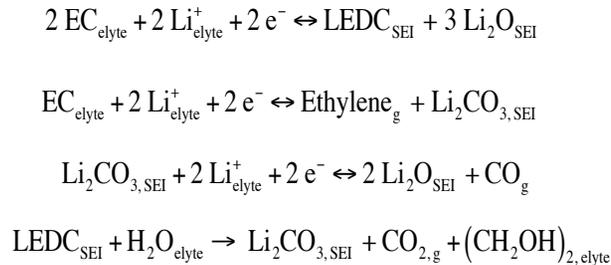
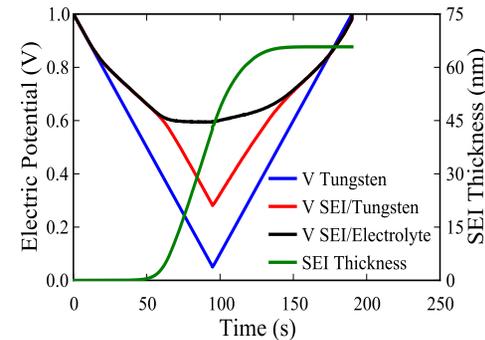


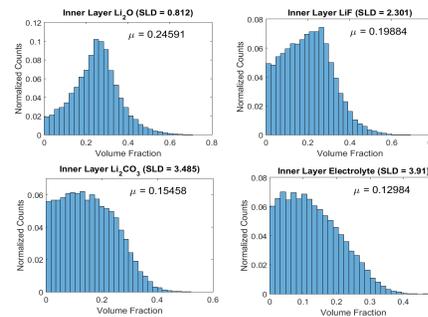
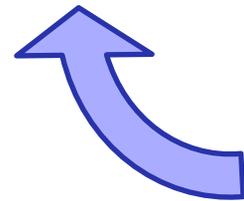
Detailed Chemistry Modeling via Cantera: A Pathway to Understand Li-ion Battery Degradation



Detailed SEI Chemistry



Numerical Simulation



SEI Chemical Composition



Steven C. DeCaluwe

Colorado School of Mines, Mechanical Engineering, Golden, CO

Presented at ECS Data Science Showcase
Monday, 01 October, 2018





Acknowledgements

Colorado School of Mines

At Colorado School of Mines:

- Christopher H. Lee (MS, 2016)
- Daniel Korff (Current PhD Student)
- Amy LeBar (Current MS Student)
- Center for High Performance Computing

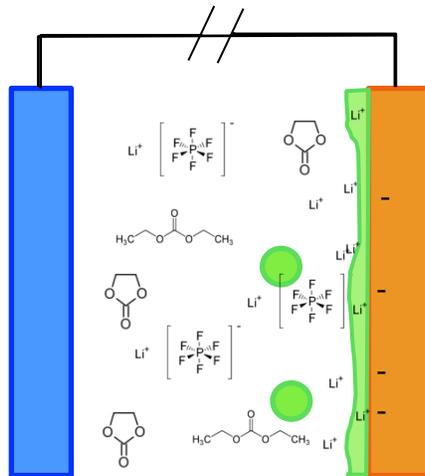
At the NCNR:

- Joseph A. Dura, Eric D. Rus – Neutron Reflectometry
- Paul Kienzle – Refl1D Fitting software

Financial Support

- **US Office of Naval Research, Award#: N00014-14-1-0059 (Program Manager: Dr. Michele Anderson).**
- **Dept. of Energy BES, Early Career, Award # DE-SC0018019 (Program Manager: Dr. Pappan Thiyagarajan).**
- **State of Colorado Energy Research Collaboratory, Seed Grant (Program contact: Maury Dobbie)**

