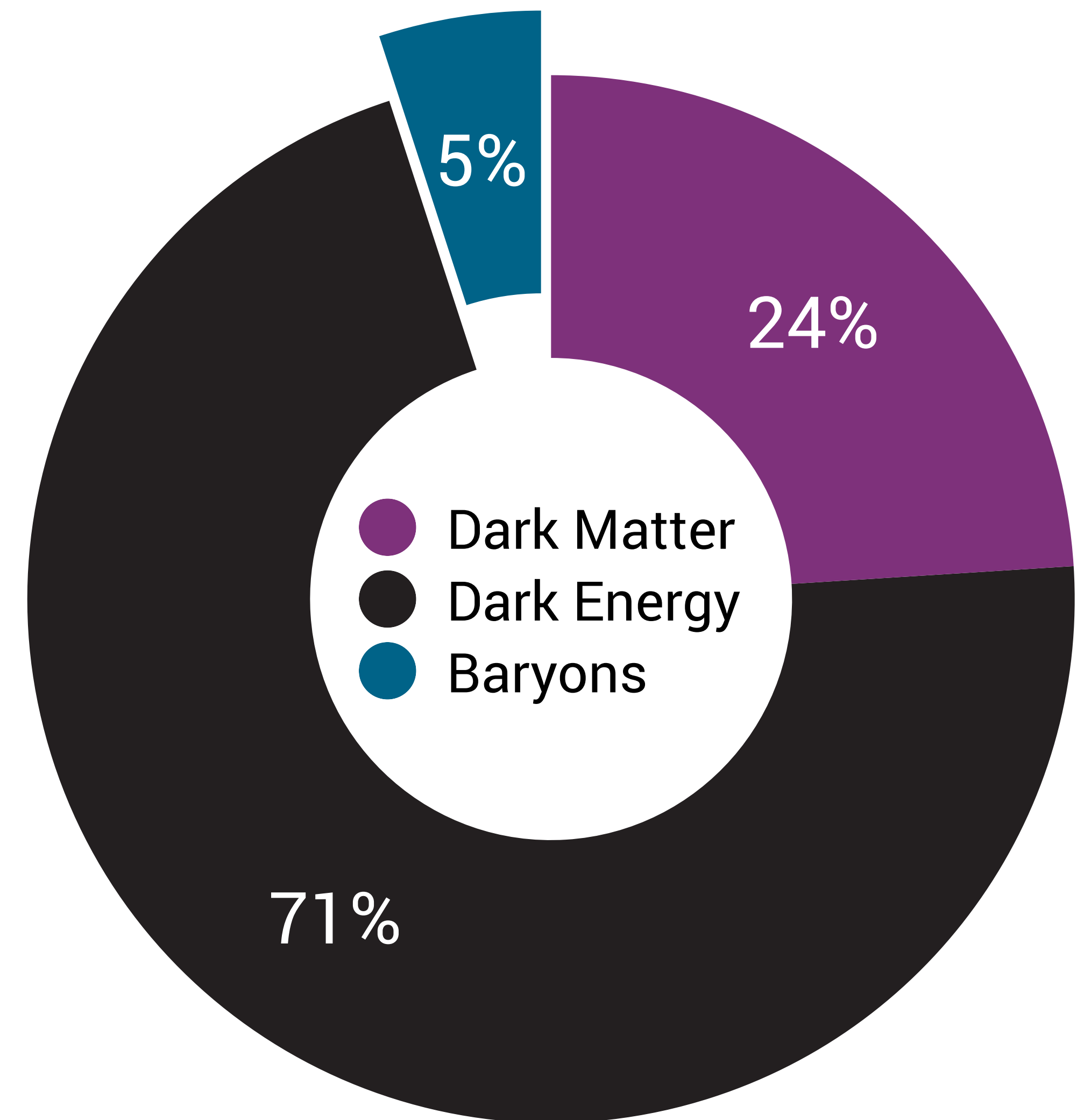


Simulating the Universe

Josh Borrow

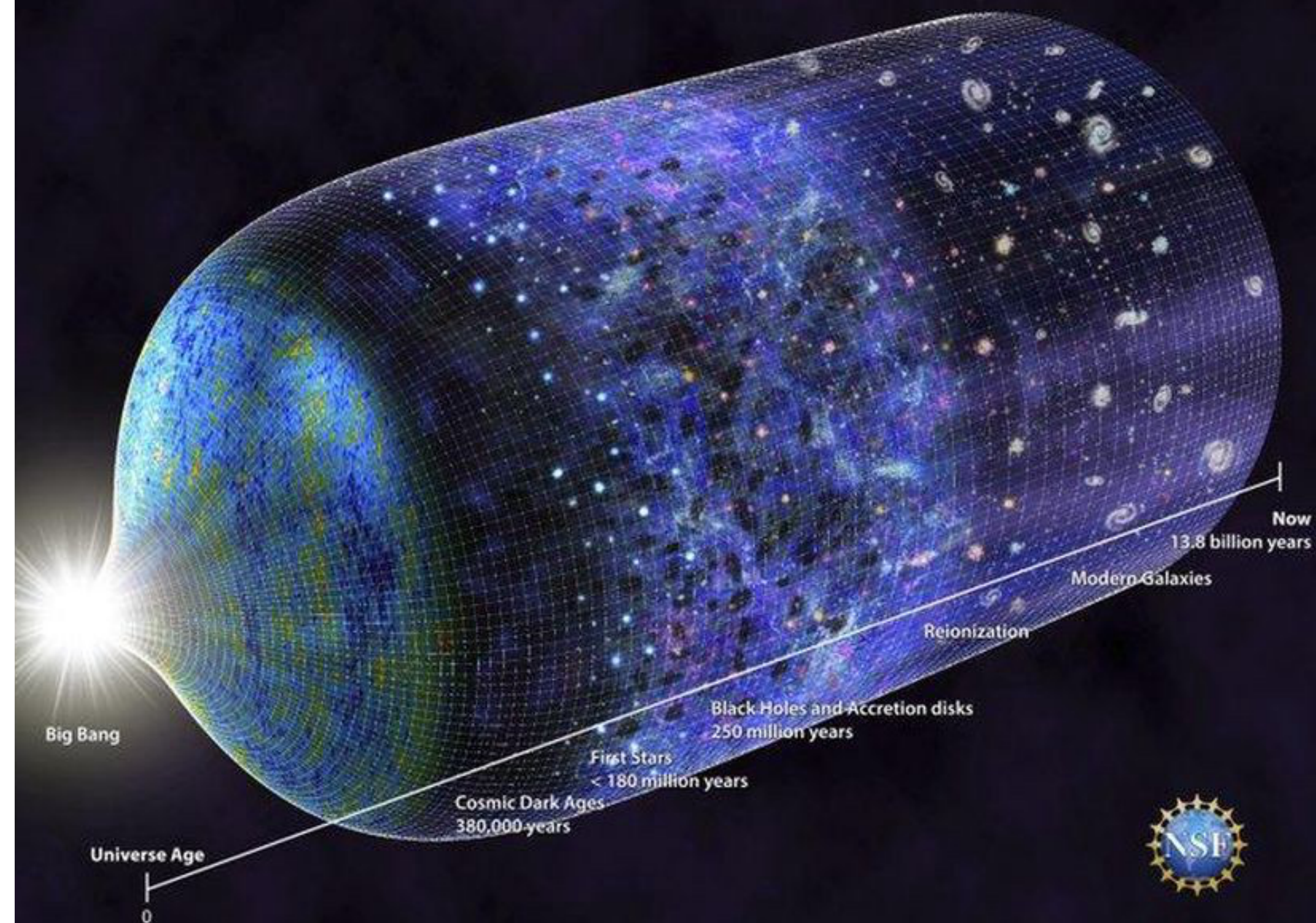
What is the Universe Made of?

- Can't see the majority of the Universe
- Complete nightmare



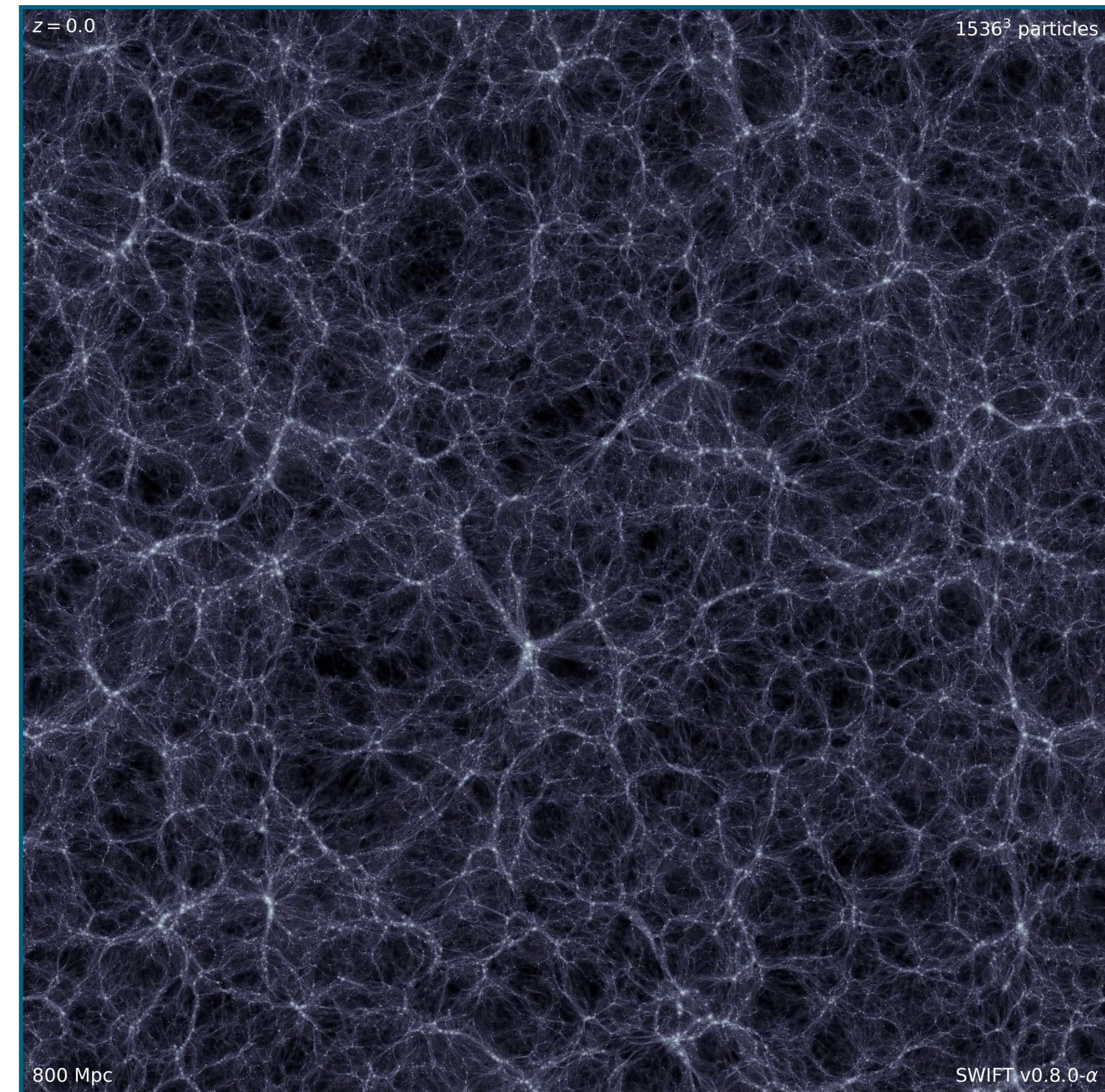
Dark Energy

- Honestly, nobody has a clue about this one
- Affects growth of large-scale structure
- Particle physics estimates differ by a factor of 10^{120}
- Thankfully this doesn't actually change galaxy formation much



Dark Matter

- Dominates gravitational attraction in the Universe
- Probably a WIMP
- Can be modelled as a cold, collision-less fluid
- Important: cannot 'cool'



Baryons!

- Everything else
- Gas, stars, black holes, planets, people...
- We can see these, so they are quite important.



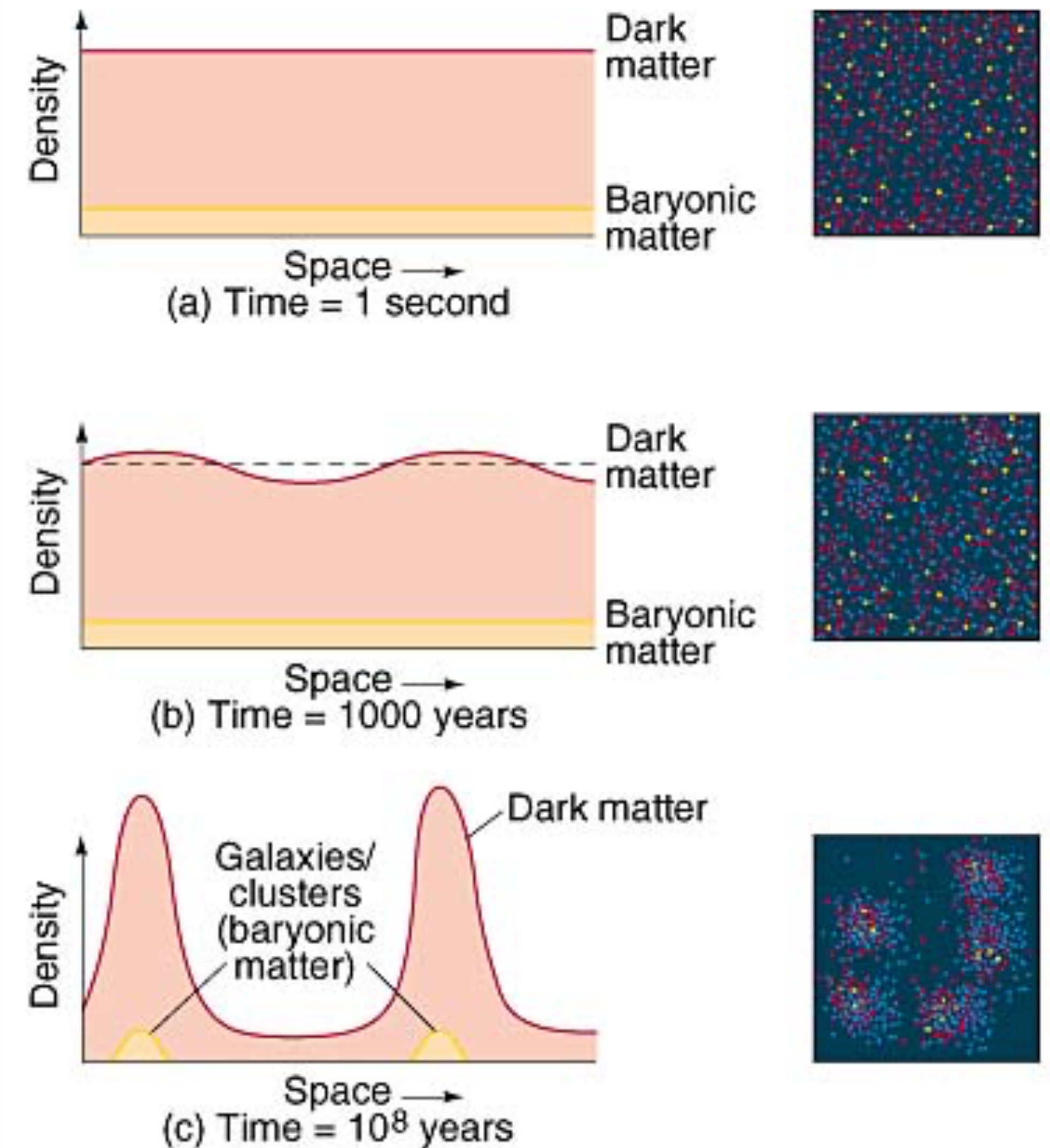
Galaxy Formation

- Where do galaxies come from?
- Dark matter and dark energy are actually quite easy, the difficult bit is the baryons.
- How can we connect cosmology (amount of stuff) to observables (e.g. distribution of masses of galaxies)?



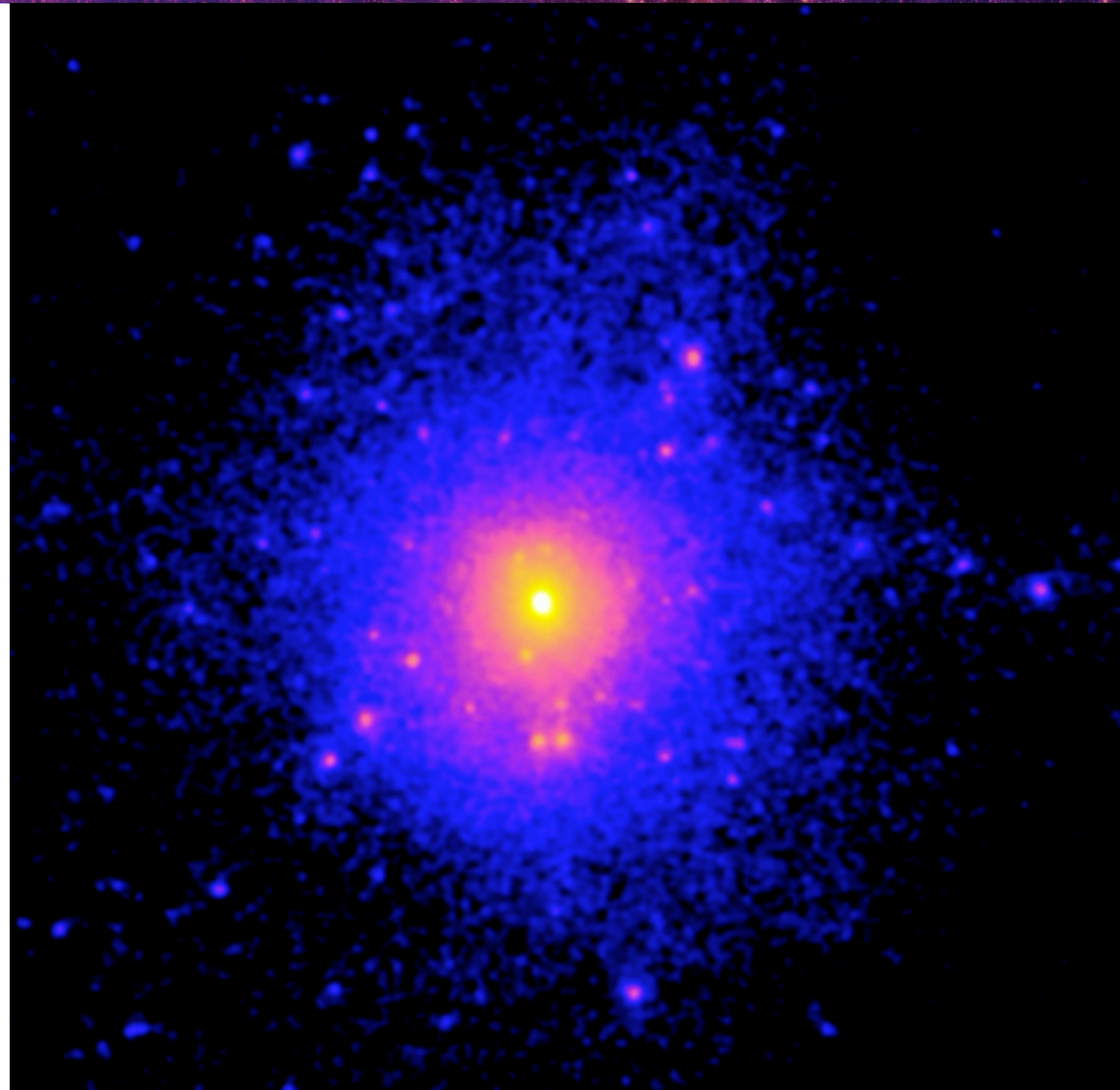
Dark Matter

- Dark matter drives galaxy formation
- Dense dark matter halos form
- These merge to form larger halos
- Gas falls into these halos and makes galaxies



