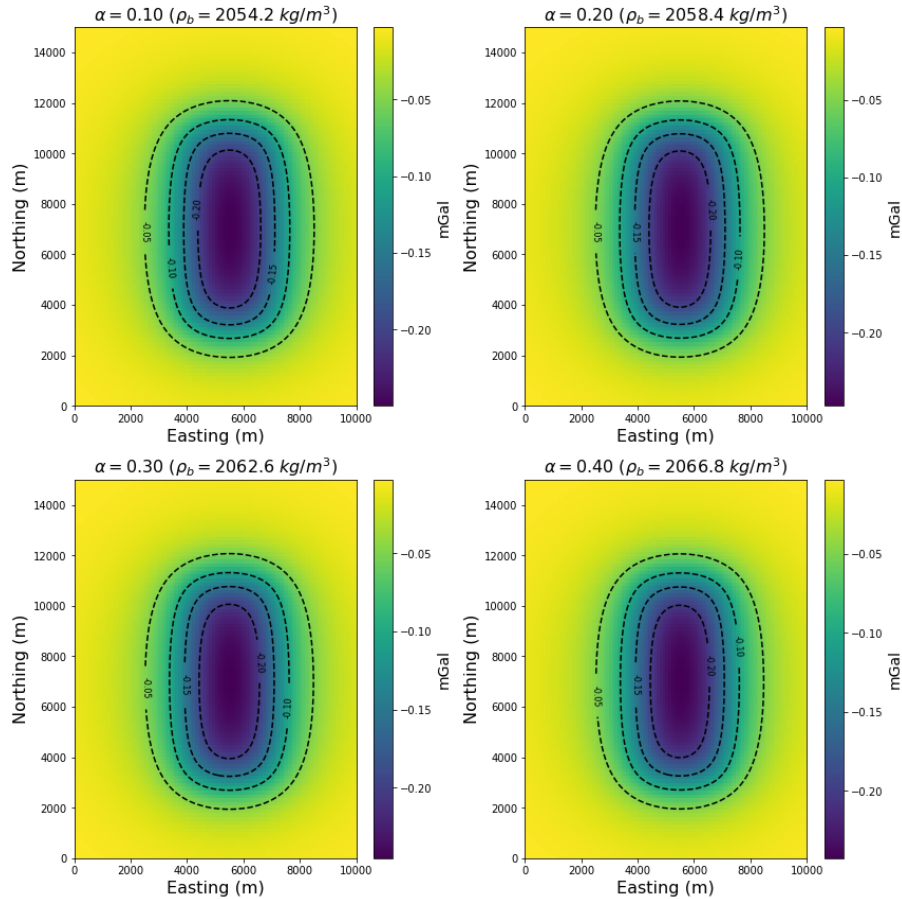
$$\rho_b(t) = \phi[\alpha(t)\rho_f + (1 - \alpha(t))\rho_o] + (1 - \phi)\rho_r$$



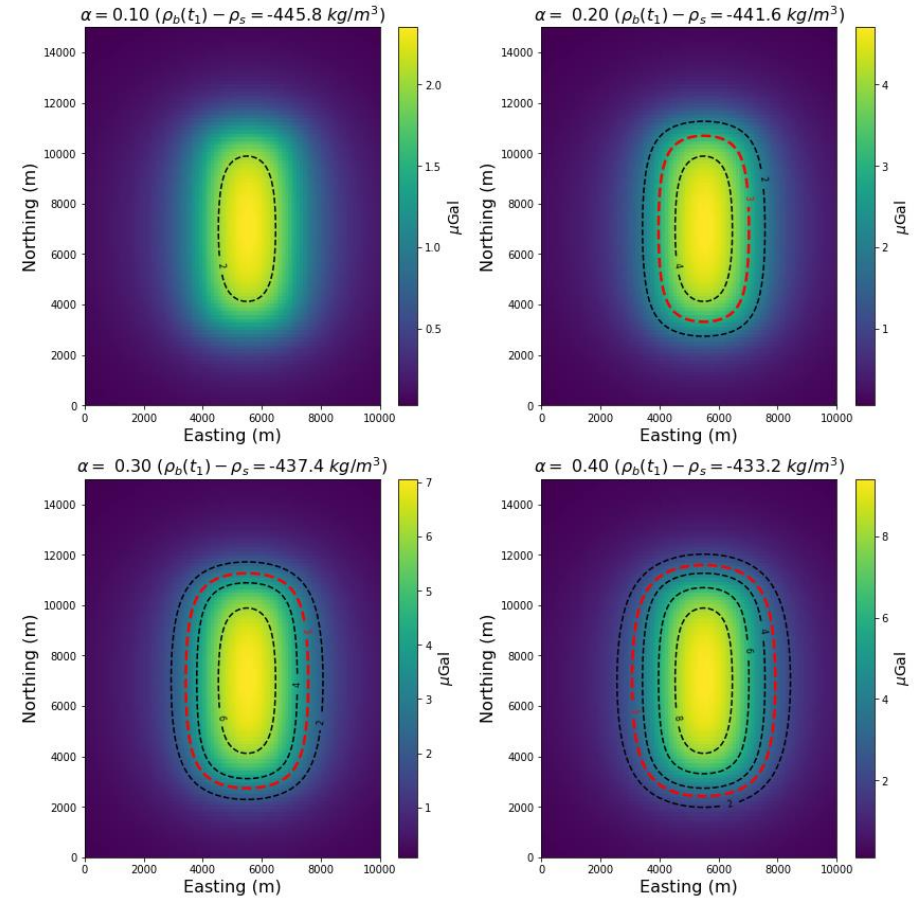
- ϕ : 30%
- $\alpha(t_0)$: 0%
- ρ_f : 1060 kg/m³
- ρ_o : 850 kg/m³
- ρ_r : 2350 kg/m³
- $\rho_b(t_0)$: 2050 kg/m³
- ρ_{back} : 2500 kg/m³

