

# Supplementary materials for ‘Performing Parentage Analysis in the Presence of Inbreeding and Null Alleles’

## Tables

Table S1: The accuracy of the Nei’s (1977) estimator and our allele frequency estimator

$f$	$p_y$	$\hat{f}$		$\hat{\beta}$		$\hat{p}_y$	
		bias	std	bias	std	bias	std
0	0	0.004	0.007	0.000	0.021	0.008	0.014
0	0.05	0.095	0.018	-0.004	0.021	-0.036	0.021
0	0.15	0.266	0.019	0.003	0.025	-0.129	0.032
0	0.3	0.470	0.020	0.048	0.040	-0.265	0.051
0.05	0	-0.005	0.016	-0.001	0.021	0.012	0.018
0.15	0	-0.005	0.018	-0.003	0.022	0.016	0.024
0.3	0	-0.005	0.020	-0.007	0.023	0.023	0.034
0.05	0.05	0.088	0.018	-0.002	0.022	-0.034	0.024
0.15	0.15	0.212	0.020	0.018	0.030	-0.123	0.039
0.3	0.3	0.299	0.020	0.102	0.057	-0.251	0.072
0				0.000	0.021	0.009	0.015
0				-0.006	0.021	0.001	0.030
0				-0.015	0.025	0.005	0.042
0		the true		-0.020	0.034	0.010	0.055
0.05		value of $f$		-0.001	0.021	0.010	0.017
0.15		is used in		-0.003	0.022	0.014	0.022
0.3		simulation		-0.006	0.023	0.020	0.032
0.05				-0.006	0.022	0.001	0.033
0.15				-0.013	0.030	0.005	0.052
0.3				-0.008	0.049	0.008	0.079

Table S2: Genetic diversity at 40 microsatellite loci with the highest estimated null allele frequency from Nietlisbach et al. (2015) dataset

Locus	<i>k</i>	<i>n</i>	$H_O$	$H_E$	PIC	<i>f</i>	$p_y$
<i>sosp_ng106</i>	2	2277	0.062	0.481	0.365	0.870	0.764
<i>Sosp046</i>	13	1977	0.241	0.844	0.826	0.715	0.544
<i>sosp_ng323</i>	8	1959	0.259	0.739	0.697	0.649	0.469
<i>sosp_ng167</i>	5	2069	0.196	0.539	0.502	0.636	0.449
<i>sosp_ng169</i>	12	2140	0.249	0.612	0.584	0.593	0.411
<i>Sosp039</i>	17	2033	0.382	0.875	0.862	0.564	0.377
<i>sosp_ng023</i>	9	1875	0.361	0.807	0.781	0.554	0.368
<i>sosp_ng136</i>	6	1358	0.345	0.773	0.736	0.553	0.367
<i>sosp_ng005</i>	5	2193	0.252	0.534	0.427	0.529	0.342
<i>sosp_ng274</i>	6	2180	0.364	0.758	0.722	0.520	0.333
<i>sosp_ng068</i>	9	2322	0.334	0.656	0.607	0.491	0.312
<i>sosp_ng074</i>	6	2199	0.342	0.640	0.581	0.467	0.286
<i>sosp_ng042</i>	5	2169	0.298	0.518	0.464	0.425	0.248
<i>sosp_ng386</i>	4	2371	0.318	0.529	0.449	0.400	0.229
<i>sosp_ng079</i>	4	2375	0.352	0.575	0.513	0.388	0.218
<i>sosp_ng116</i>	5	2385	0.364	0.582	0.527	0.374	0.208
<i>sosp_ng105</i>	9	2364	0.530	0.824	0.803	0.357	0.197
<i>sosp_ng340</i>	3	1832	0.279	0.434	0.355	0.357	0.197
<i>Sosp028</i>	9	2198	0.533	0.780	0.752	0.317	0.170
<i>Sosp111</i>	10	2249	0.463	0.681	0.626	0.320	0.169
<i>sosp_ng388</i>	8	2343	0.391	0.556	0.498	0.298	0.163
<i>sosp_ng022</i>	5	2367	0.288	0.403	0.371	0.286	0.145
<i>sosp_ng384</i>	9	2355	0.583	0.782	0.750	0.255	0.123
<i>sosp_ng121</i>	13	2202	0.683	0.884	0.873	0.228	0.106
<i>sosp_ng014</i>	12	2339	0.501	0.634	0.590	0.210	0.097
<i>sosp_ng093</i>	13	2235	0.643	0.808	0.789	0.205	0.091
<i>sosp_ng127</i>	11	2329	0.664	0.815	0.792	0.186	0.079
<i>Sosp144</i>	11	2367	0.688	0.803	0.776	0.144	0.053
<i>sosp_ng322</i>	4	2470	0.449	0.522	0.485	0.140	0.052
<i>sosp_ng268</i>	19	2463	0.687	0.795	0.769	0.136	0.049
<i>sosp_ng300</i>	7	2461	0.544	0.627	0.576	0.132	0.049
<i>sosp_ng198</i>	3	2334	0.330	0.384	0.342	0.140	0.048
<i>sosp_ng299</i>	4	2472	0.458	0.518	0.478	0.117	0.039
<i>sosp_ng055</i>	7	2401	0.653	0.739	0.696	0.117	0.038
<i>sosp_ng349</i>	8	2459	0.640	0.727	0.679	0.120	0.038
<i>sosp_ng066</i>	5	2384	0.529	0.598	0.523	0.116	0.035
<i>Sosp064</i>	16	2381	0.738	0.830	0.810	0.111	0.035
<i>sosp_ng256</i>	7	2461	0.577	0.640	0.594	0.098	0.032
<i>Sosp055</i>	10	2352	0.707	0.792	0.760	0.108	0.032
<i>sosp_ng395</i>	8	2458	0.639	0.703	0.654	0.091	0.024
Average	8.175	2254.0	0.448	0.669	0.625	0.333	0.200