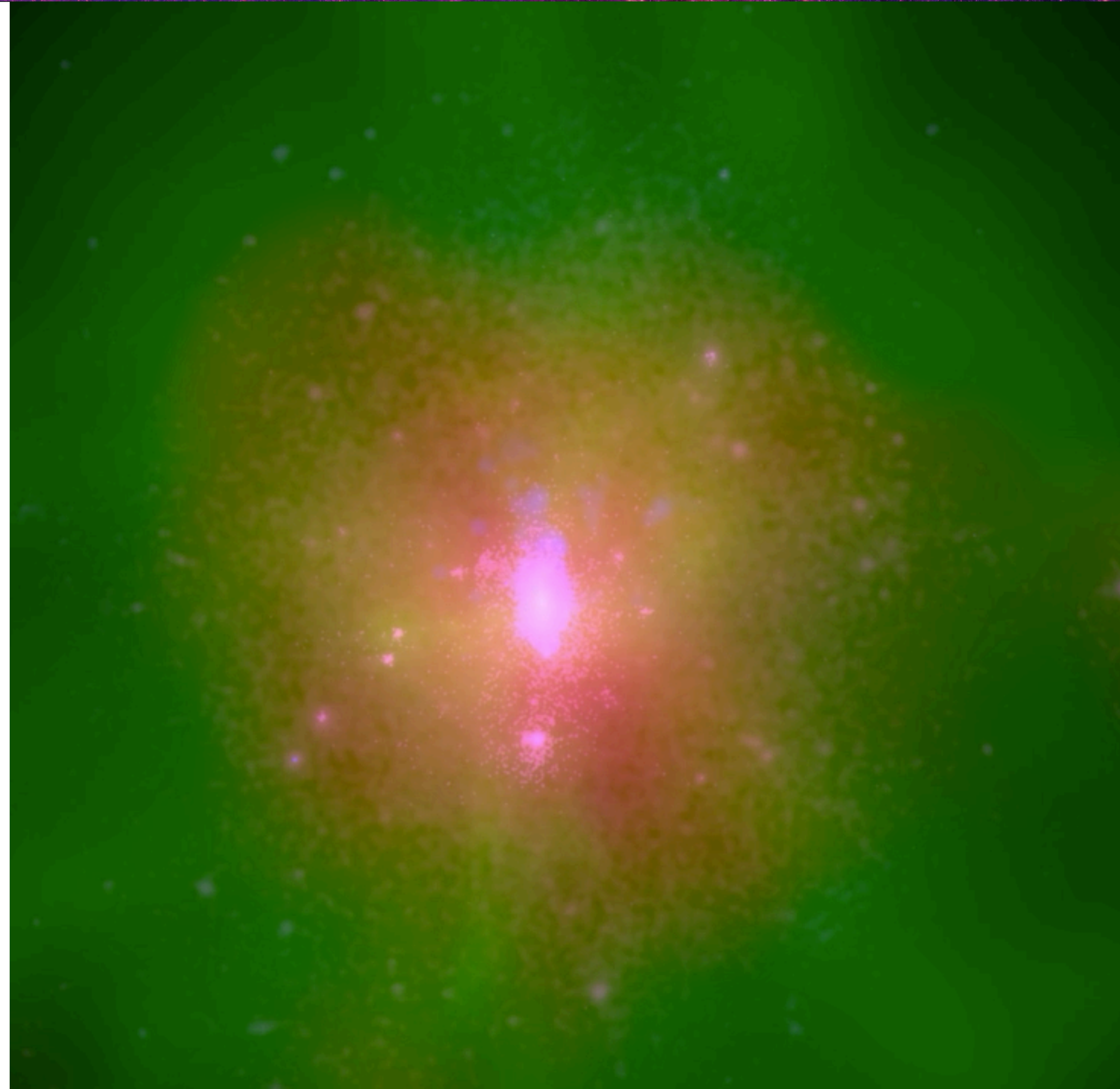
Dark Matter Halos

- Dark matter is collisionless
- Cannot 'cool'
- Hence halos are spherical (conservation of angular momentum)
- They have a very well characterised density profile (NFW)!



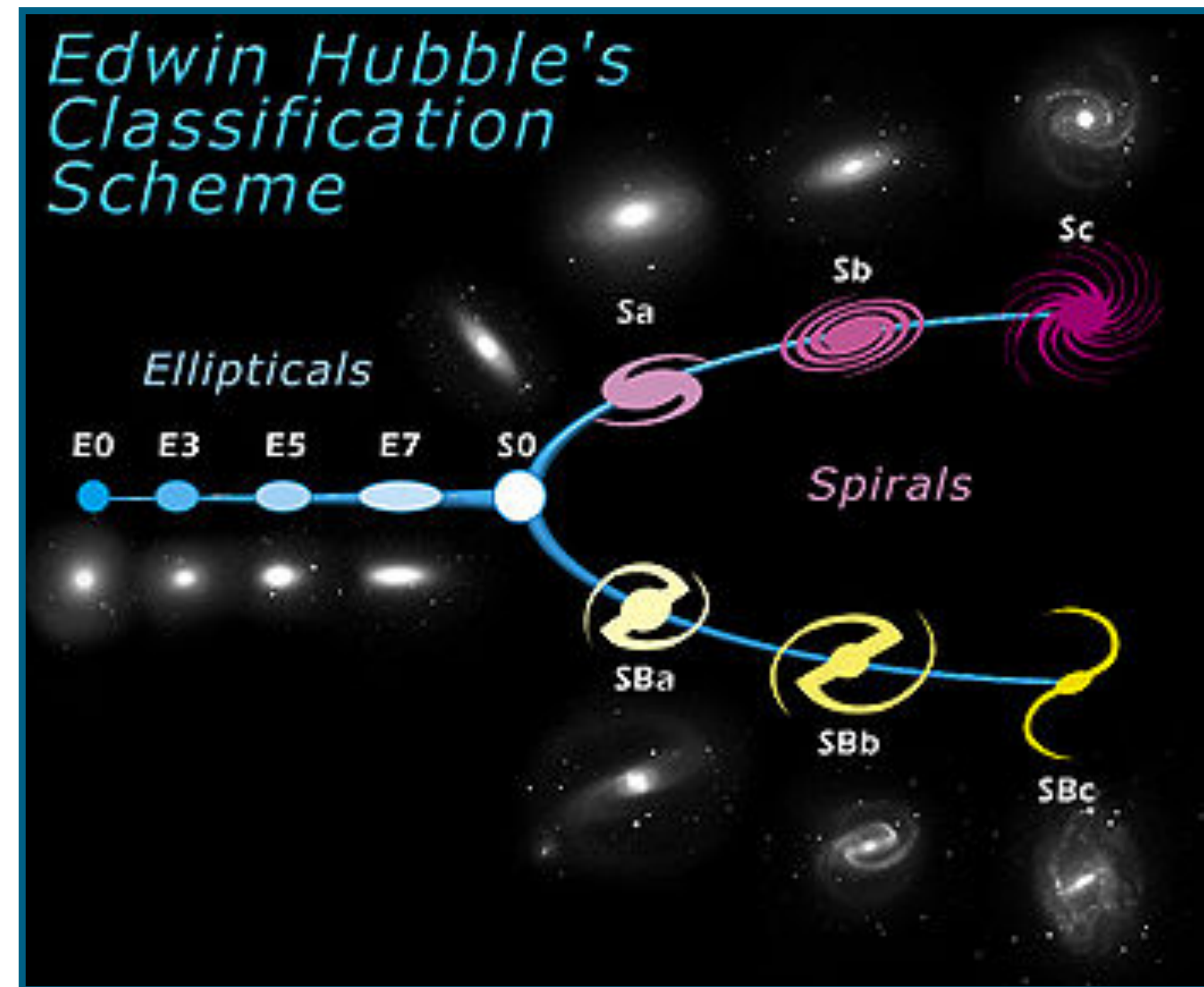
Gas Cooling

- Gas, unlike dark matter, *can* lose angular momentum
- This allows it to fall into the deepest part of the halo's potential well
- This makes the gas even more dense
- The energy loss from cooling is nonlinear!



Galaxies?

- So we've got a dense ball of dark matter
- A dense disk of gas
- That's a galaxy, right?



I think
you'll
find
it's a
bit
more
complicated
than
that

Ben Goldacre

Bestselling author of *Bad Science* and *Bad Pharma*

A visualization of the cosmic web, showing a complex network of filaments and clusters of galaxies. The filaments are primarily red and pink, while the clusters are more blue and white. The background is a deep blue with scattered white stars.

Galaxies in the Real Universe

Timescales: The Biggest Killer

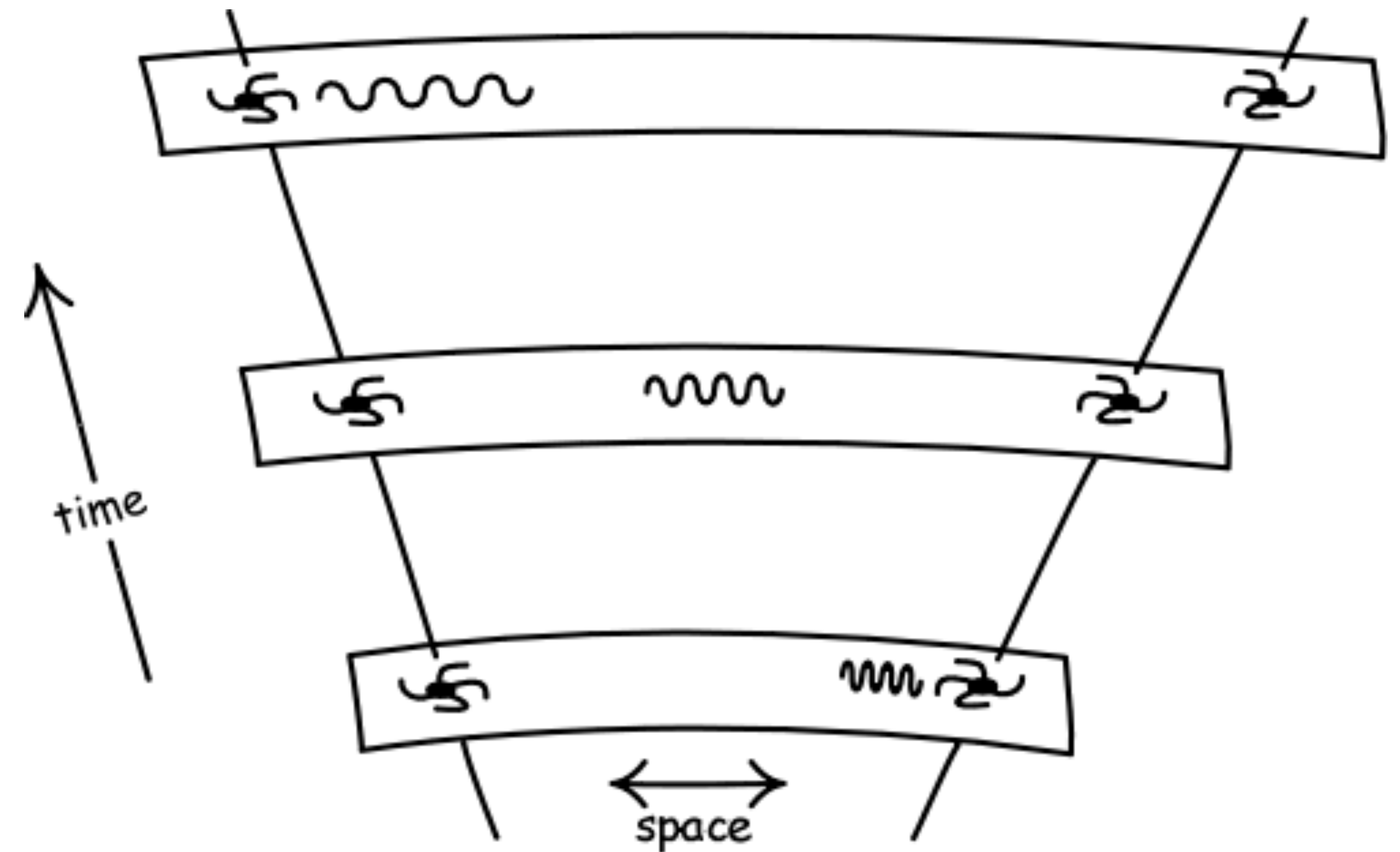
- Typical timescales in galaxy formation are ~100s of millions of years
- Your grand⁴⁰⁰⁰⁰⁰children will be able to see significant changes in the galaxy population

TODAY

WHEN I DIE (HOPEFULLY IN QUITE A WHILE)

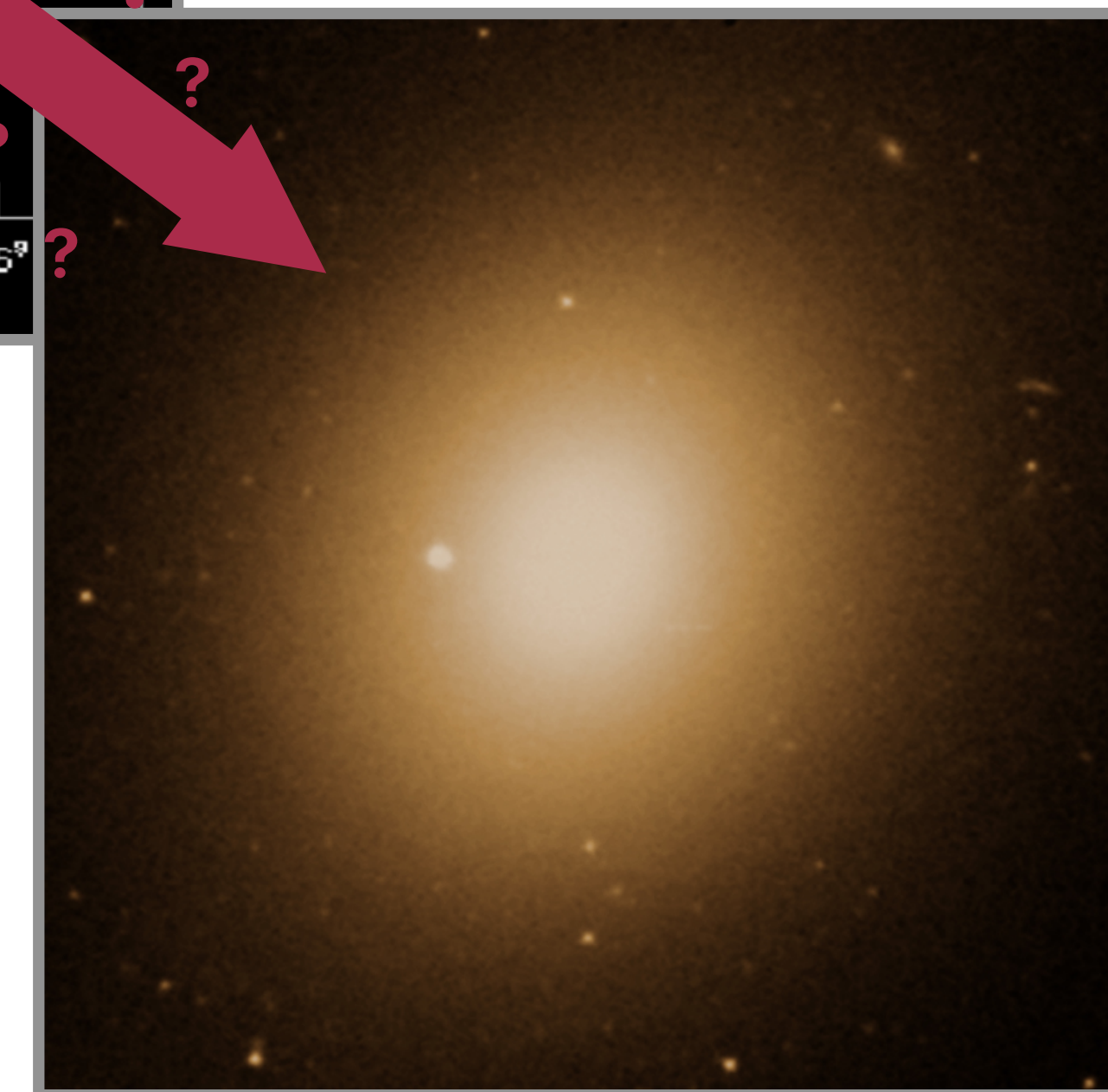
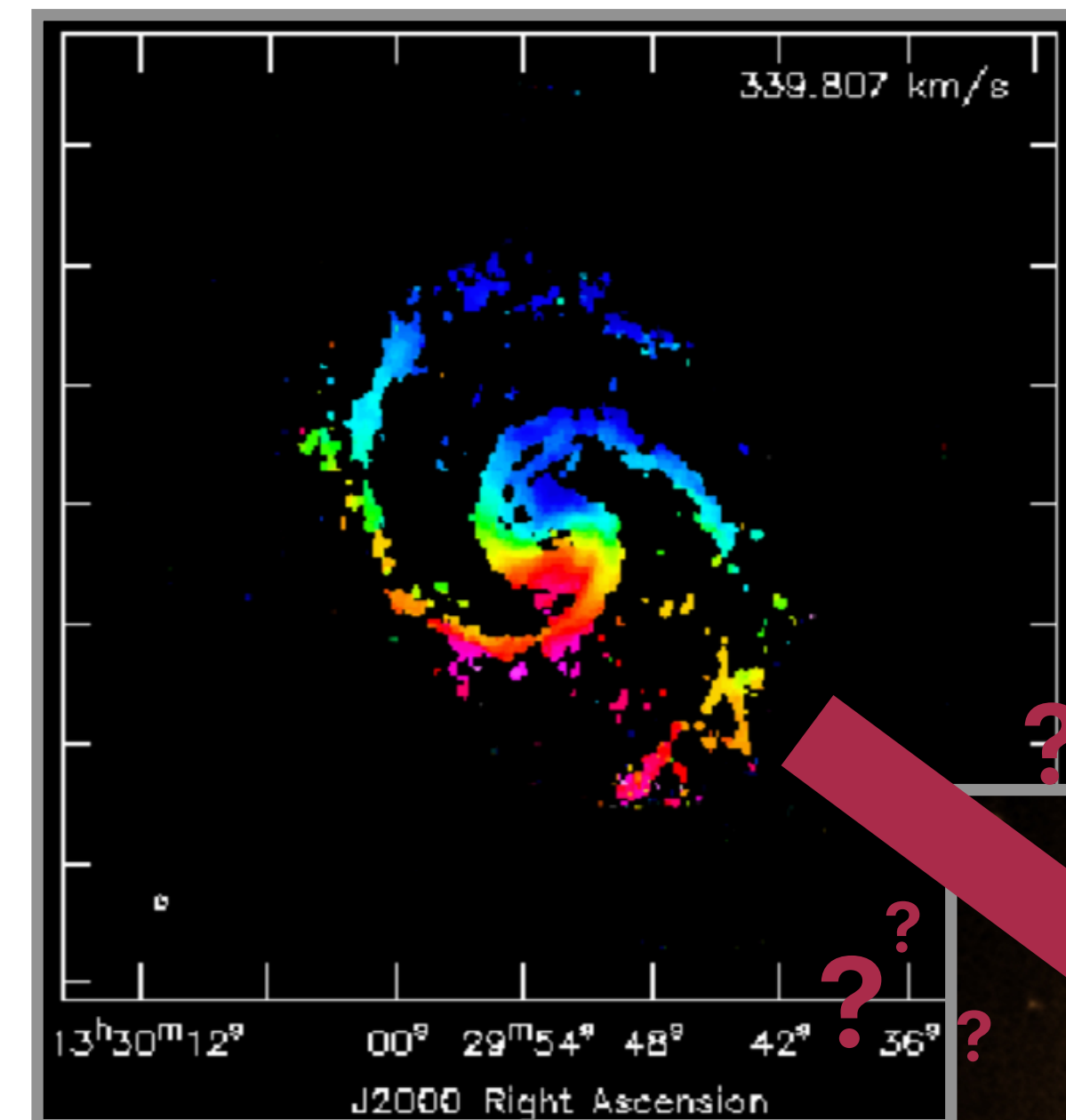
Addendum: Cosmological Redshift

- Astronomers use redshift as a proxy for distance
- Hubble flow, $v = H_0 d$ gives recession velocity, which then gives redshift
- Objects at higher redshifts are also seen further back in time because of light's finite speed of travel.