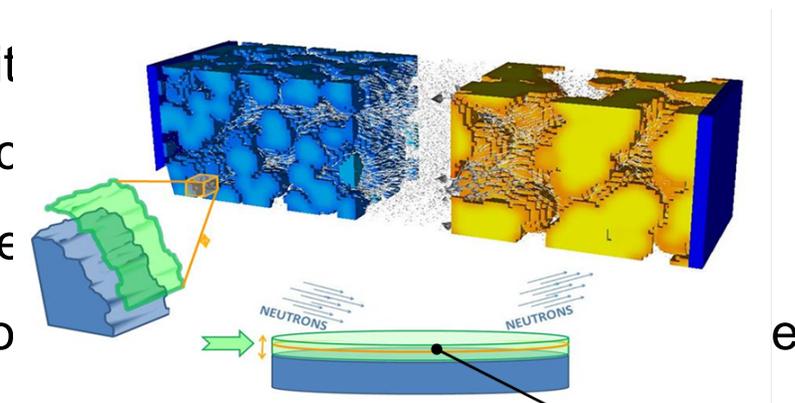
Lithium batteries: promise, challenges, and the SEI (2)



- Because the electrolyte breaks down at the bare anode, LIBs cannot operate without a passivation layer.
 - Electrolyte formulations create a passivating film from the decomposition products: Solid Electrolyte Interphase (SEI).

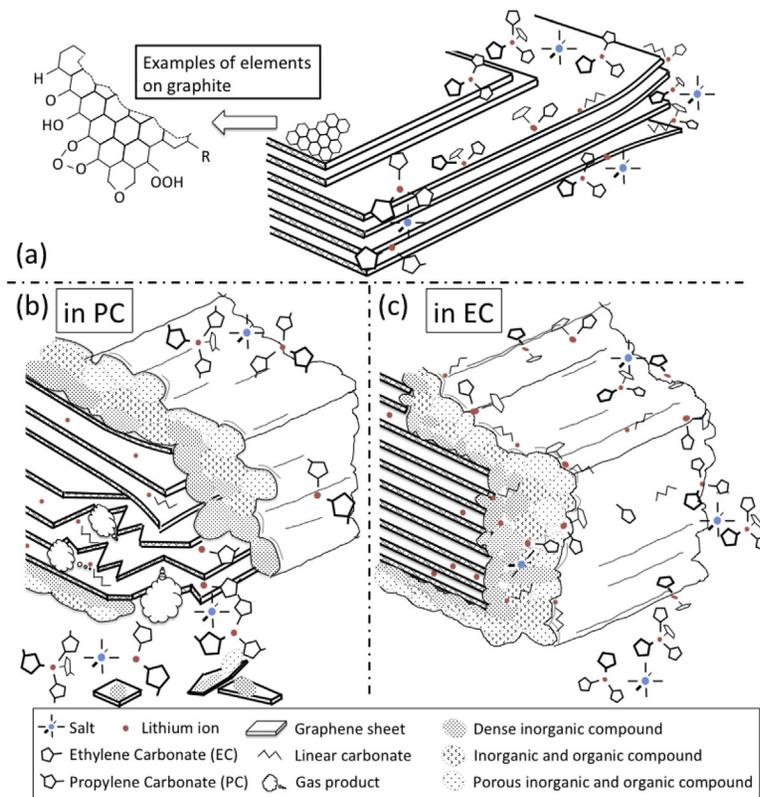
• In reality, continued SEI growth during battery operation decreases device durability and efficiency.

- Long-term capacity fade due to Li⁺ crossover
- Durability and safety issues – SEI delamination
- Higher resistance, lower power – slow interface.