Where we denote *k* for the number of visible alleles, *n* for the number of individuals genotyped at the located locus,  $H_O$  and  $H_E$  for the observed and expected heterozygosities, PIC for the polymorphic information content, *f* for the inbreeding coefficient, and  $p_y$  for the frequency of null allele.

Table S3: Genetic diversity of the top 40 highest arbitrarily chosen alphabetically ranked microsatellite loci taken from Nietlisbach et al. (2015) dataset

Locus	<i>k</i>	<i>n</i>	$H_O$	$H_E$	PIC	<i>f</i>	$p_y$
<i>Escu01</i>	10	3234	0.776	0.771	0.737	-0.007	0.000
<i>Gf005</i>	15	2072	0.863	0.862	0.848	-0.002	0.000
<i>Mme001</i>	9	1825	0.678	0.694	0.656	0.023	0.000
<i>Mme02</i>	17	3289	0.798	0.802	0.779	0.005	0.000
<i>Mme08</i>	9	3279	0.842	0.839	0.818	-0.004	0.000
<i>Mme12</i>	10	3271	0.536	0.535	0.507	-0.001	0.000
<i>sosp_ng001</i>	5	2378	0.745	0.753	0.712	0.010	0.000
<i>sosp_ng002</i>	3	2378	0.496	0.489	0.372	-0.015	0.000
<i>sosp_ng004</i>	10	2237	0.488	0.482	0.461	-0.012	0.000
<i>sosp_ng005</i>	5	2193	0.252	0.534	0.427	0.529	0.342
<i>sosp_ng006</i>	9	2262	0.472	0.467	0.414	-0.010	0.000
<i>sosp_ng007</i>	3	2423	0.544	0.525	0.412	-0.036	0.000
<i>sosp_ng008</i>	11	2437	0.807	0.863	0.847	0.065	0.007
<i>sosp_ng012</i>	7	2387	0.629	0.621	0.550	-0.012	0.000
<i>sosp_ng014</i>	12	2339	0.501	0.634	0.590	0.210	0.097
<i>sosp_ng022</i>	5	2367	0.288	0.403	0.371	0.286	0.145
<i>sosp_ng023</i>	9	1875	0.361	0.807	0.781	0.554	0.368
<i>sosp_ng024</i>	9	2283	0.745	0.784	0.754	0.050	0.000
<i>sosp_ng033</i>	5	2379	0.699	0.708	0.658	0.012	0.000
<i>sosp_ng034</i>	12	2446	0.672	0.686	0.664	0.020	0.000
<i>sosp_ng037</i>	7	2417	0.714	0.724	0.684	0.013	0.000
<i>sosp_ng040</i>	16	2381	0.859	0.854	0.837	-0.006	0.000
<i>sosp_ng042</i>	5	2169	0.298	0.518	0.464	0.425	0.248
<i>sosp_ng045</i>	4	2432	0.386	0.374	0.333	-0.033	0.000
<i>sosp_ng048</i>	8	2128	0.761	0.753	0.711	-0.011	0.000
<i>sosp_ng053</i>	4	2358	0.377	0.402	0.349	0.061	0.009
<i>sosp_ng054</i>	16	2352	0.795	0.807	0.784	0.015	0.000
<i>sosp_ng055</i>	7	2401	0.653	0.739	0.696	0.117	0.038
<i>sosp_ng058</i>	7	2424	0.771	0.780	0.747	0.011	0.000
<i>sosp_ng066</i>	5	2384	0.529	0.598	0.523	0.116	0.035
<i>sosp_ng068</i>	9	2322	0.334	0.656	0.607	0.491	0.312
<i>sosp_ng071</i>	12	2465	0.886	0.879	0.867	-0.007	0.000
<i>sosp_ng072</i>	6	2217	0.596	0.631	0.565	0.055	0.006
<i>sosp_ng074</i>	6	2199	0.342	0.640	0.581	0.467	0.286
<i>sosp_ng079</i>	4	2375	0.352	0.575	0.513	0.388	0.218
<i>sosp_ng081</i>	10	2356	0.732	0.746	0.713	0.018	0.000
<i>sosp_ng082</i>	15	2404	0.761	0.822	0.801	0.074	0.013
<i>sosp_ng083</i>	9	2431	0.270	0.270	0.258	0.000	0.000
<i>sosp_ng086</i>	12	2343	0.765	0.738	0.711	-0.036	0.000
<i>sosp_ng088</i>	12	2448	0.747	0.784	0.755	0.047	0.000
Average	8.725	2409.0	0.603	0.664	0.621	0.097	0.053