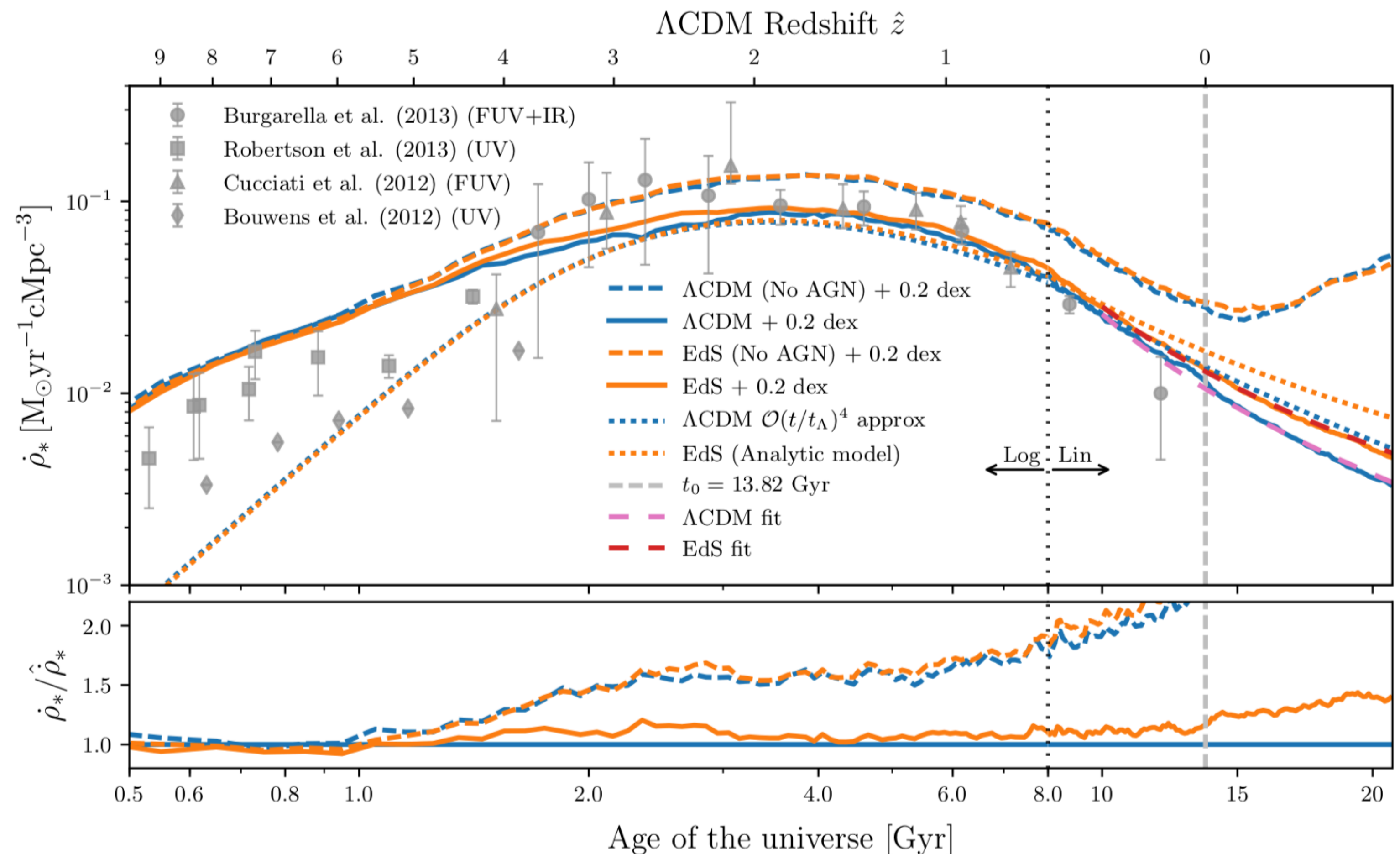
Progenitor Matching

- We must match *different* galaxies to their nearby counterparts (by mass or other properties)
- This is rubbish as we can't see the direct correspondence between objects



Statistics

- What we can do is collect statistical information about the galaxy population
- This is a very famous plot that shows the star formation history of the Universe

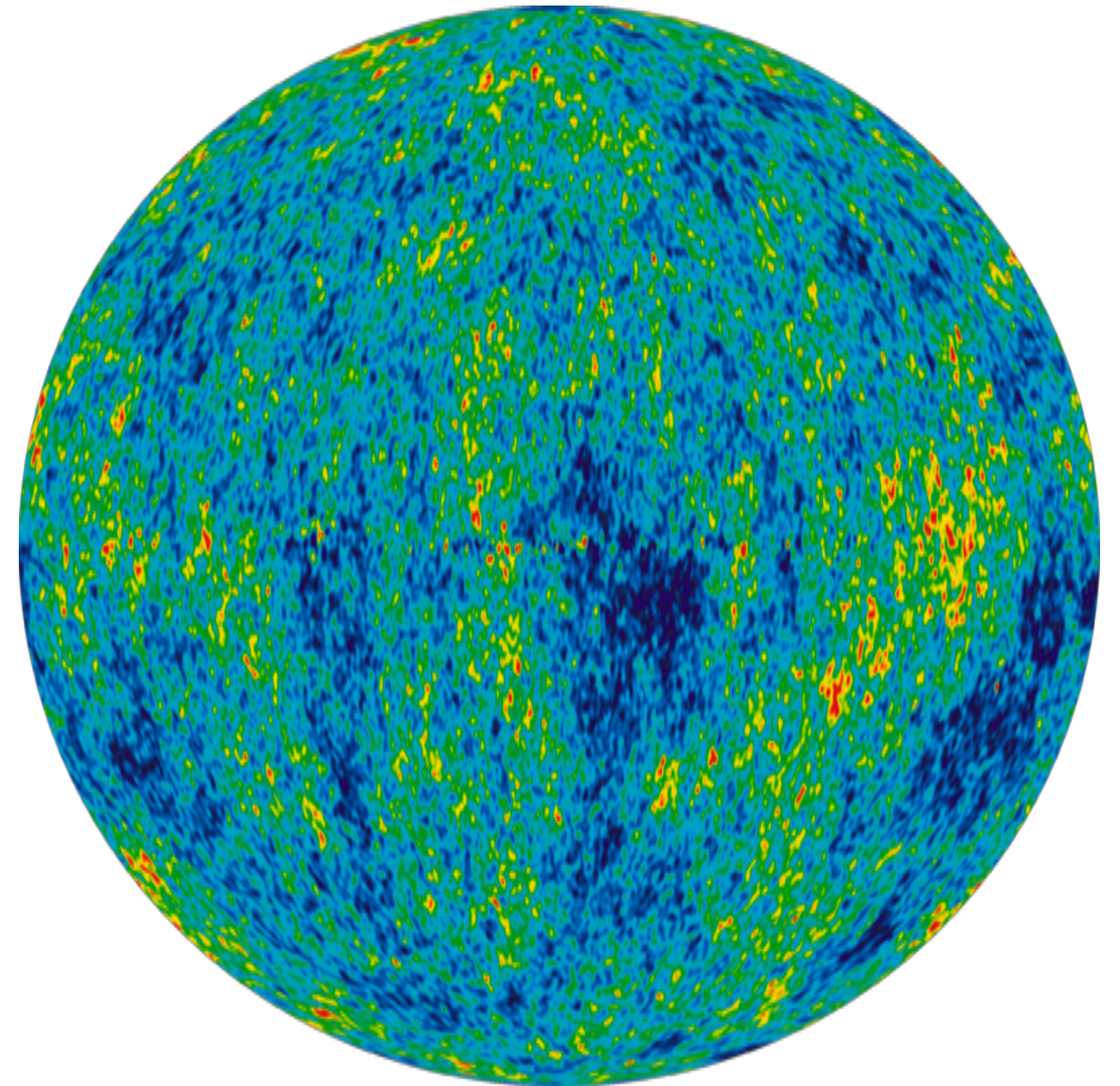


A visualization of the cosmic web, showing a complex network of filaments and clusters of galaxies. The filaments are primarily red and pink, while the clusters are more blue and white. The background is a deep blue with scattered white stars.

Understanding Galaxy Formation

Where can we go from here?

- We have a conceptual idea of galaxy formation
- Also have some statistical properties of the Universe
- No idea how a specific galaxy formed
- Difficult to pin down what processes are important!