Reduce electrolyte on working electrode (non intercalating) to form SEI

State of SEI Understanding (1)



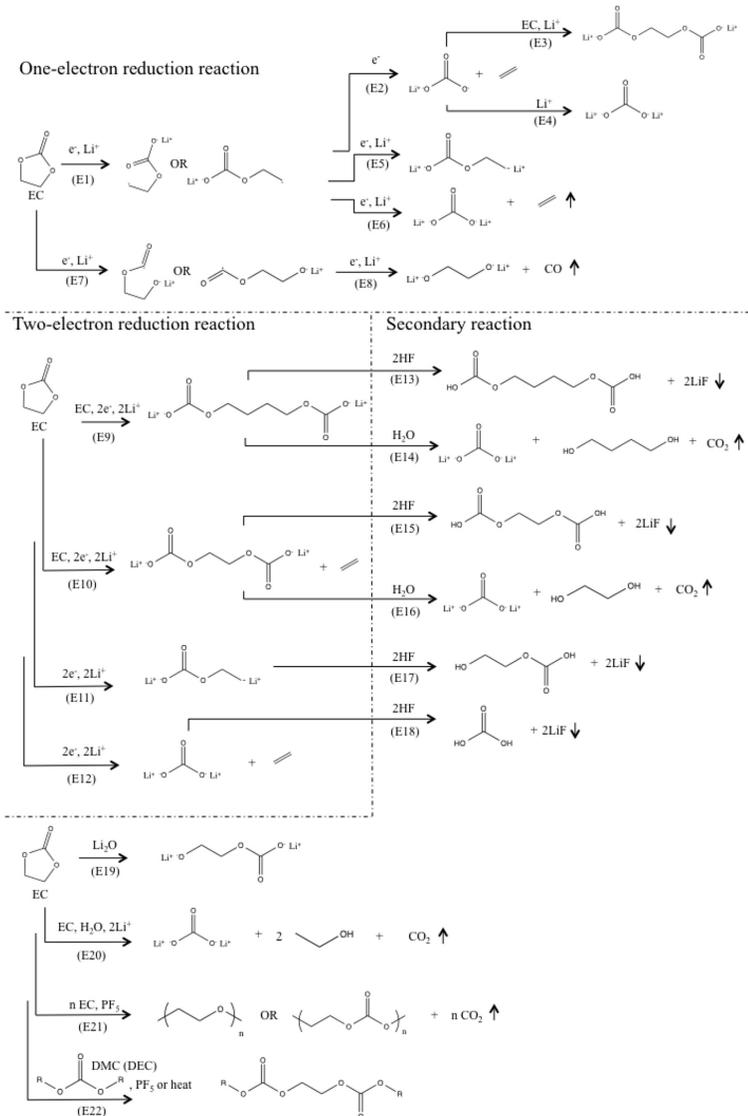
Potential vs. Li/Li⁺

< 1.4V
SEI formation
from additive

< 0.9V
SEI formation
from electrolyte

< 0.2V
Lithium intercalation
& SEI formation