The definitions for symbols in the header row are as for Table S1.

# Figures

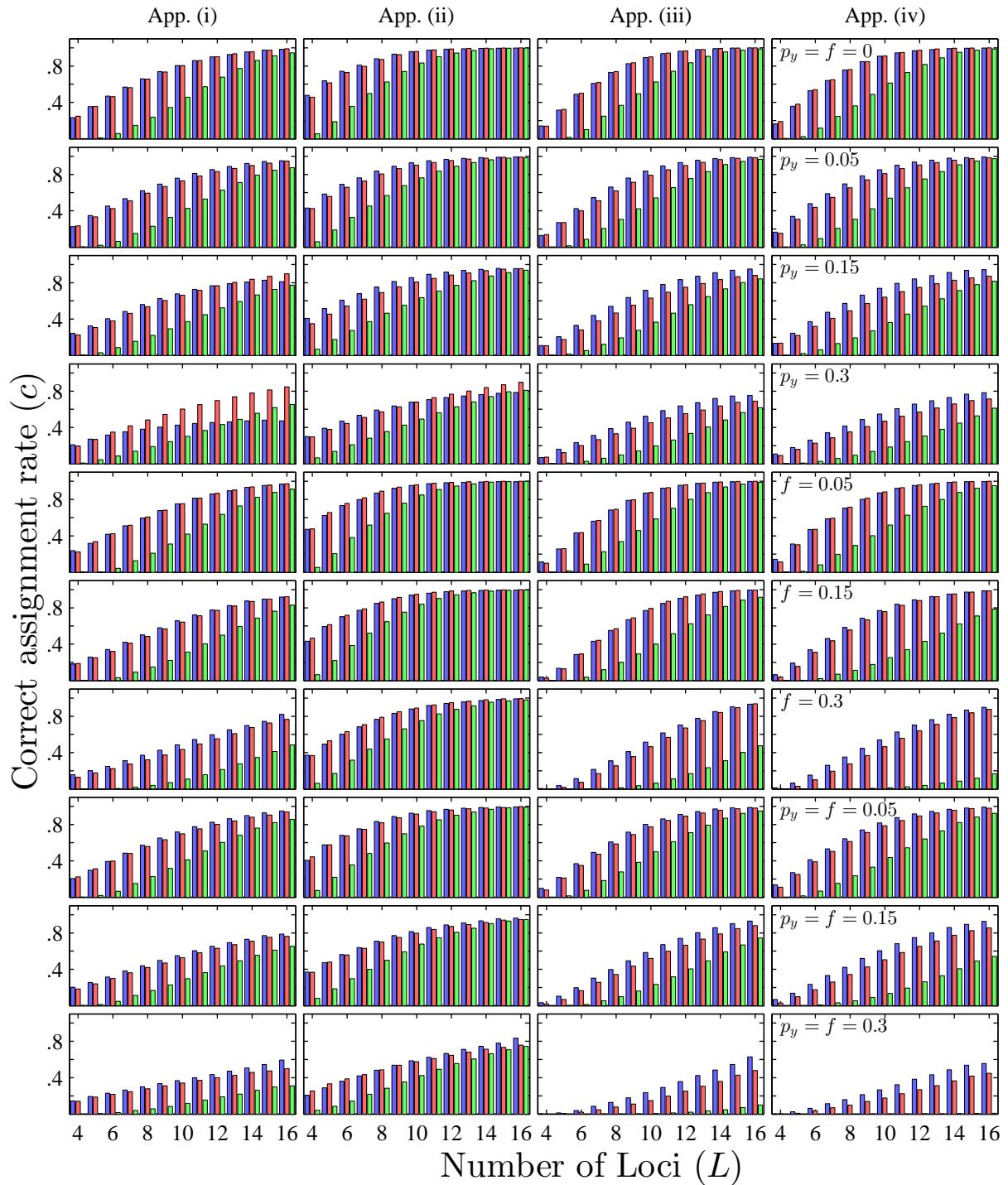


Figure S1: Results of simulated data with the threshold  $\Delta_{0.80}$ . The definitions of bars together with their colors are as for Figure 3.