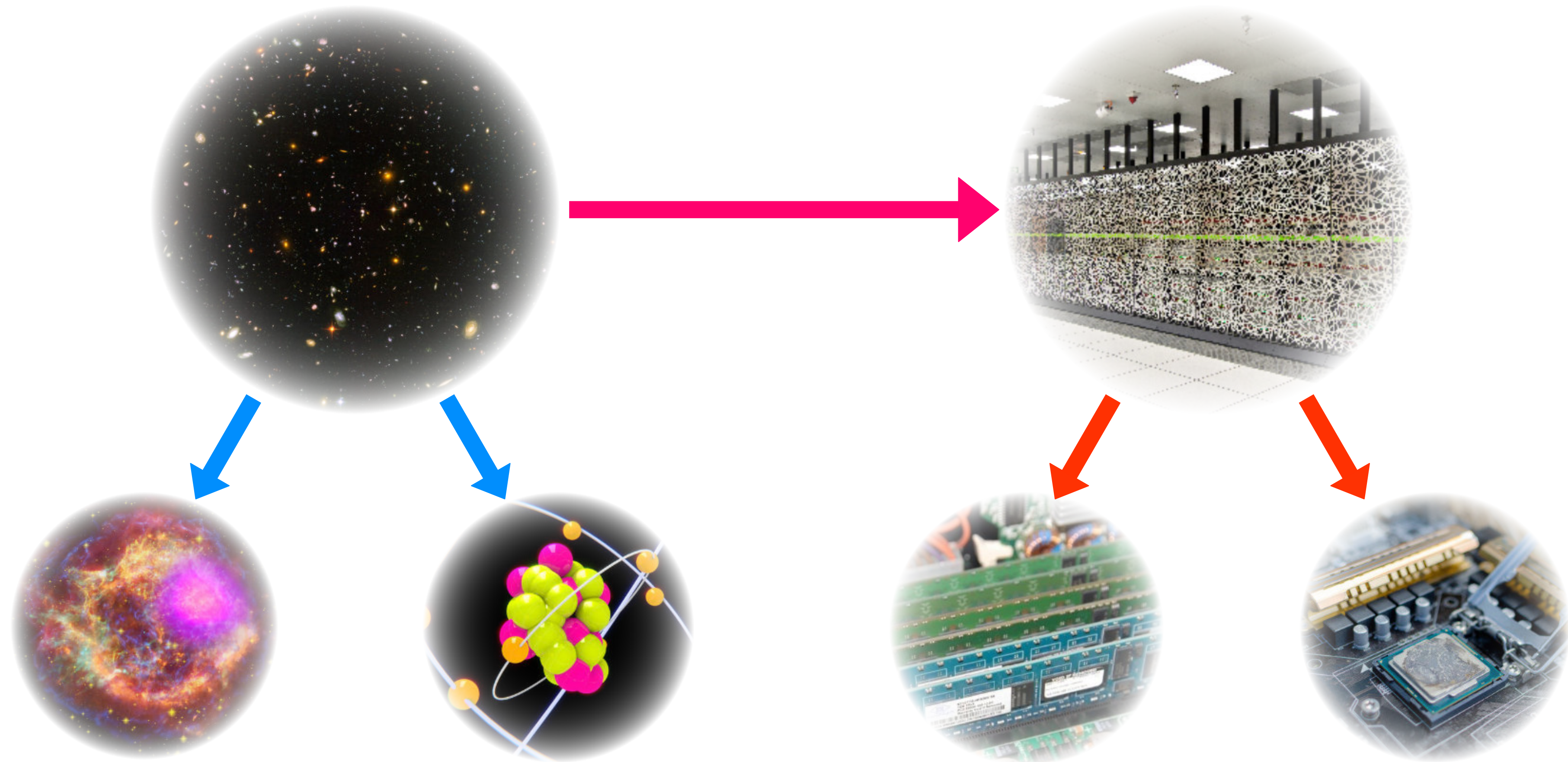


The cosmic microwave background (CMB) as seen by WMAP

Running a Simulation of the Universe

The Universe

HPC System



Infinite Volume

Infinite Scale

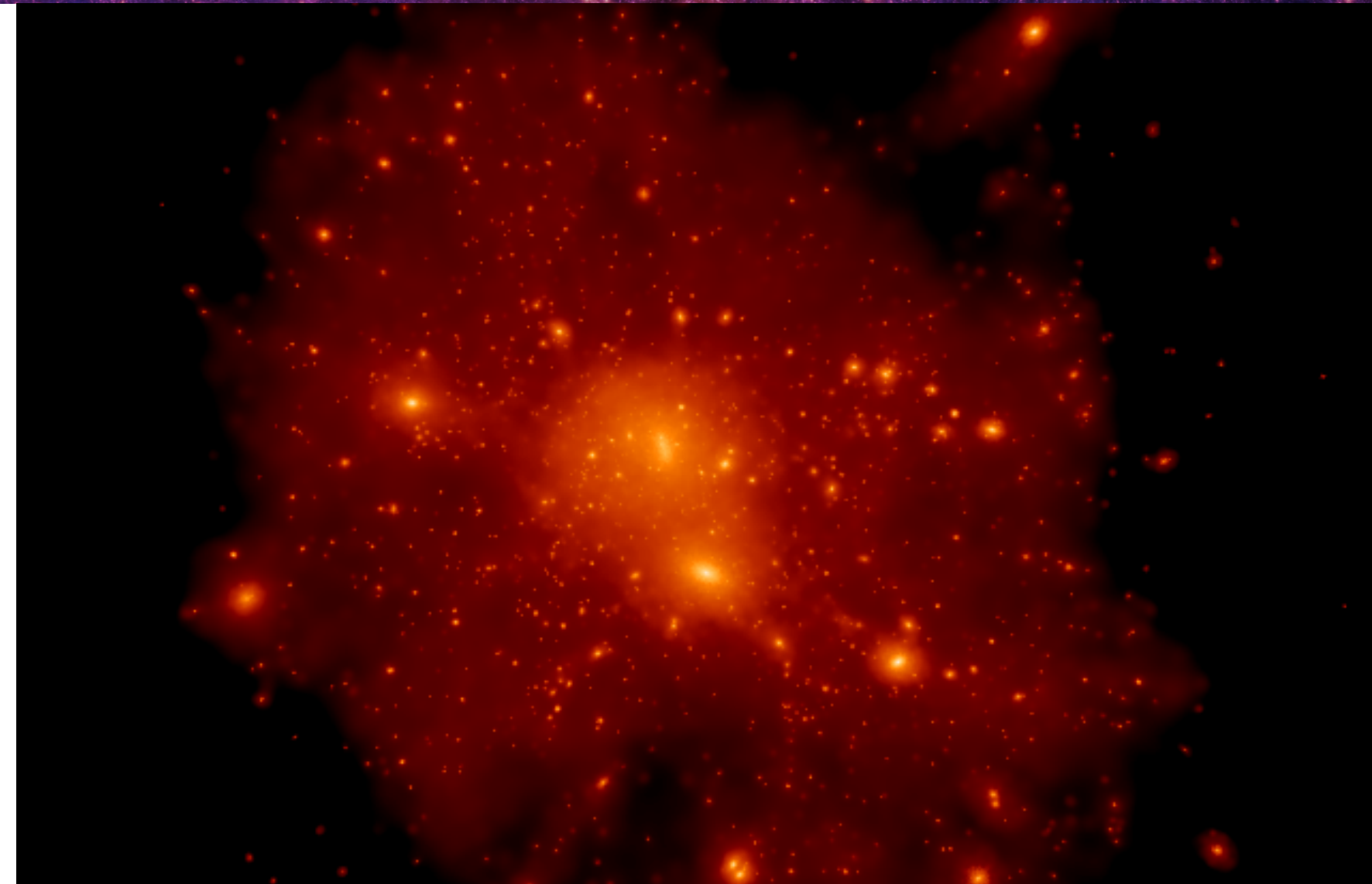
Limited Memory

Finite Scale

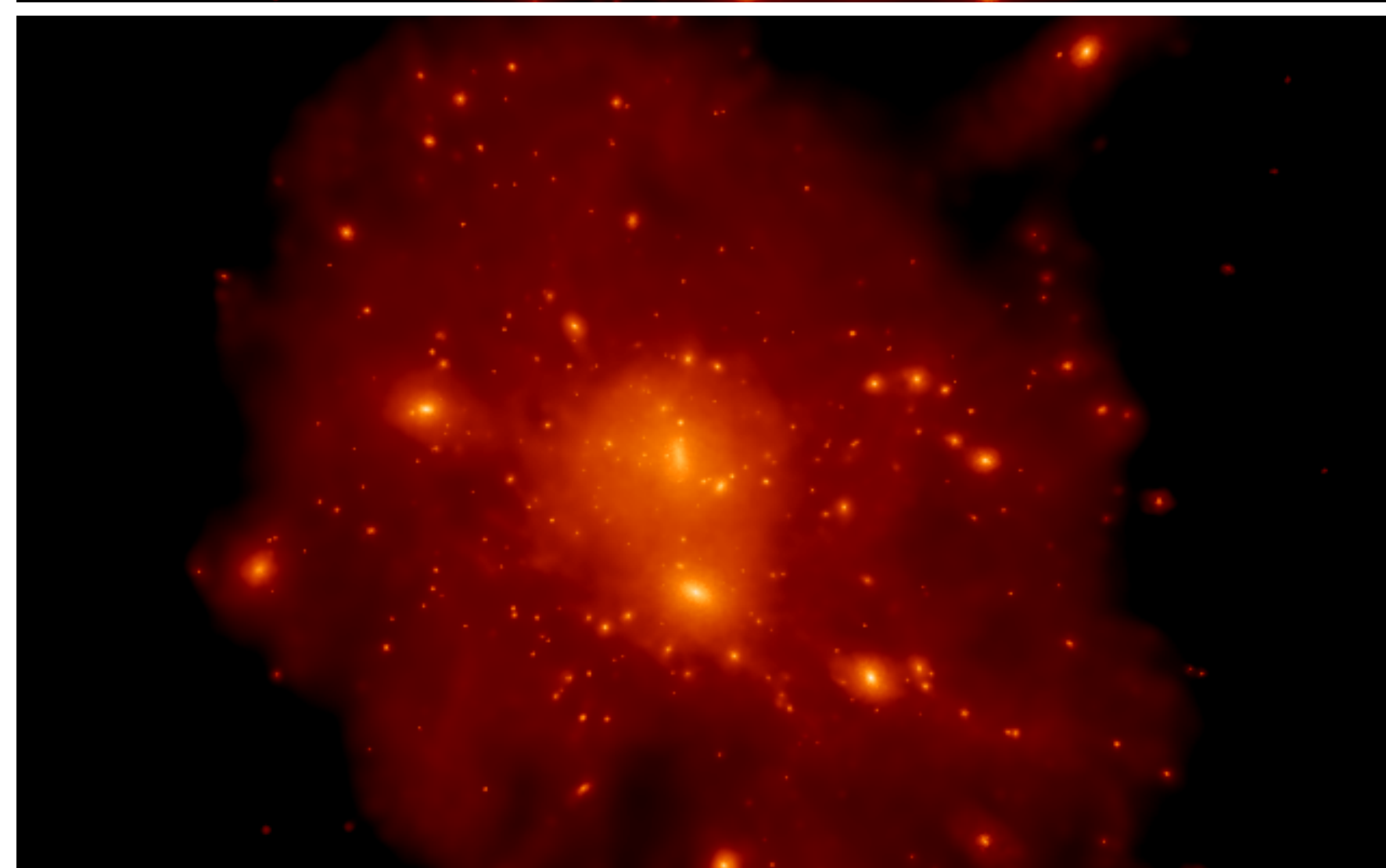
Step 1: Get the Dark Matter Right

- Cosmology tells us *how much* dark matter there is, but not of what *type*.
- We can run gravity-only simulations of dark matter to determine how it affects structure formation in the Universe.
- These allow us to predict e.g. how many satellite galaxies we'd expect around the Milky Way

CDM: WIMP

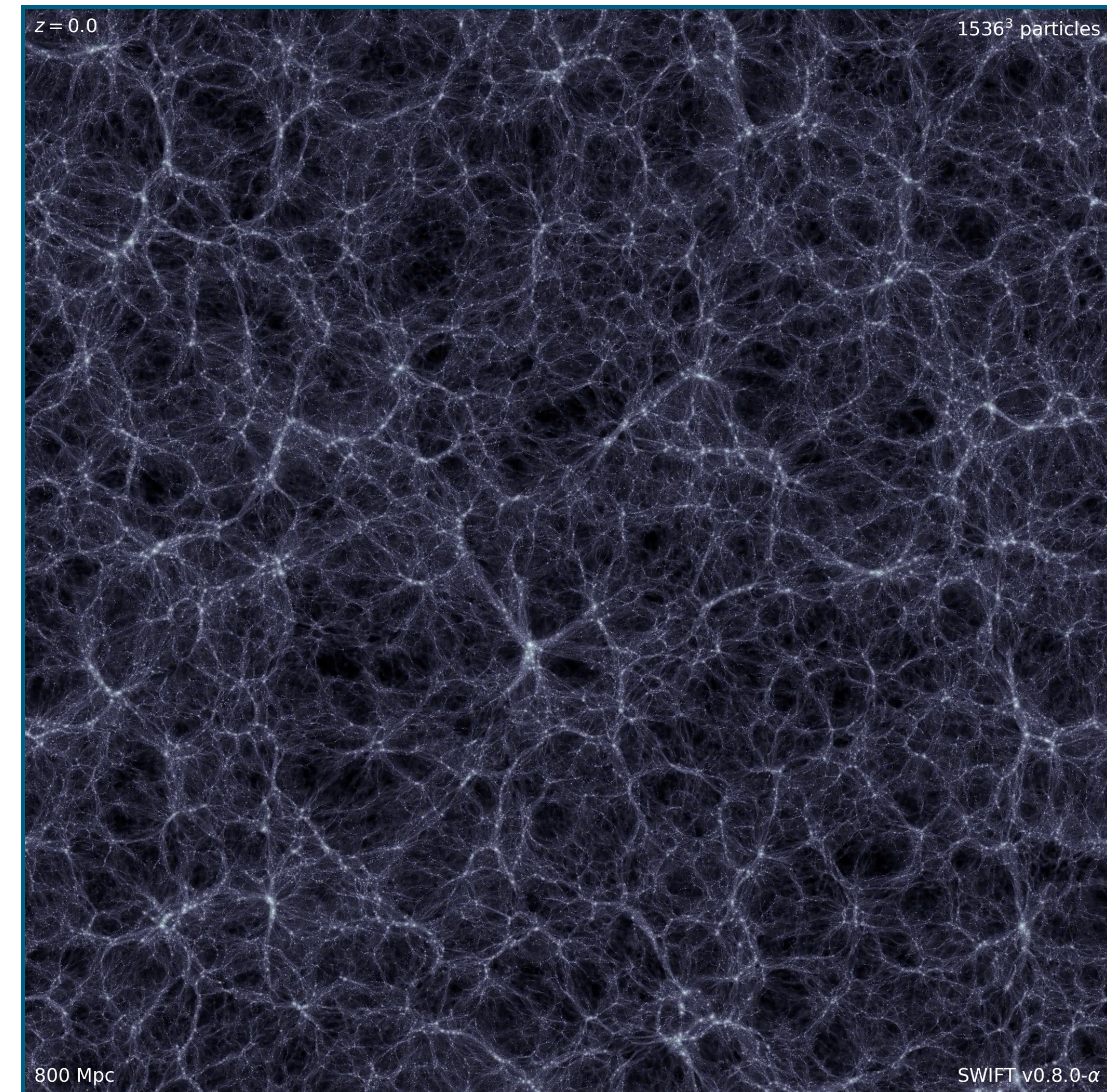


WDM: Neutrinos



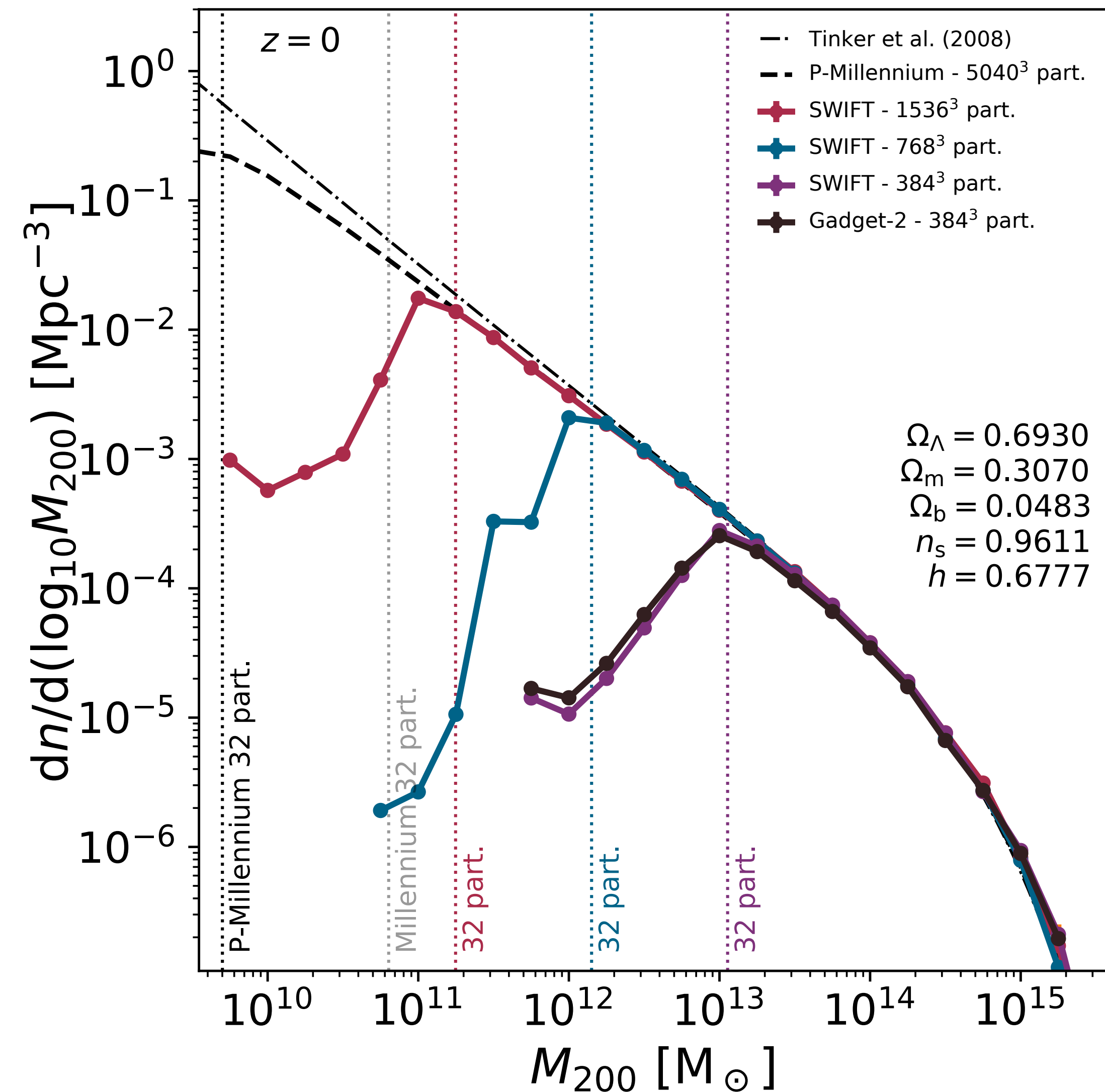
Step 1: Get the Dark Matter Right

- We can run these 'N-body' simulations super fast these days
- 5000^3 or higher (125 billion) particle simulations are not uncommon



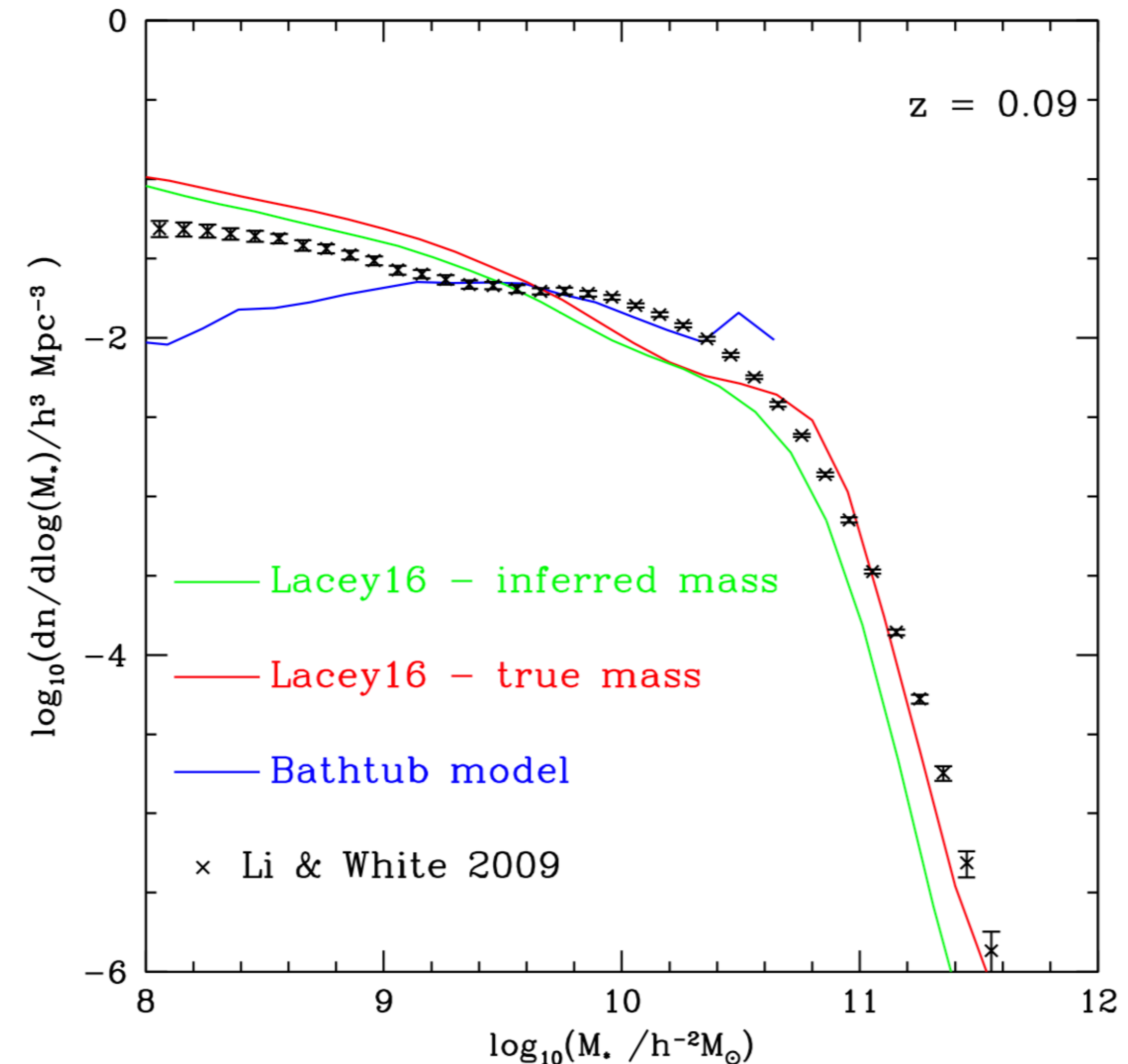
The Halo Mass Function

- Shows the abundance of dark matter halos as a function of mass
- This is self-similar all the way down
- Clearly that's not the same for baryons...



Semi-Analytic Models

- Use the dark matter-only simulations as a base
- Stick on top a 'semi-analytic' model of galaxy formation that has equations to model galaxy properties
- Caveat: these are boring AF and have no pretty pictures



What do SAMs say about Galaxy Formation?

- A lot.
- Pretty much everything we know comes from these models.
- Important processes:
 - Star formation and stellar “feedback”
 - Black holes and their associated “AGN feedback”
 - Gas cooling

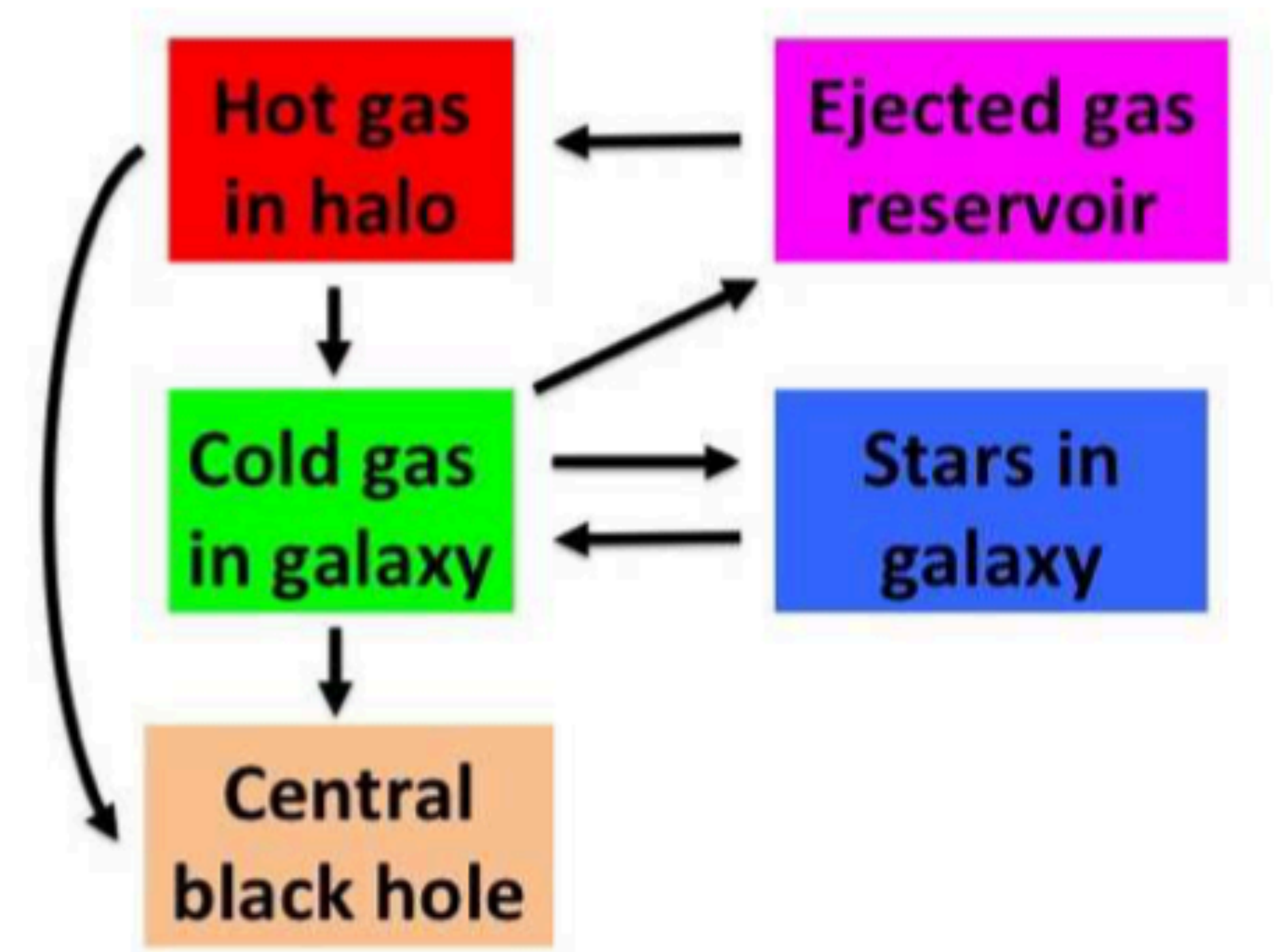


Figure 1. Flow chart showing the different baryonic components in a halo, and transfers between them.