Results - Density Changes in Reservoir

Gravimetric Effect After α Variation. Reservoir Top at 3 km Depth

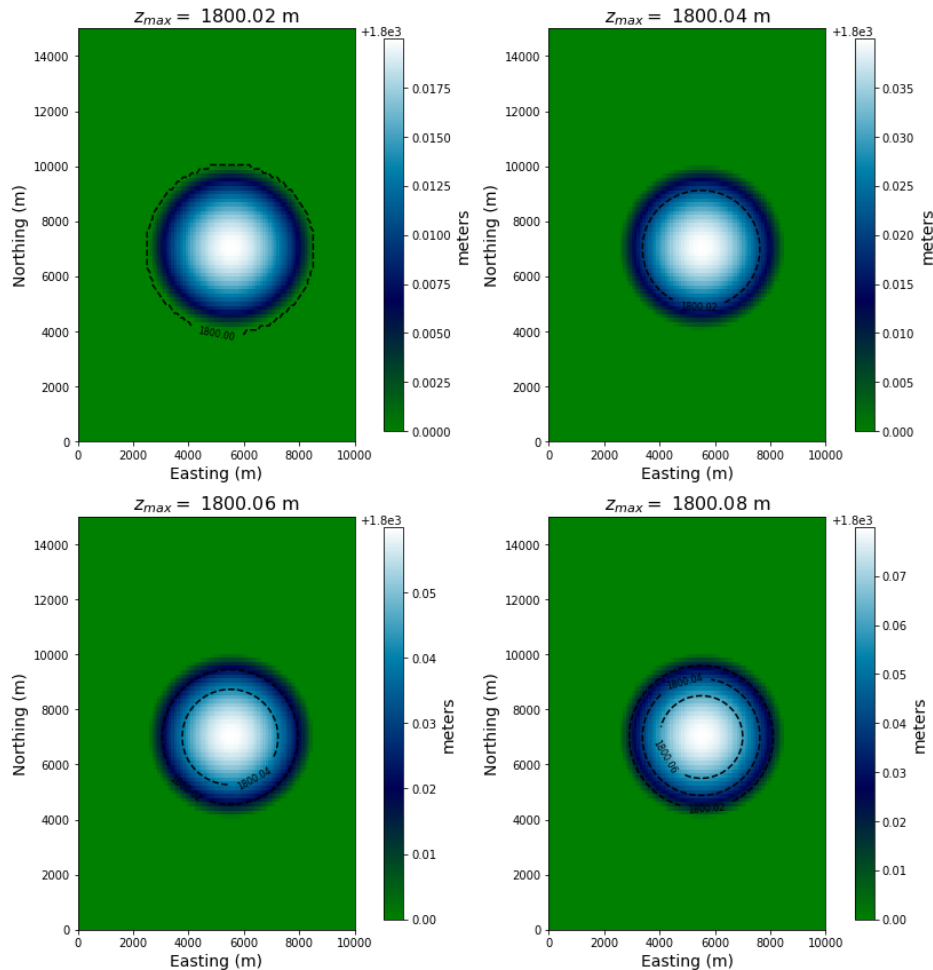


Gravimetric Difference due to α Variation. Reservoir Top at 3 km Depth



Results - Subsidence Effect

Bathymetry After Subsidence



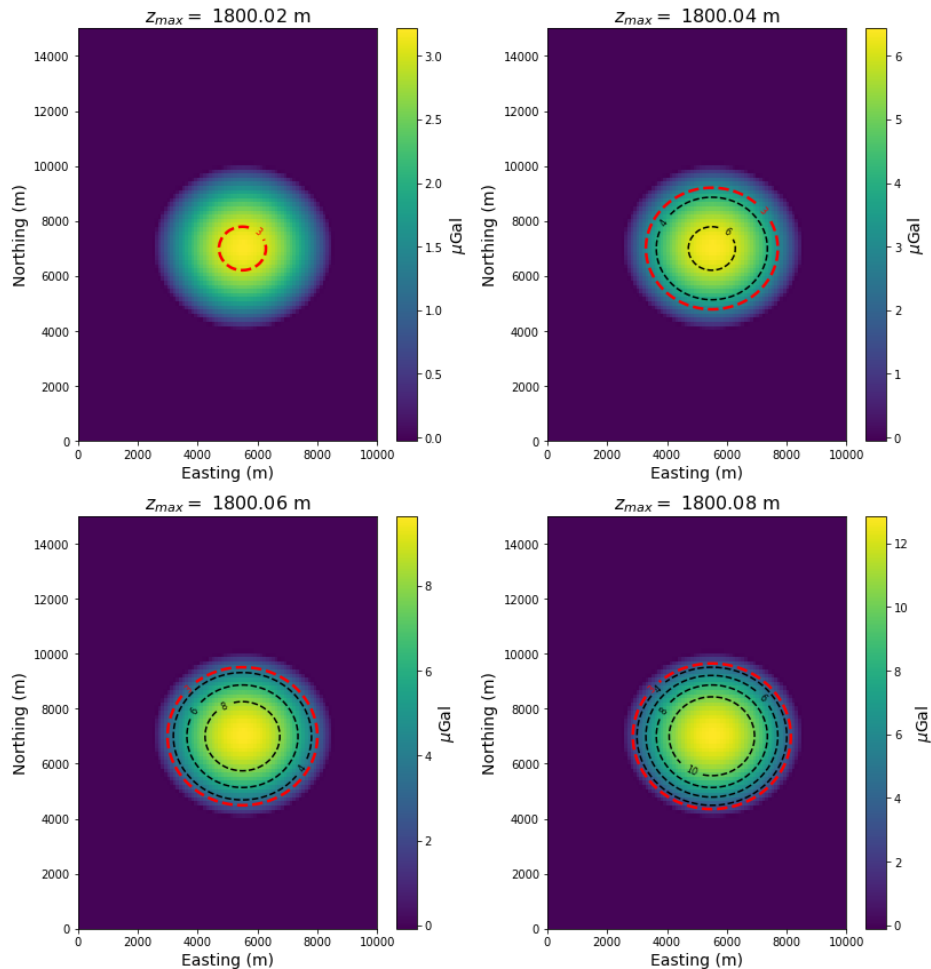
$$z(t_1) = -\left[\frac{(x - x_c)^2}{a^2} + \frac{(y - y_c)^2}{b^2}\right] + z_{max}$$

$$a = \frac{-R_x}{\sqrt{z_{max} - z(t_0)}} \quad b = \frac{-R_y}{\sqrt{z_{max} - z(t_0)}}$$

- x_c : 7,000 m
- y_c : 5,500 m
- $R_x = R_y$: 3,000 m
- z_{obs} : 1,800 m

Results - Subsidence Effect

Gravimetric 4D Effect due to Subsidence



$$z(t_1) = -\left[\frac{(x - x_c)^2}{a^2} + \frac{(y - y_c)^2}{b^2}\right] + z_{max}$$

$$a = \frac{-R_x}{\sqrt{z_{max} - z(t_0)}} \quad b = \frac{-R_y}{\sqrt{z_{max} - z(t_0)}}$$

- x_c : 7,000 m
- y_c : 5,500 m
- $R_x = R_y$: 3,000 m
- z_{obs} : 1,800 m

Conclusions

- Variations in water surface in a magnitude of few cm could affect the data.
- For the reservoir model used, detectability is reached when the substitution from oil to salty water is between 10% and 20%.
- For a sea-bottom originally flat in 1,800 m, a subsidence of few cm could be detected.
- This methodology can be very useful in reservoir monitoring and in guaranteeing the safety of offshore oil facilities in Brazil.

Acknowledgements



THANK YOU