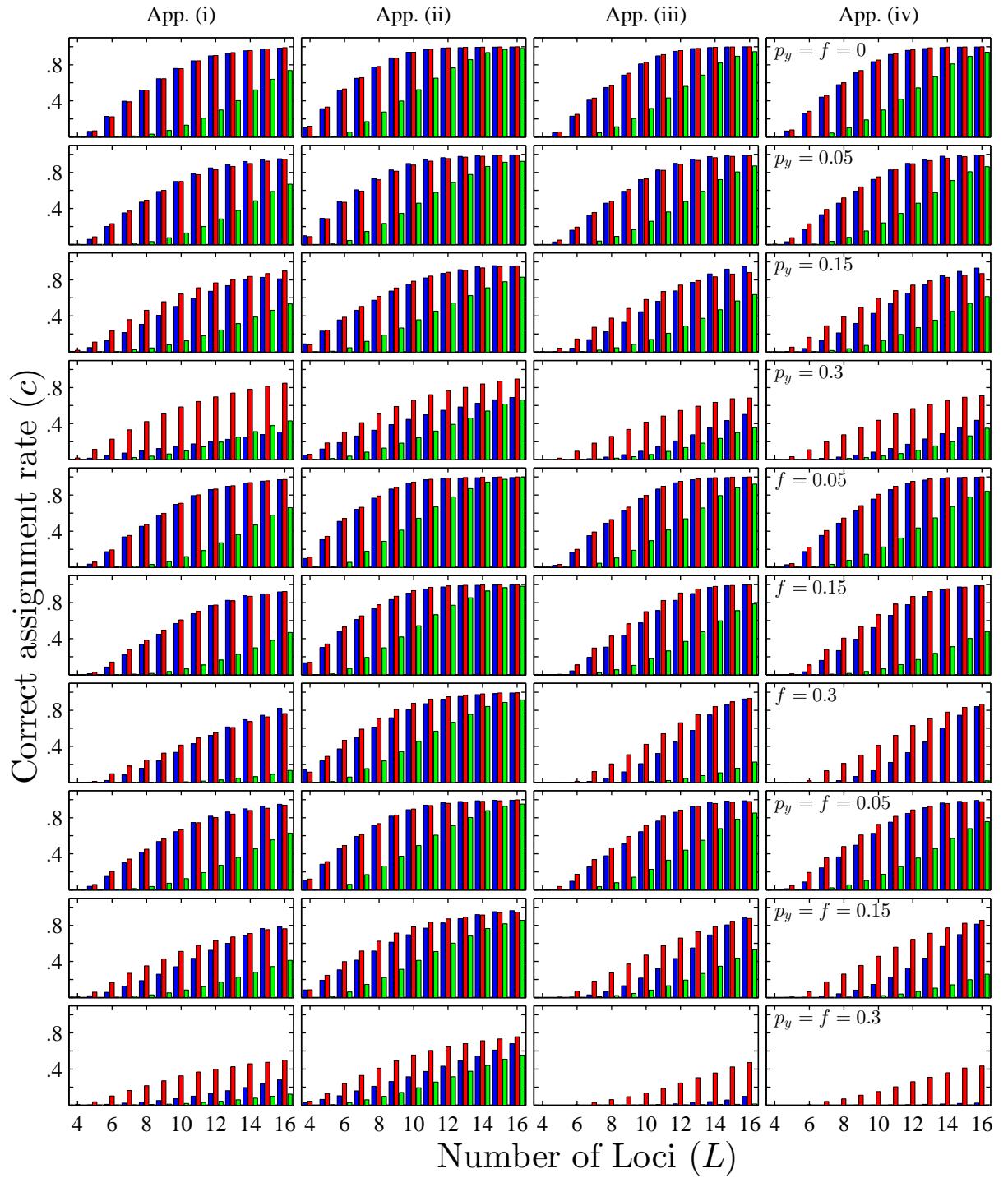


Figure S2: Results of simulated data with the threshold  $\Delta_{0.99}$ . The definitions of bars together with their colors are as for Figure 3.