The Problem with SAMs

- Boring
- Ugly
- No resolved properties!
- Cannot study the interaction of galaxies with their environment
- Difficult to study galaxy interactions

52 Lacey et al.

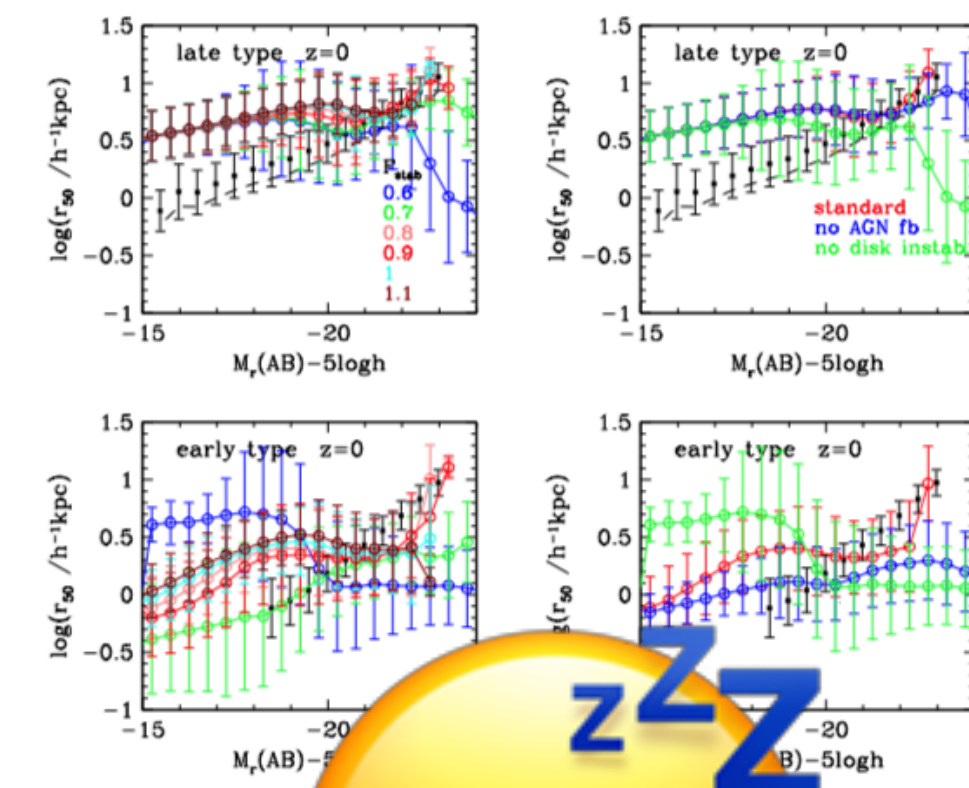


Figure C11. Effects on the half-light radii of late- and early-type galaxies at $z=0$ of varying the stability parameter F_{stab} , and (b) of turning off AGN feedback or disk instabilities. A single parameter is varied in each panel. The red curves show the standard model. The observational data plotted are the same as in Fig. 13.

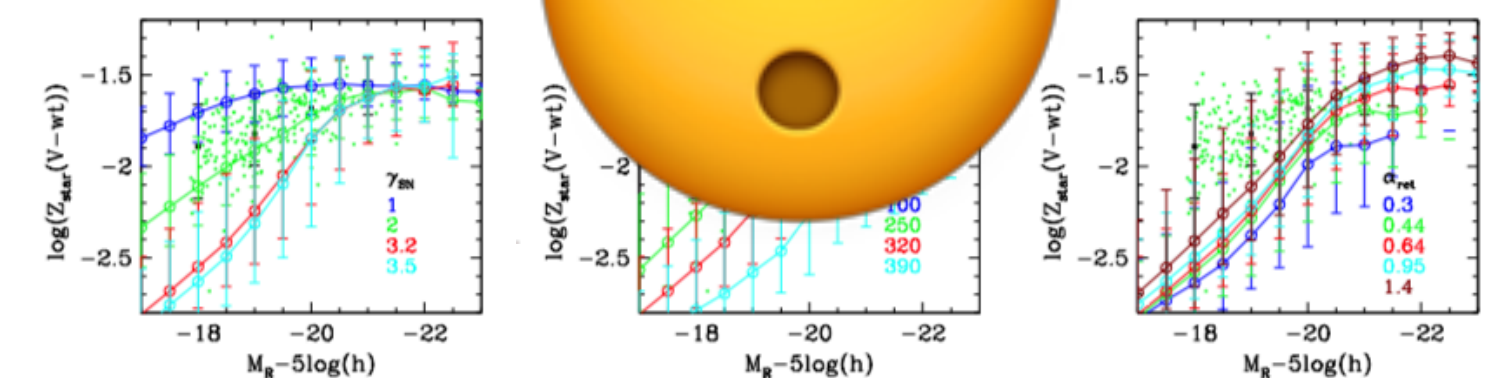


Figure C12. Effects on the stellar metallicity in early-type galaxies at $z=0$ of varying the supernova feedback parameters γ_{SN} and V_{SN} , and the gas return timescale parameter α_{ret} . The red curves show the standard model. The observational data plotted are the same as in Fig. 13.

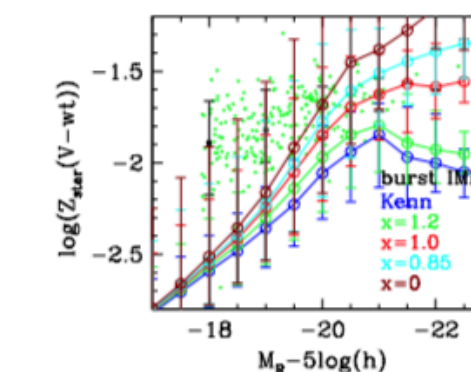


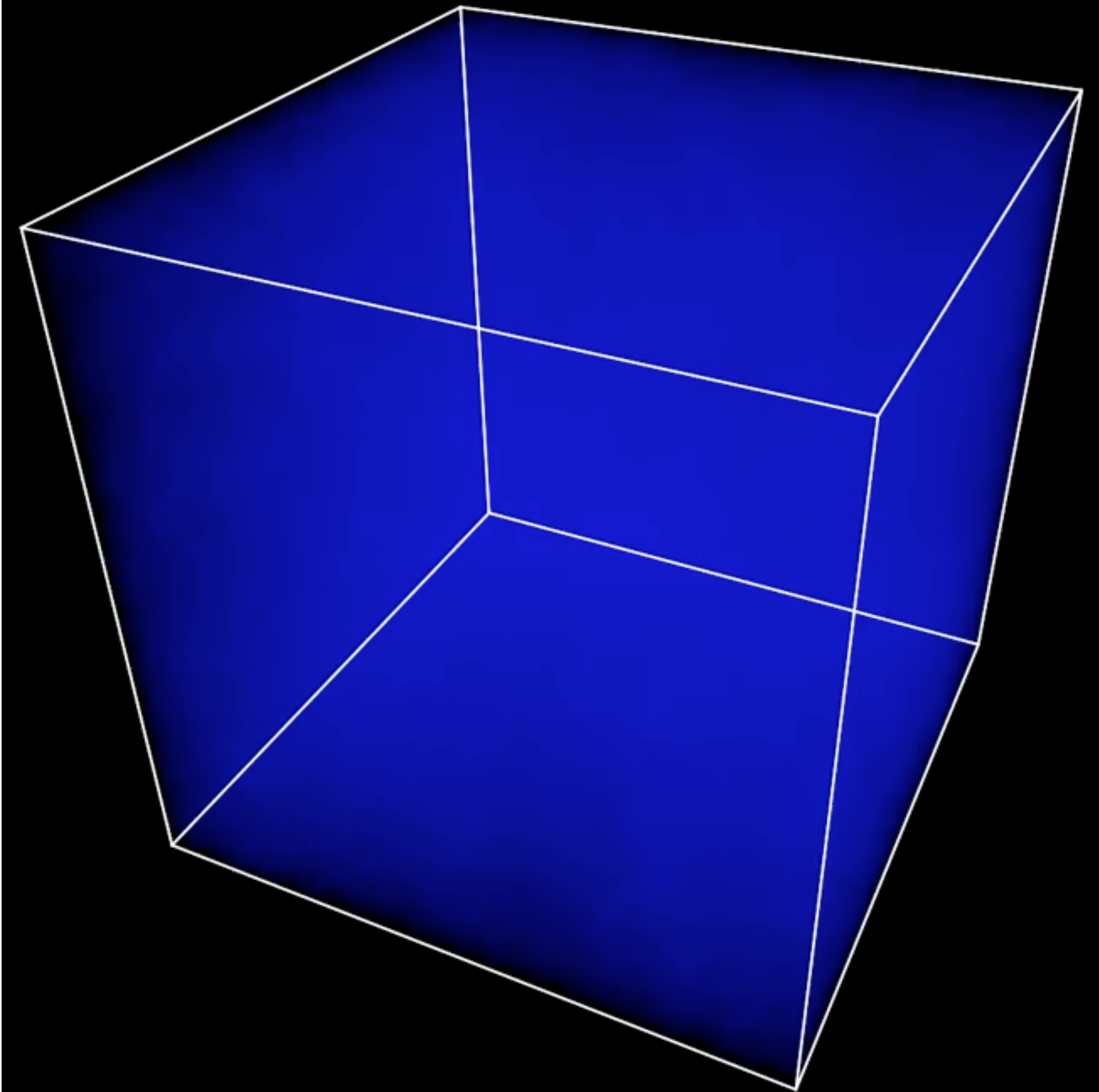
Figure C13. Effects on the stellar metallicity in early-type galaxies at $z=0$ of changing the slope x of the starburst IMF.

The background of the slide is a complex, colorful visualization of a cosmological hydrodynamics simulation. It features a dense network of filaments and structures in shades of red, pink, and white, set against a deep blue background. These structures represent the distribution of matter and gas in the universe, showing the formation of galaxy clusters and the cosmic web. The overall effect is a sense of vast, dynamic cosmic space.

Cosmological Hydrodynamics Simulations

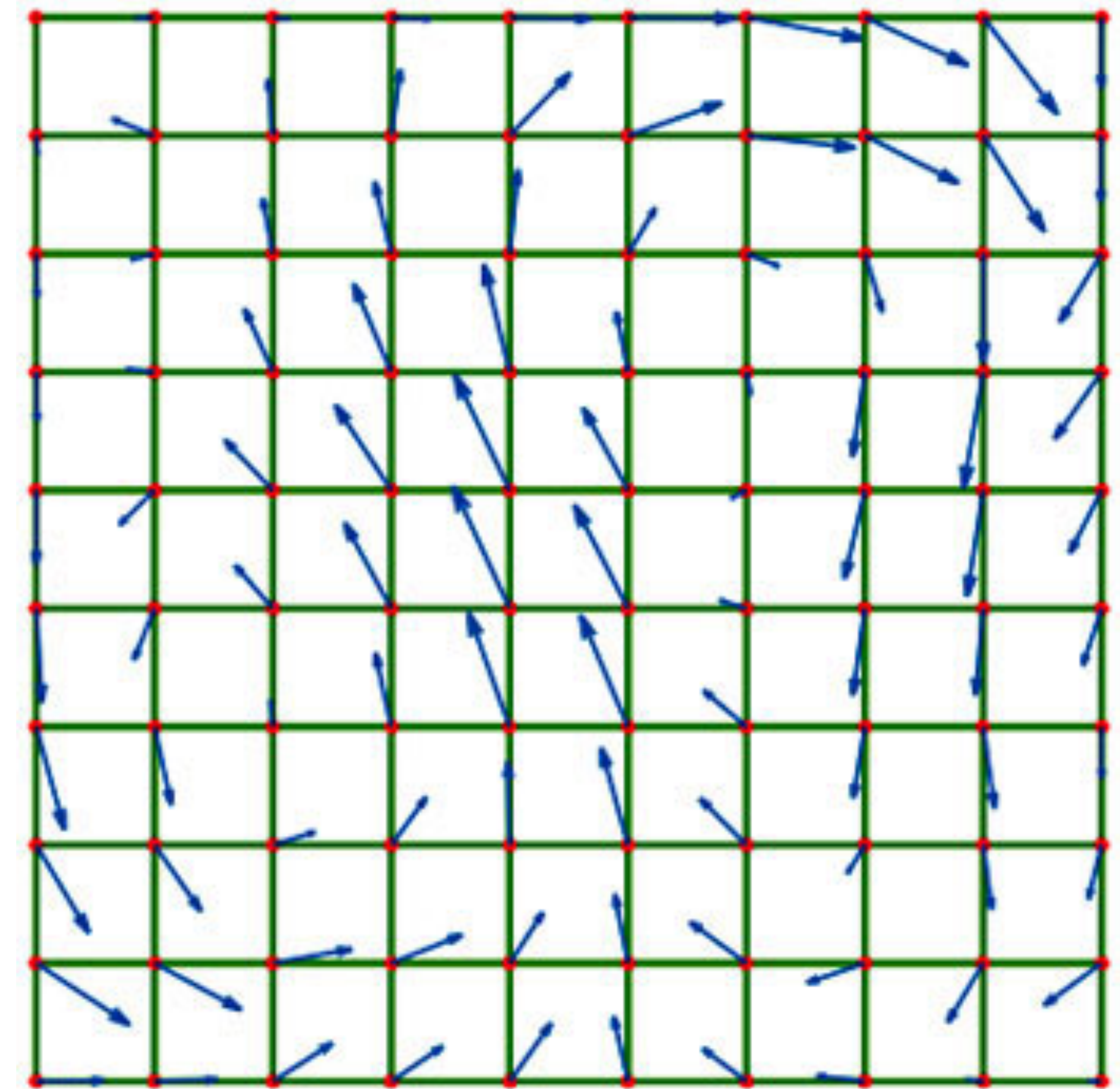
Step 2: Do it 'Properly'

- Need to couple (at least) three main key pieces of physics
 - Cosmology
 - Hydrodynamics
 - Gravity
 - (+ Radiative transfer..???)
 - (+ Magnetic fields..???)

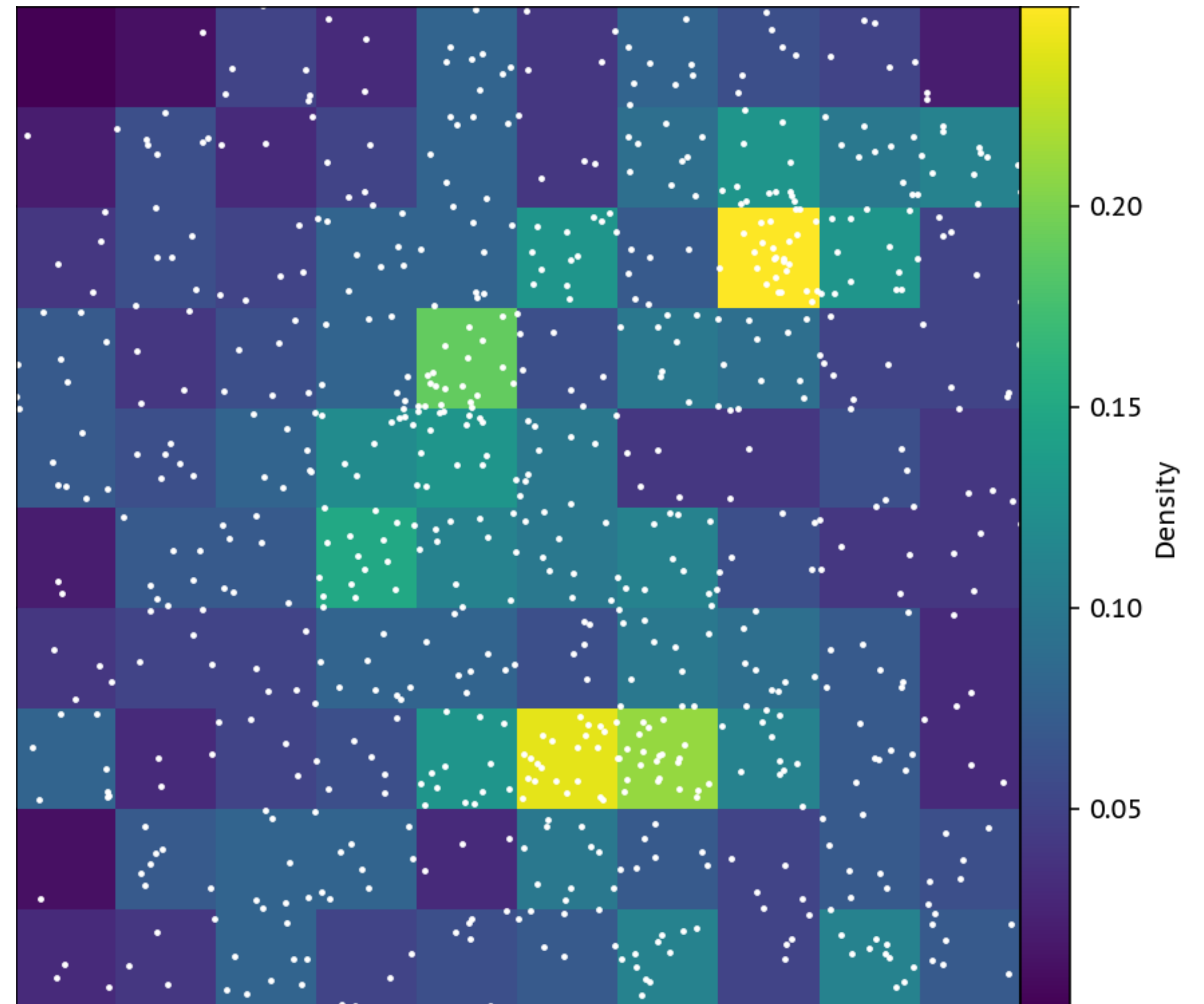
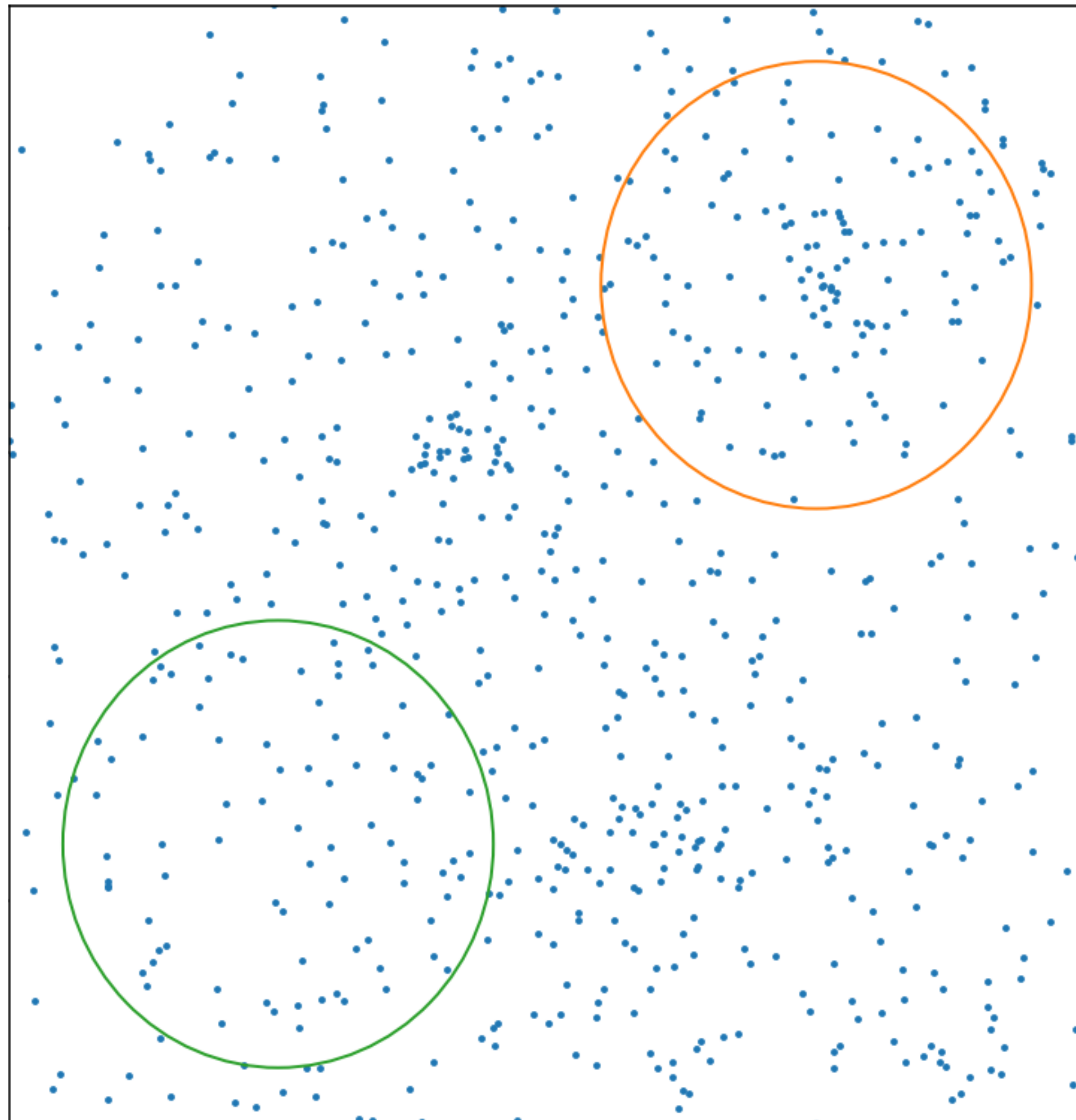