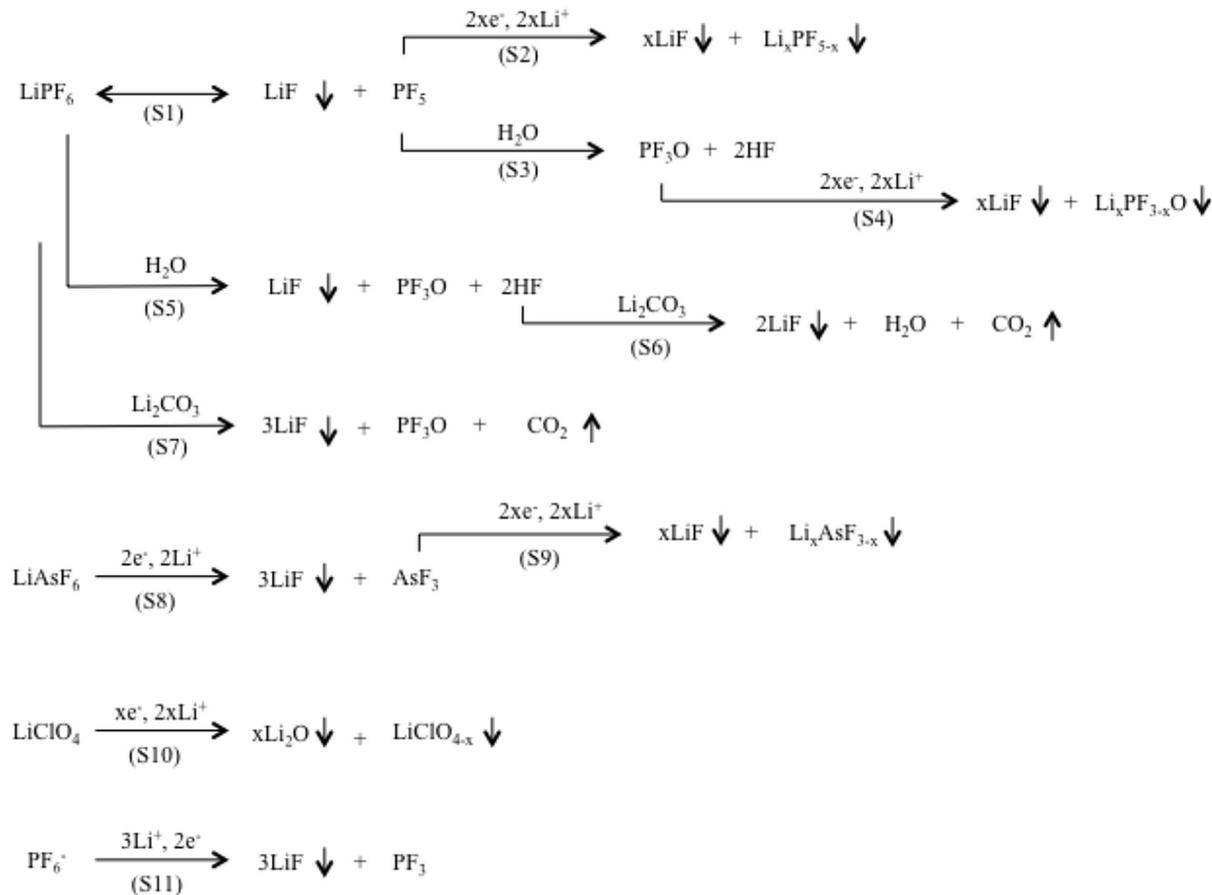
0V



An, et al., Carbon (2016)

Fig. 8. Ethylene carbonate (EC) reduction process (reference groups in parentheses; details are shown in Table 2).

State of SEI Understanding (3)



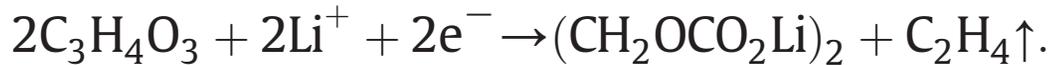
An, et al., *Carbon* (2016)