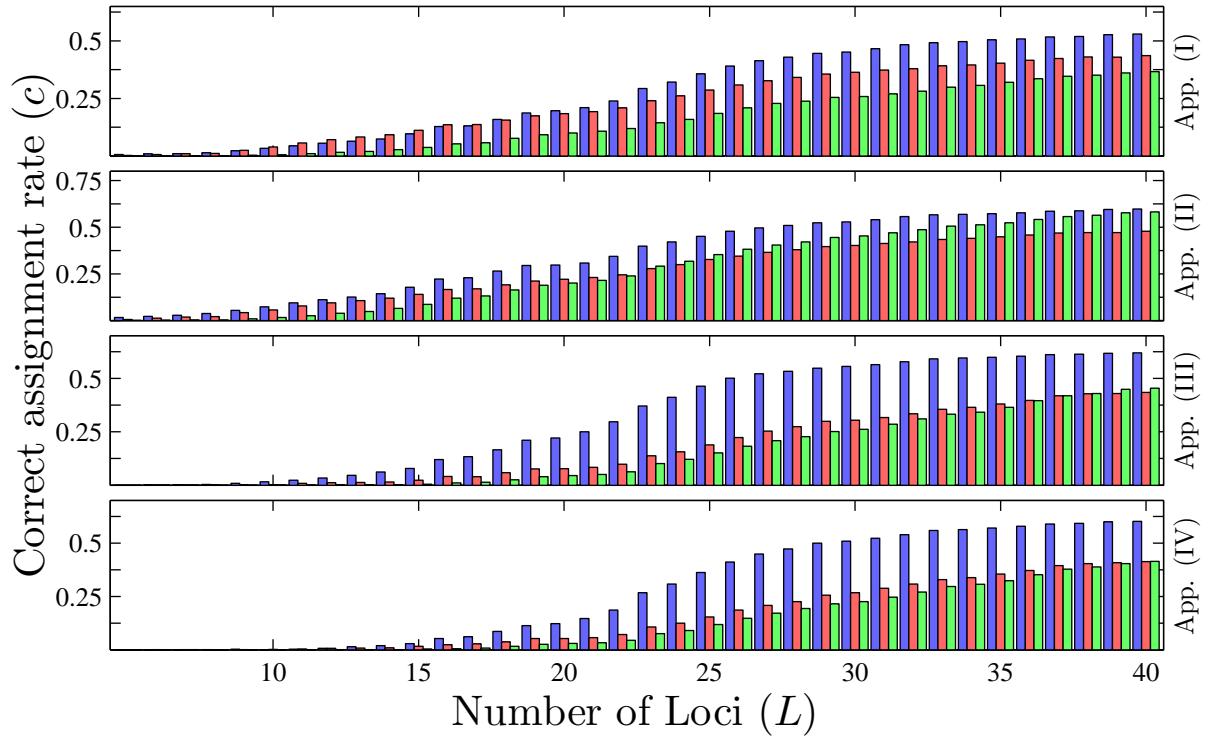


Figure S3: Results of empirical data with the threshold  $\Delta_{0.80}$ . The definitions of bars together with their colors are as for Figure 4.