Hydrodynamics

- Typical way to do this: lay down a grid and compute fluid flows between cells
- Several problems:
 - Lack of adaptivity
 - **Cannot track fluid flow over time**
 - Makes gravity difficult



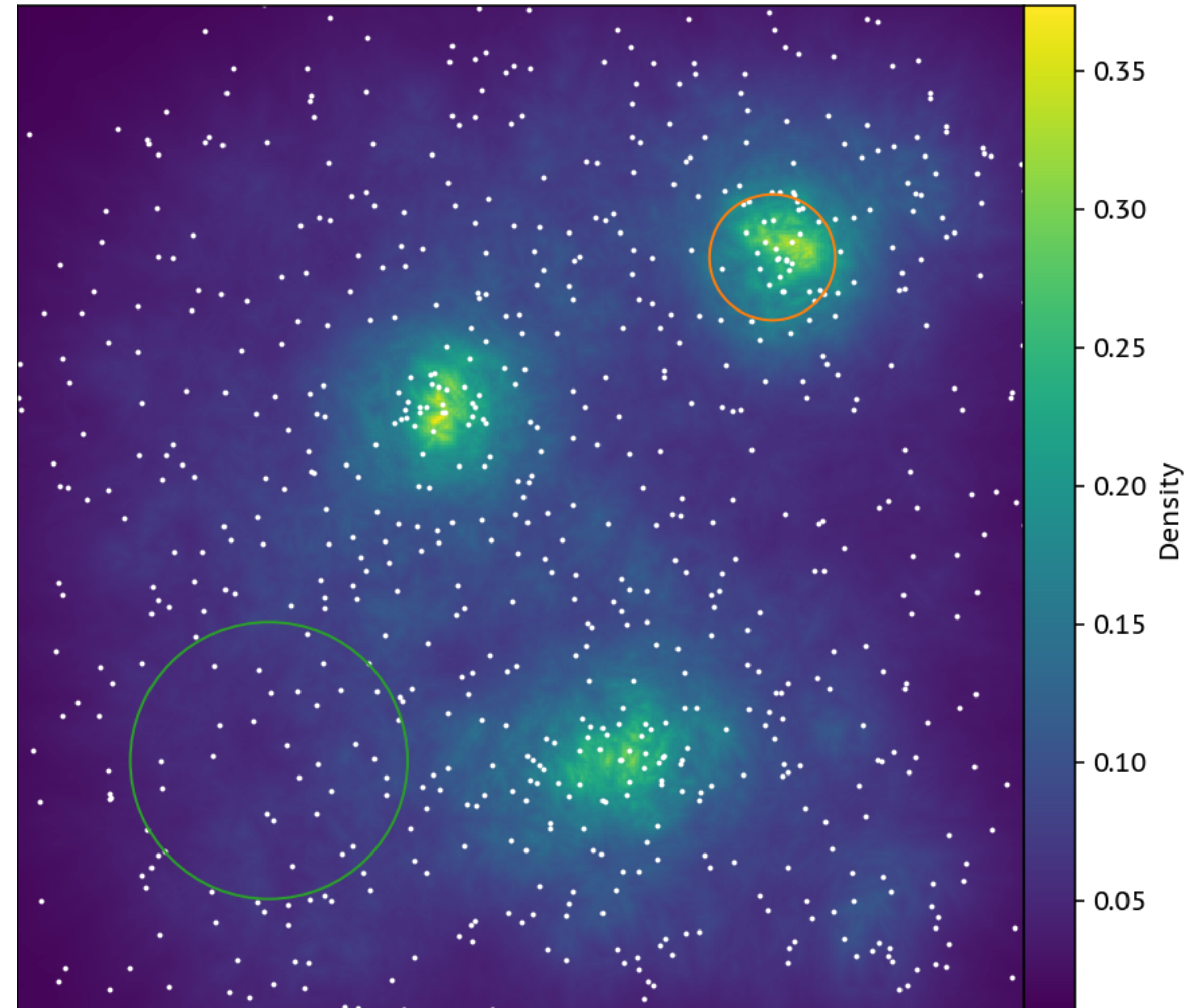
Hydrodynamics with Particles



Improving our Density Estimate

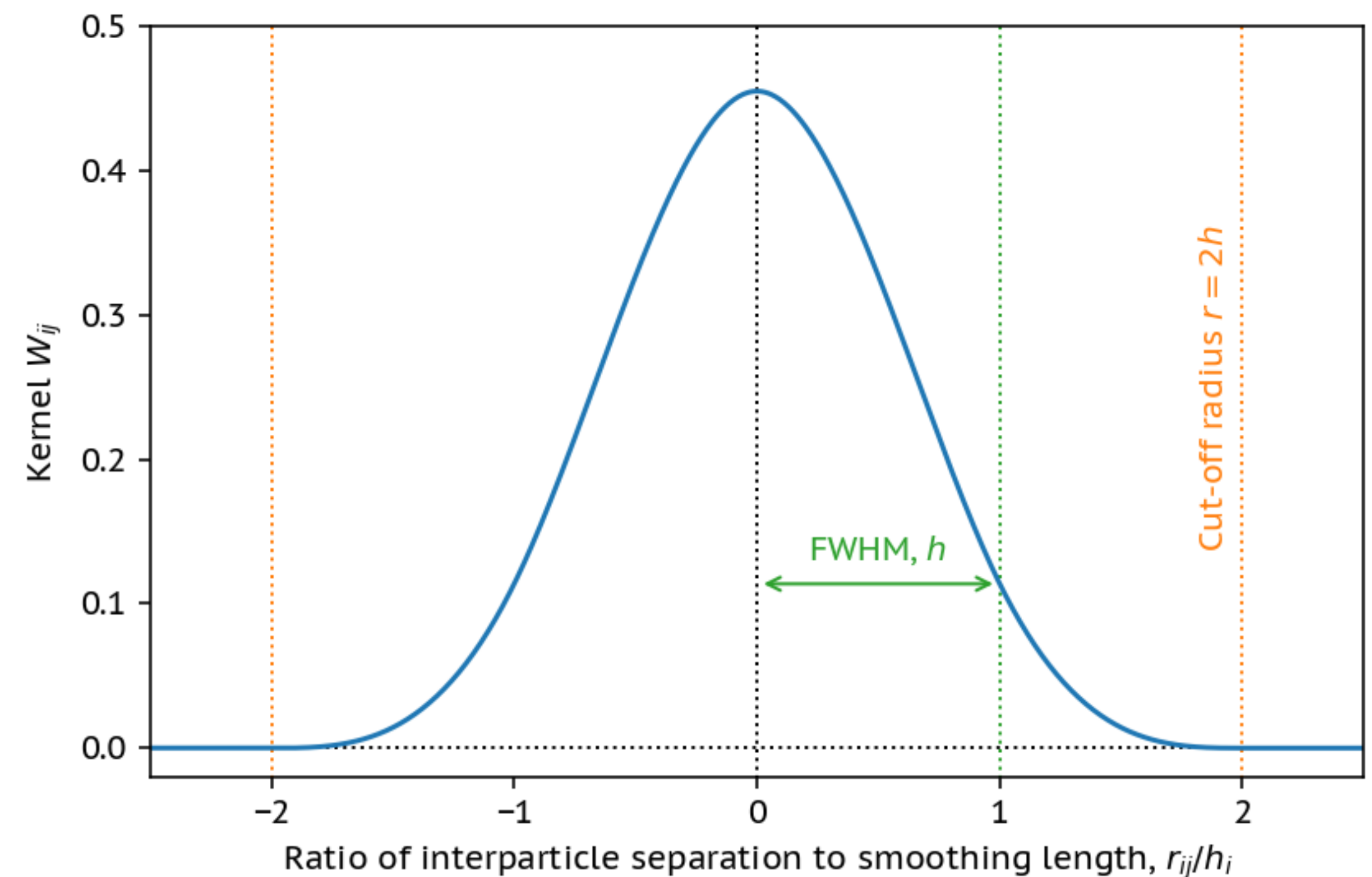
- What if we change the volume we consider for each particle?
- Set R such that our volume encloses 30 particles.
- Density for each particle is then

$$\rho_i = \frac{30m_{\text{part}}}{\frac{4}{3}\pi R_i^3}$$



Turning Down the Noise

- We can do better! We care less about particles that are further away.
- Weight the contribution from each particle with a "kernel".
- Size kernel to enclose 30 particles within cut-off radius.

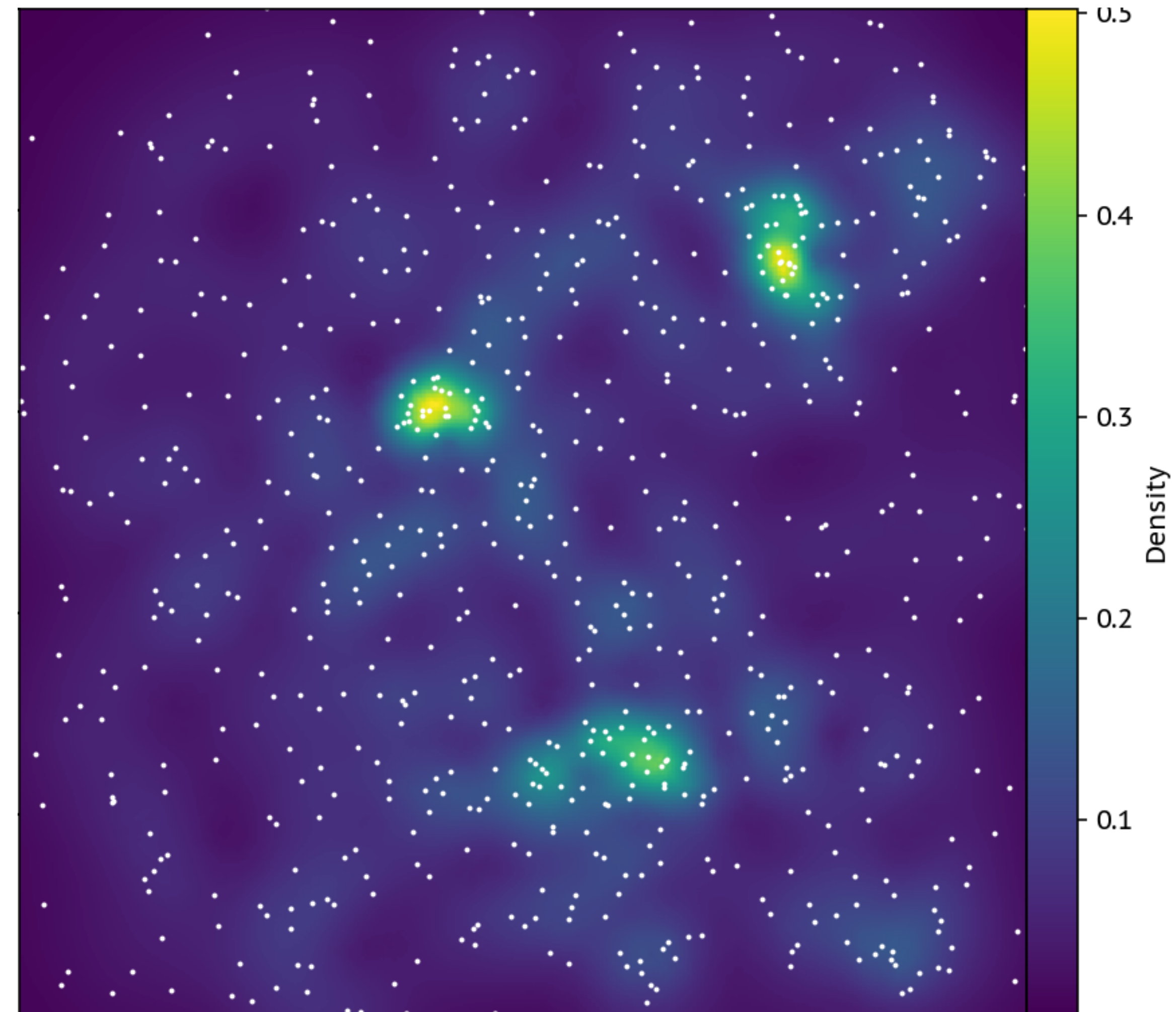


A Smooth Density Estimate

- Density for each particle now given by:

$$\rho_i = \sum_{j=1}^{30} m_{\text{part}} W(r_{ij}, h_i)$$

- Density (+ temperature, tracked by particles) gives pressure, which gives dynamics



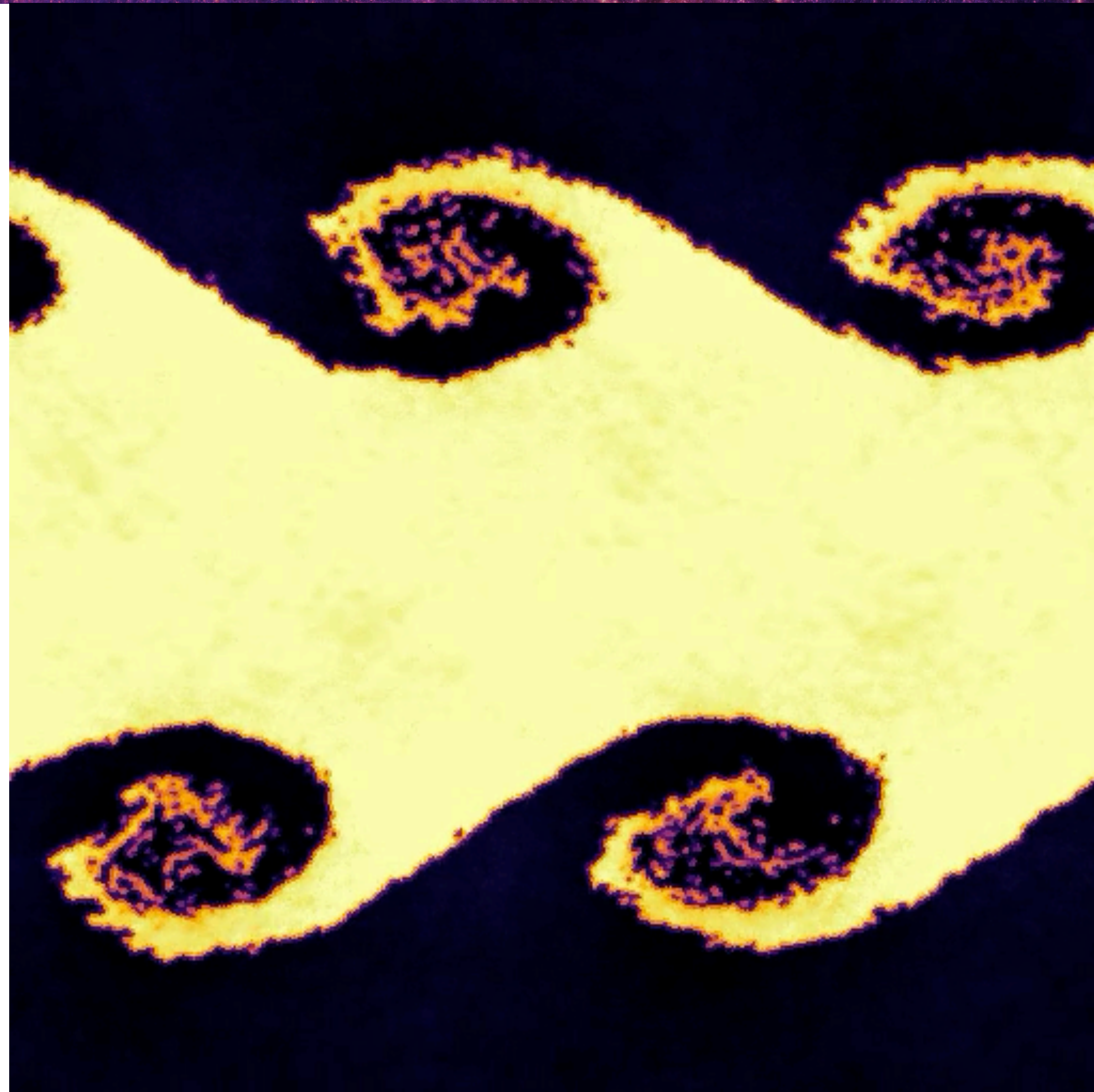
Adding in the 'Dynamics'

$$L(q, \dot{q}) = \frac{1}{2} \sum_{i=1}^N m_i \dot{r}_i^2 - \sum_{i=1}^N m_i u_i,$$

$$\left. \frac{\partial u_i}{\partial q_i} \right|_A = -\frac{P_i}{m_i} \frac{\partial \Delta V_i}{\partial q_i}, \quad + \quad \phi_i(\mathbf{q}) = \kappa h_i^{n_d} \frac{1}{\Delta \tilde{V}} - N_{ngb} = 0,$$

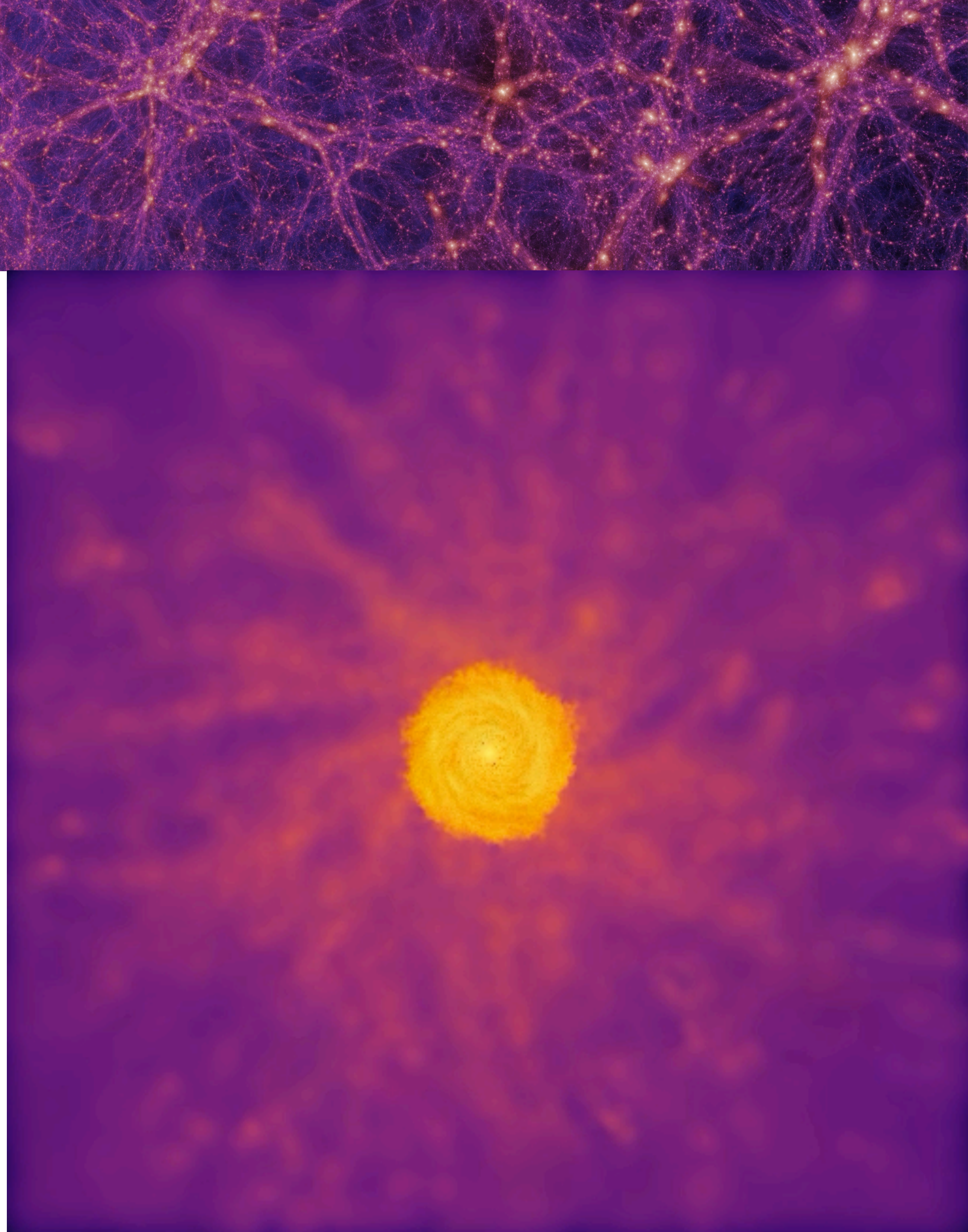
$$m_i \frac{d\mathbf{v}_i}{dt} = \sum_{j=1}^N P_j \nabla_i \Delta \tilde{V}_j \psi_j + P_j \nabla_i \Delta V_j.$$

$$\frac{d\mathbf{v}_i}{dt} = - \sum_{j=1}^N x_i x_j \left[\frac{f_{ij} P_i}{y_i^2} \nabla_i W_{ij}(h_i) + \frac{f_{ji} P_j}{y_j^2} \nabla_i W_{ji}(h_j) \right]$$



Sub-Grid Physics

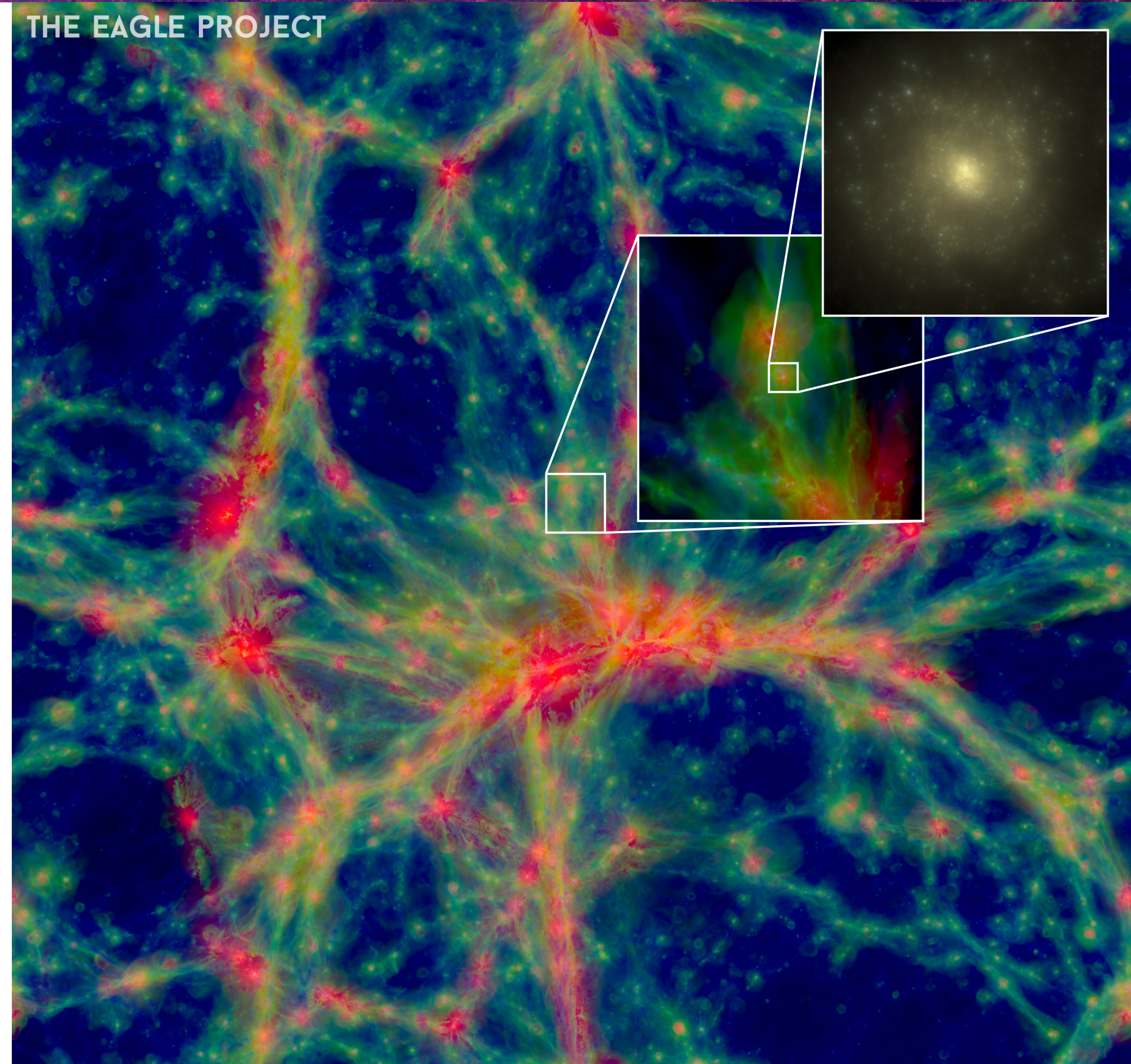
- We cannot resolve everything
- Typical resolution is about 10^6 solar masses
- Lots of processes occur at smaller scales:
 - Gas cooling (atomic transitions...)
 - Star formation
 - Black hole accretion



Galaxy Formation Models

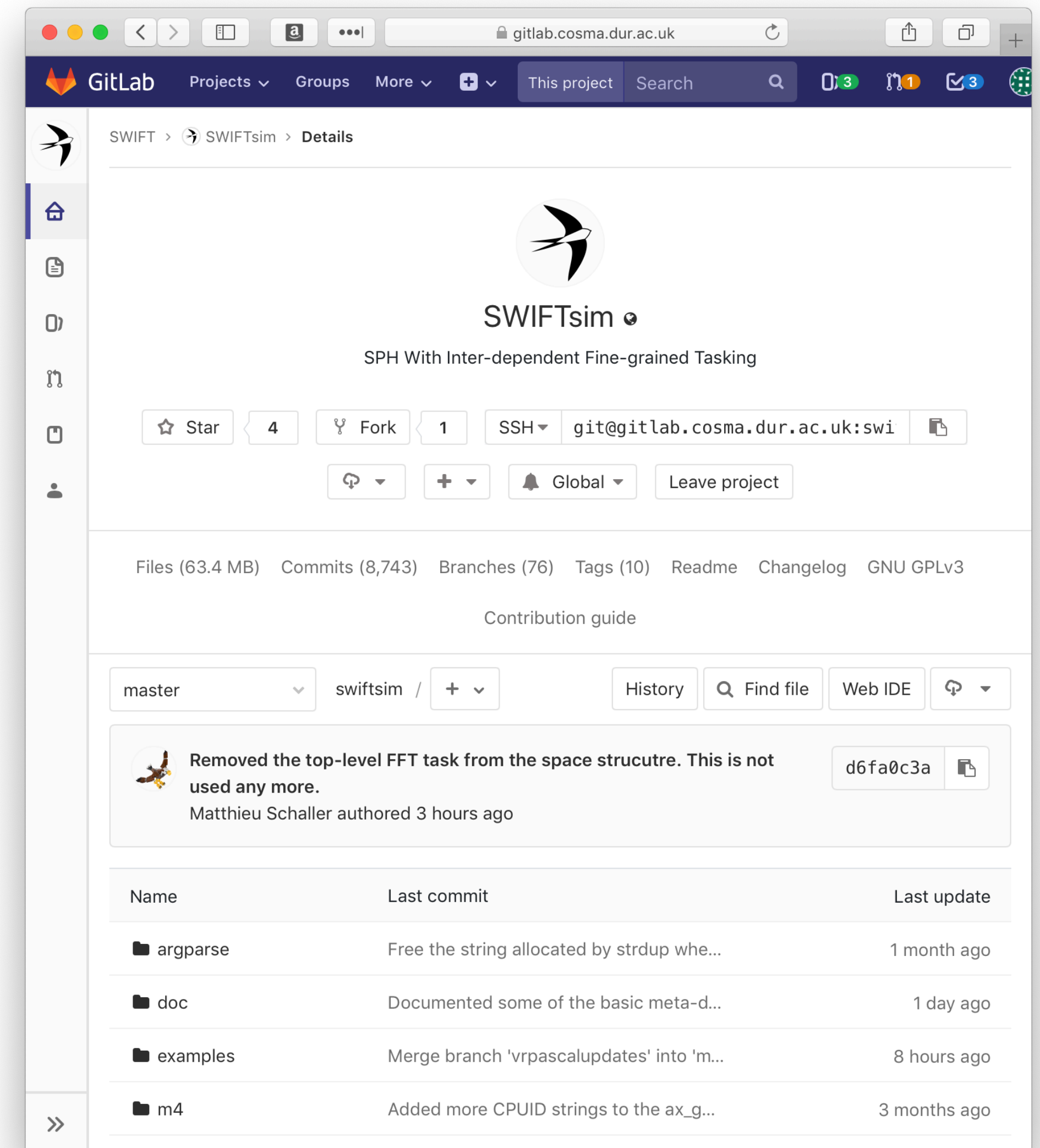
- This 'sub-grid' physics is directly related to the SAMs we discussed before
- They contain similar information, but the full models can be much simpler

THE EAGLE PROJECT



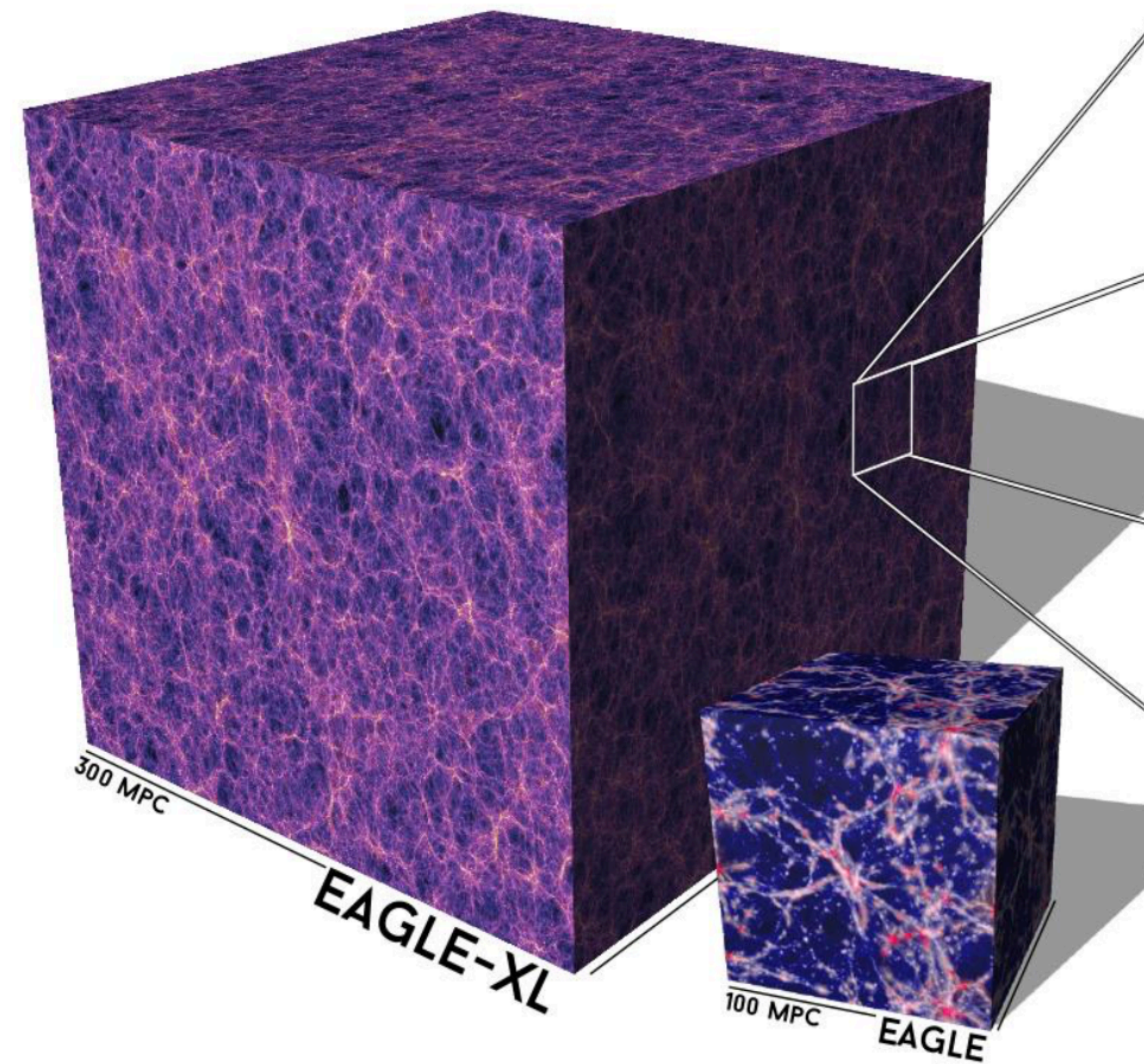
Implementation

- 100'000 lines of open-source C99 code
- Hybrid (MPI + threads)
- Collaboration between astronomy, computer science, and industry
- Supported by DiRAC



How big?