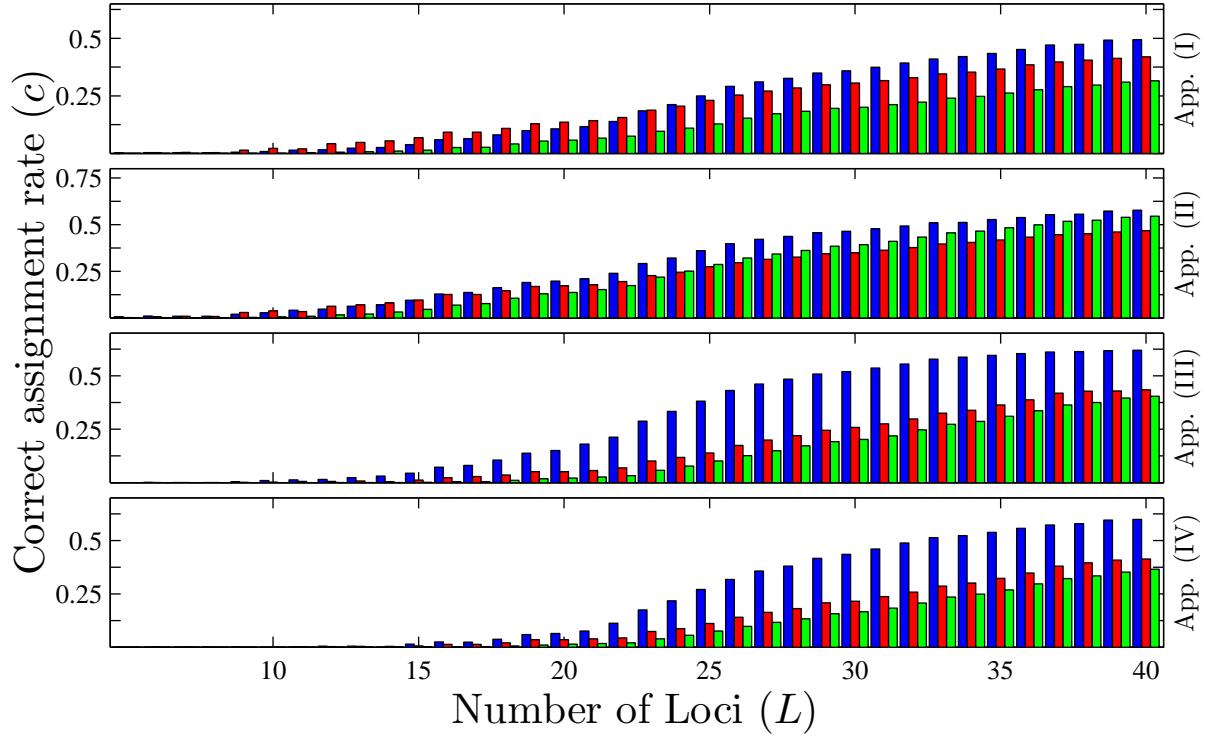


Figure S4: Results of empirical data with the threshold  $\Delta_{0.99}$ . The definitions of bars together with their colors are as for Figure 4.