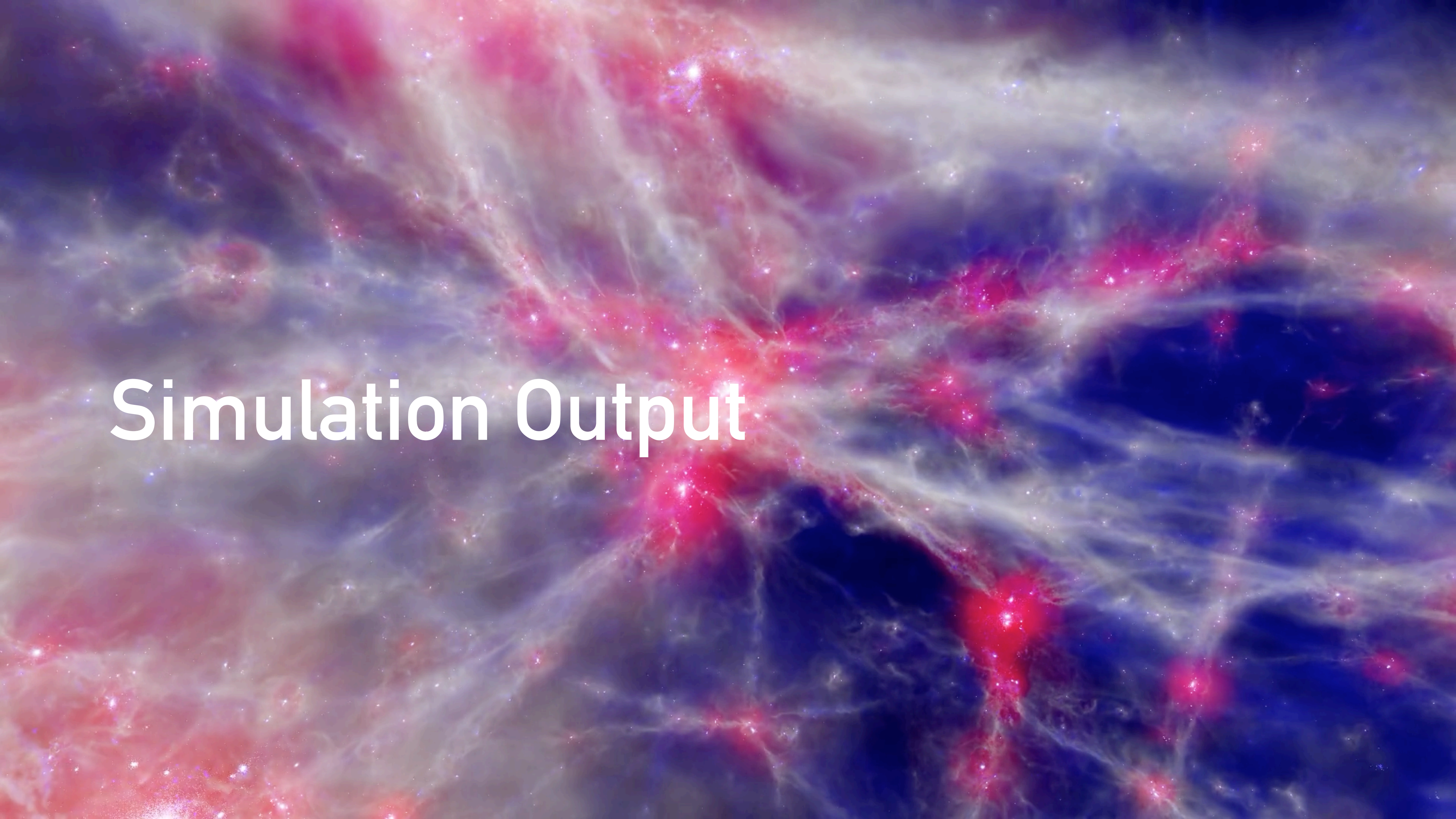
- Our next big run:
- Nearly **100 billion particles**
- 30'000 galaxies with a mass similar to our own Milky Way
- Each galaxy resolved by 10'000 - 100'000 particles



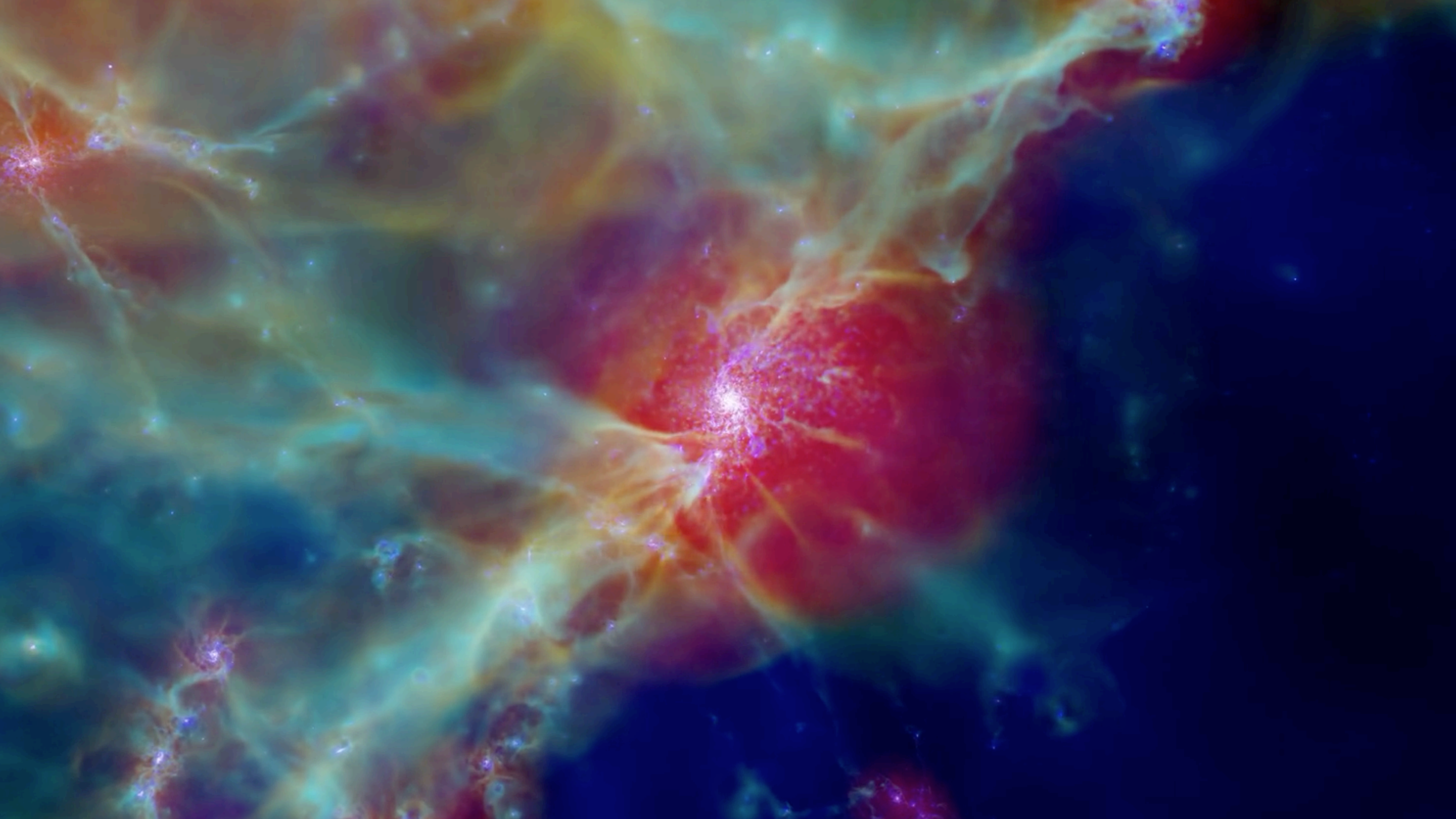
Computing Resources

- Need Tier-0 resources
- 10s of millions of core hours
- 10'000s of CPUs
- ~200-300 TB of RAM
- Snapshots ~4-5 TB each



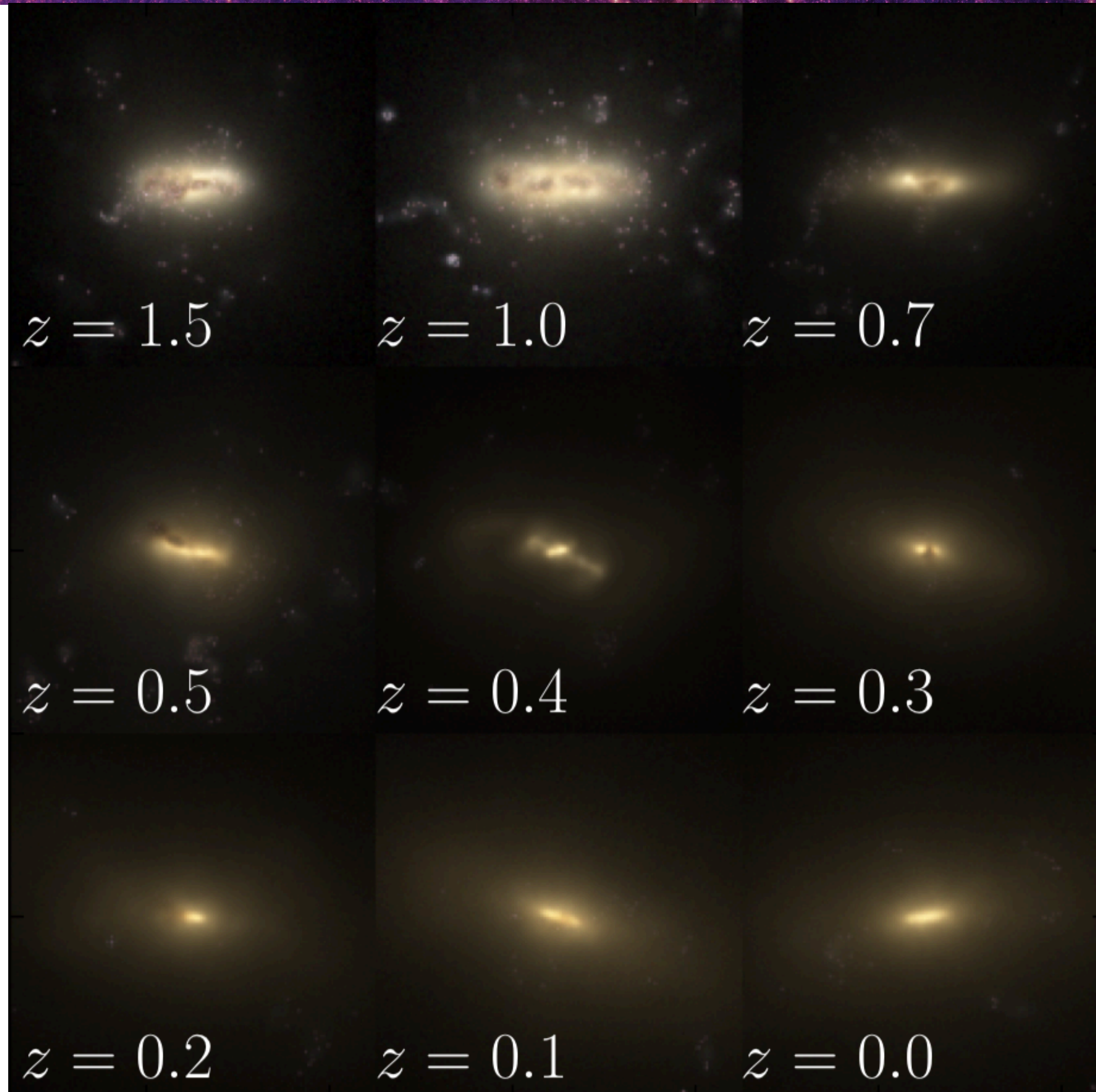
The background of the image is a vibrant, abstract representation of a cosmic web simulation. It features a complex network of glowing, filamentary structures in shades of red, pink, and white, set against a deep blue and purple background. These filaments represent the distribution of matter in the universe, with brighter areas indicating higher density. The overall effect is one of dynamic energy and vast scale.

Simulation Output



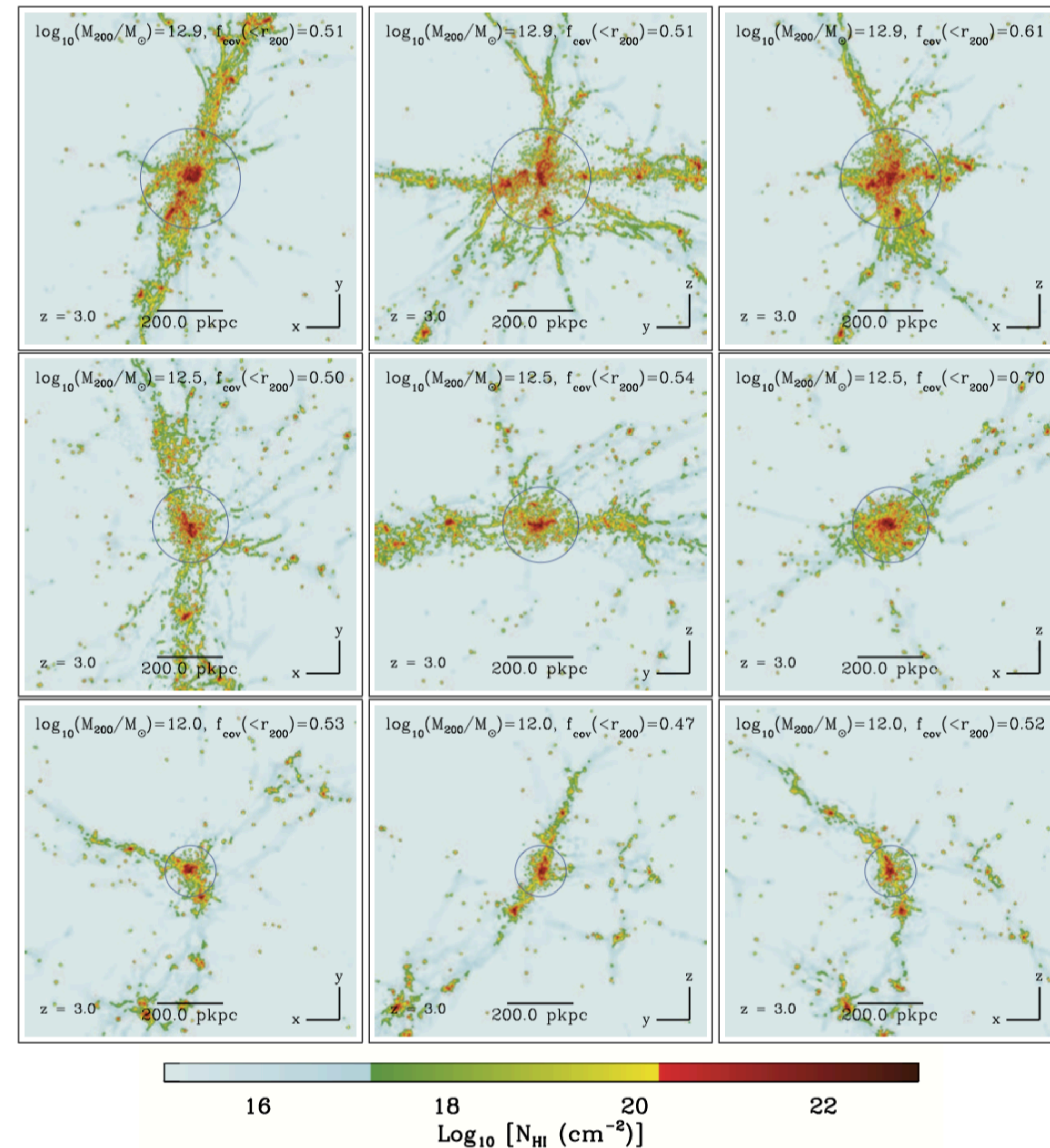
Seeing Galaxies Grow and Change

- We can see the emergence of the "Tuning Fork" by following *individual* galaxies through their evolution
- Turns out that it goes backwards, with Ir -> Spiral -> Elliptical.



Effects on Large-Scale Structure

- Can see how the gas physics changes the morphology of the large-scale structure
- This feeds back into the calibrations (e.g. dust absorption) that we make when observing distant objects.



Huge Predictive Power

- Cosmological simulations have huge predictive power
- They can be used to tell observers where to point their telescopes for the best chance of finding rare objects
- We can also compare abundances of weird objects to see if some are missing, and figure out why.

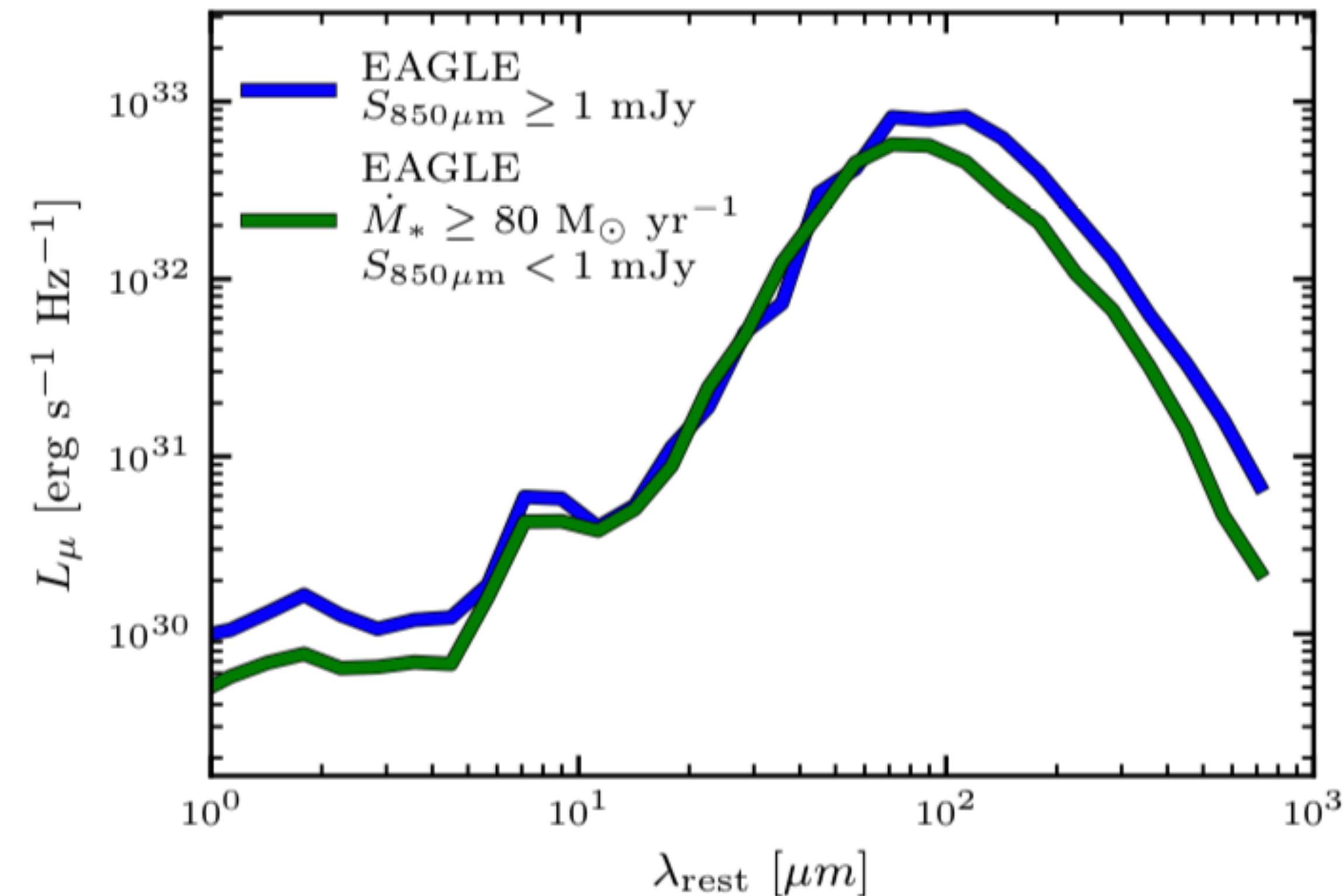


Figure 9. Composite broadband spectral energy distributions (SEDs) for the $S_{850\mu\text{m}} \geq 1 \text{ mJy}$ and highly star-forming Submm-Faint galaxies. The leftward shifting of the peak in the dust emission for the highly star-forming Submm-Faint sample signifies hotter dust temperatures than the $S_{850\mu\text{m}} \geq 1 \text{ mJy}$ galaxies.

Summary

- Large timescales make cosmology and astrophysics really challenging
- We can address some of this by using cosmological simulations
- To perform a useful calculation, you need some of the largest supercomputers in the world
- We can make pretty movies...