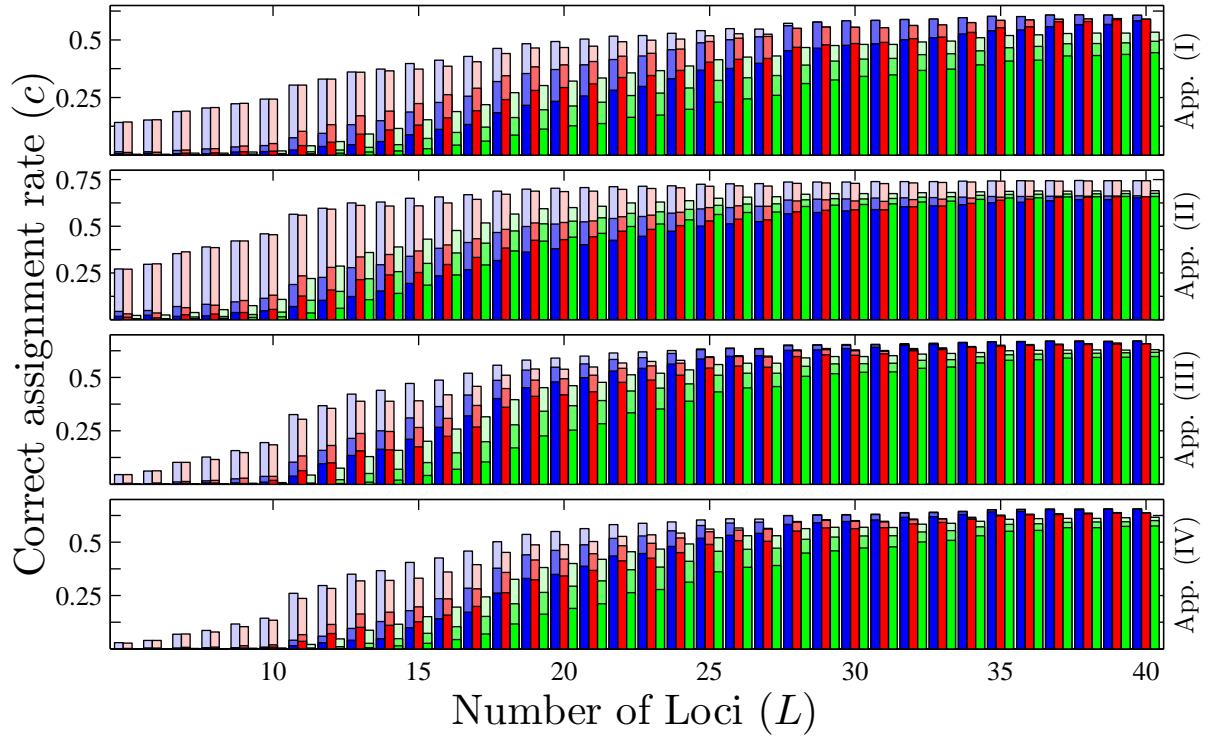


Figure S5: Results of the parentage analysis using the dataset of Nietlisbach et al. (2015), in which the loci chosen are with the highest rank of alphabetical order. Each row denotes an application. The definitions of bars together with their colors are as for Figure 3.

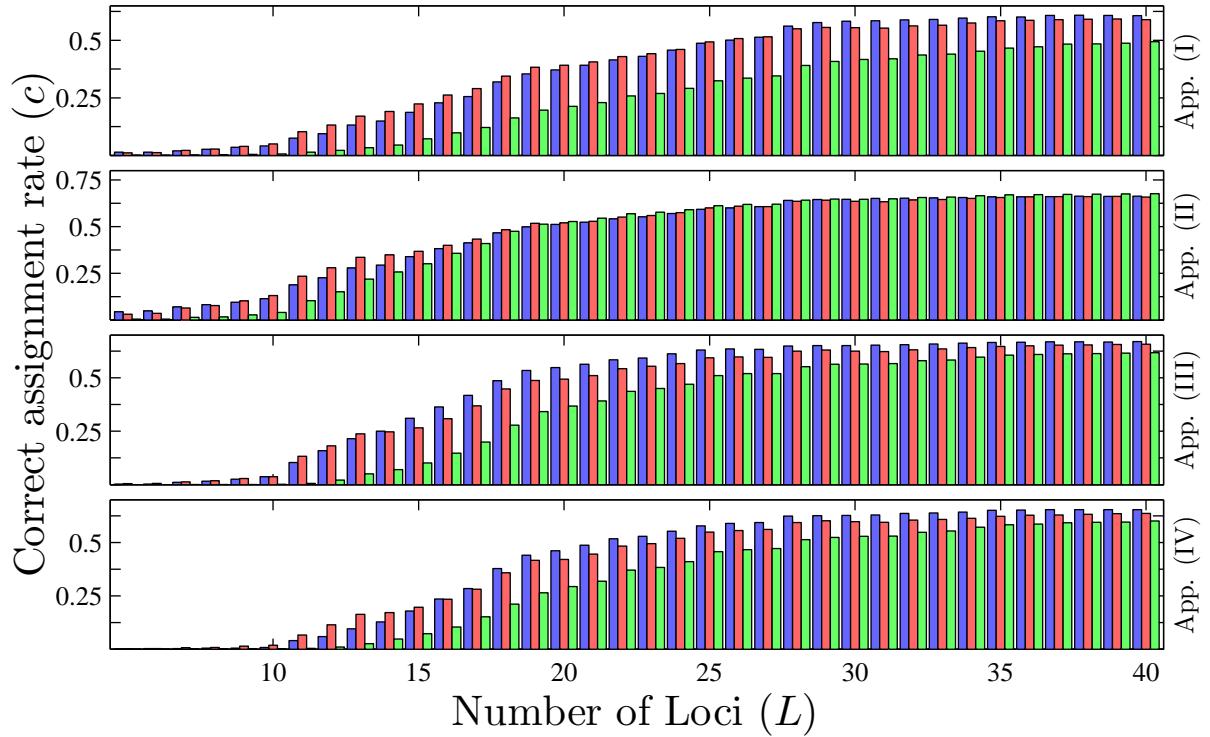


Figure S6: Results of empirical data with the threshold  $\Delta_{0.80}$ . The definitions of bars together with their colors are as for Figure S5.

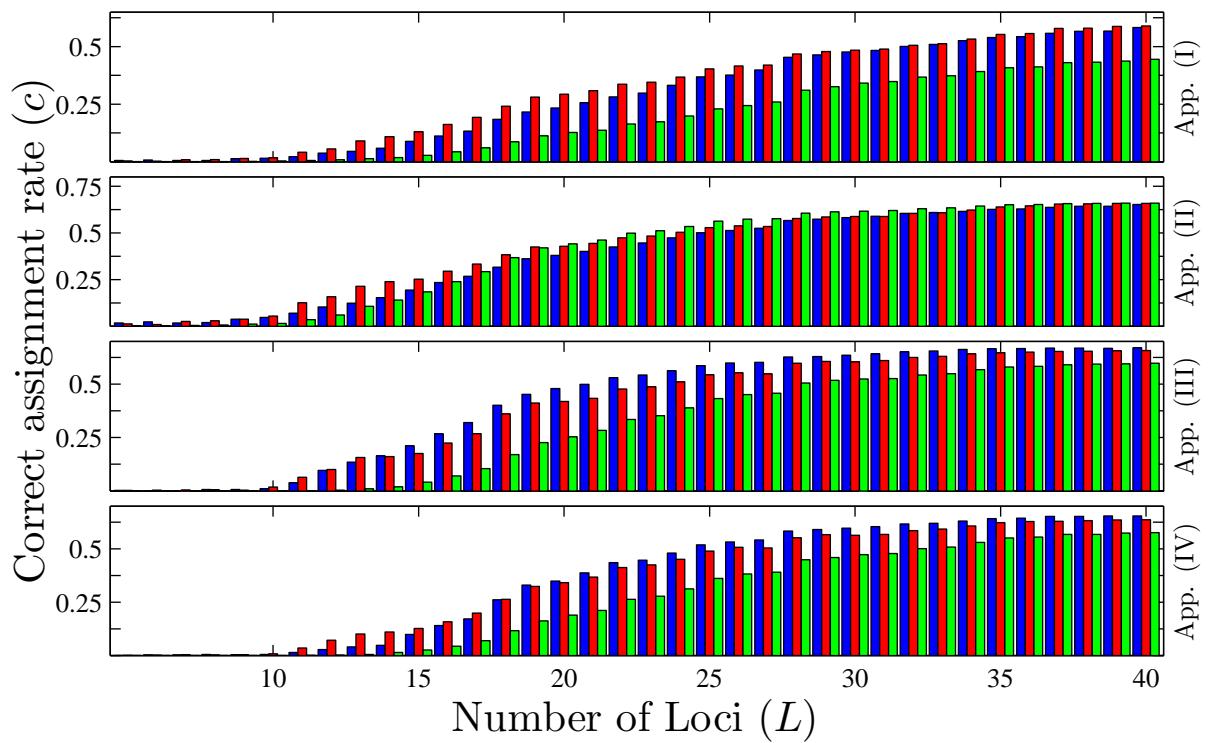


Figure S7: Results of empirical data with the threshold  $\Delta_{0.99}$ . The definitions of bars together with their colors are as for Figure S5.