Outline

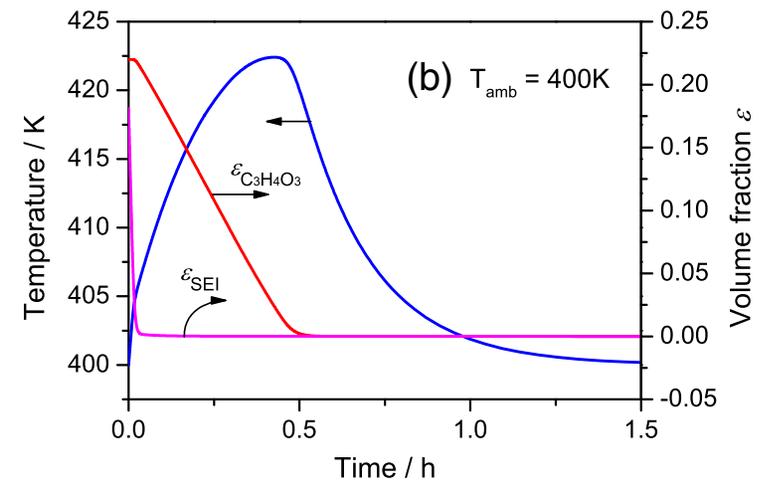
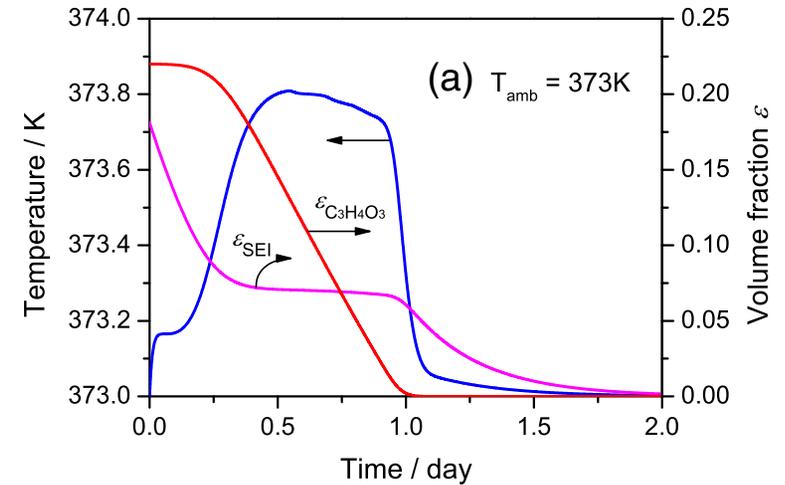
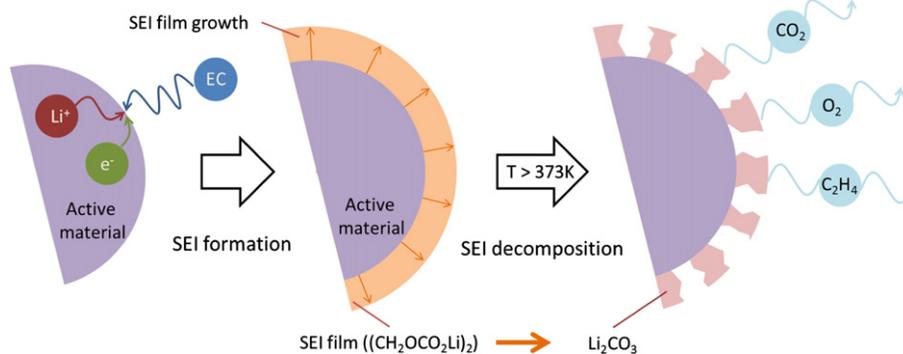
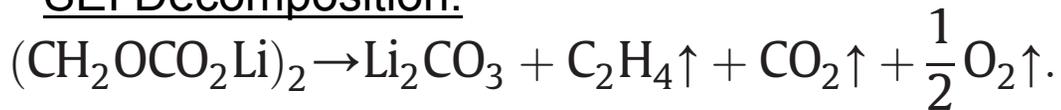
- Introduction: Current understanding of the SEI
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(Solid State Ionics, 2014)

SEI Growth:

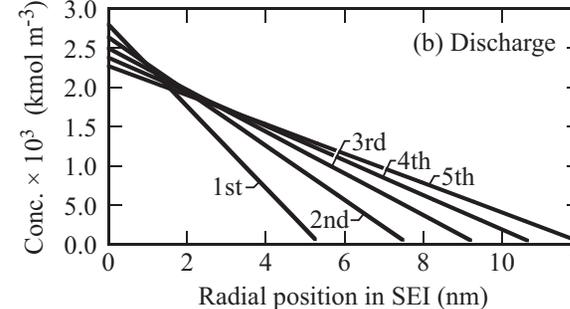
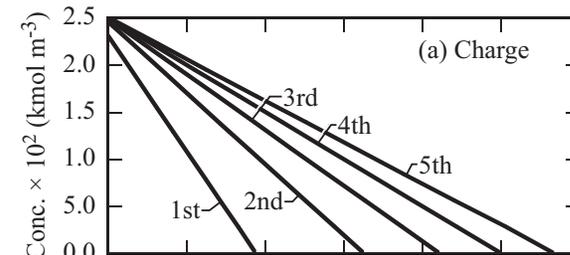
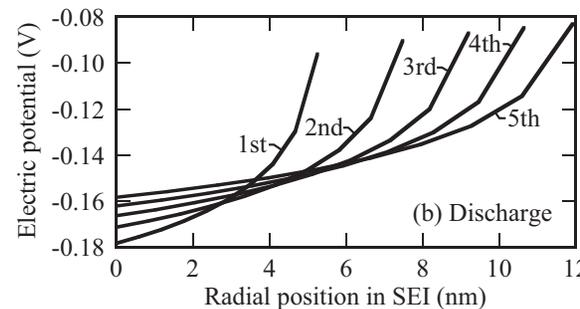
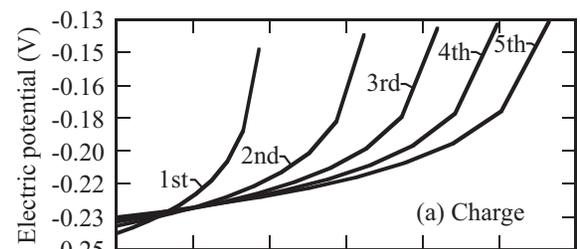


SEI Decomposition:



(Electrochimica Acta, 2011)

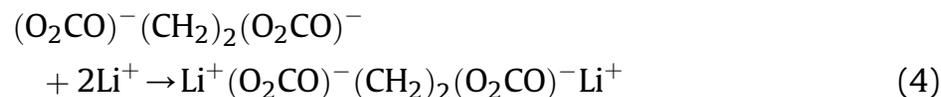
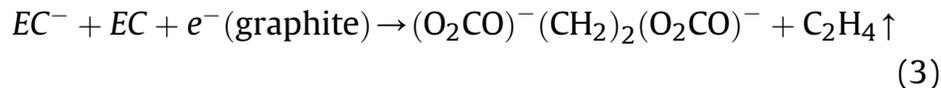
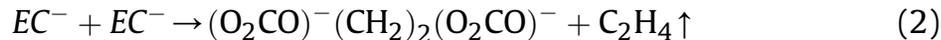
	Reaction
<i>SEI-electrolyte interface</i>	
1	$C_3H_4O_3(E) + (S^s) \rightleftharpoons C_3H_4O_3(S^s)$
2	$Li^+(S^s) \rightleftharpoons Li^+(E) + (S^s)$
3	$C_2H_4(E) + 2(S^s) \rightleftharpoons C_2H_4(S^s)$
4	$C_3H_4O_3^-(S^s) \rightleftharpoons C_3H_4O_3(S^s) + e_{S^b}^-$
5	$C_2H_4(S^s) + CO_3^{2-}(S^s) \rightleftharpoons C_3H_4O_3^-(S^s) + e_{C_b}^- + 2(S^s)$
6	$CO_3^{2-}(S^s) + 2Li^+(S^s) + (S^b) \rightleftharpoons Li_2CO_3(S^b) + 3(S^s)$
7	$Li(S^b) + (S^s) \rightleftharpoons V^-(S^b) + Li^+(S^s)$
8	$Li_{S^b}^+ + (S^s) \rightleftharpoons Li^+(S^s)$
<i>Graphite-SEI interface</i>	
9	$e_{S^b}^- \rightleftharpoons e_{C_6}^-$
10	$Li(C_6) + V^-(S^b) \rightleftharpoons Li(S^b) + e_{C_6}^- + (C_6)$
11	$Li(C_6) \rightleftharpoons Li_{S^b}^+ + e_{C_6}^- + (C_6)$



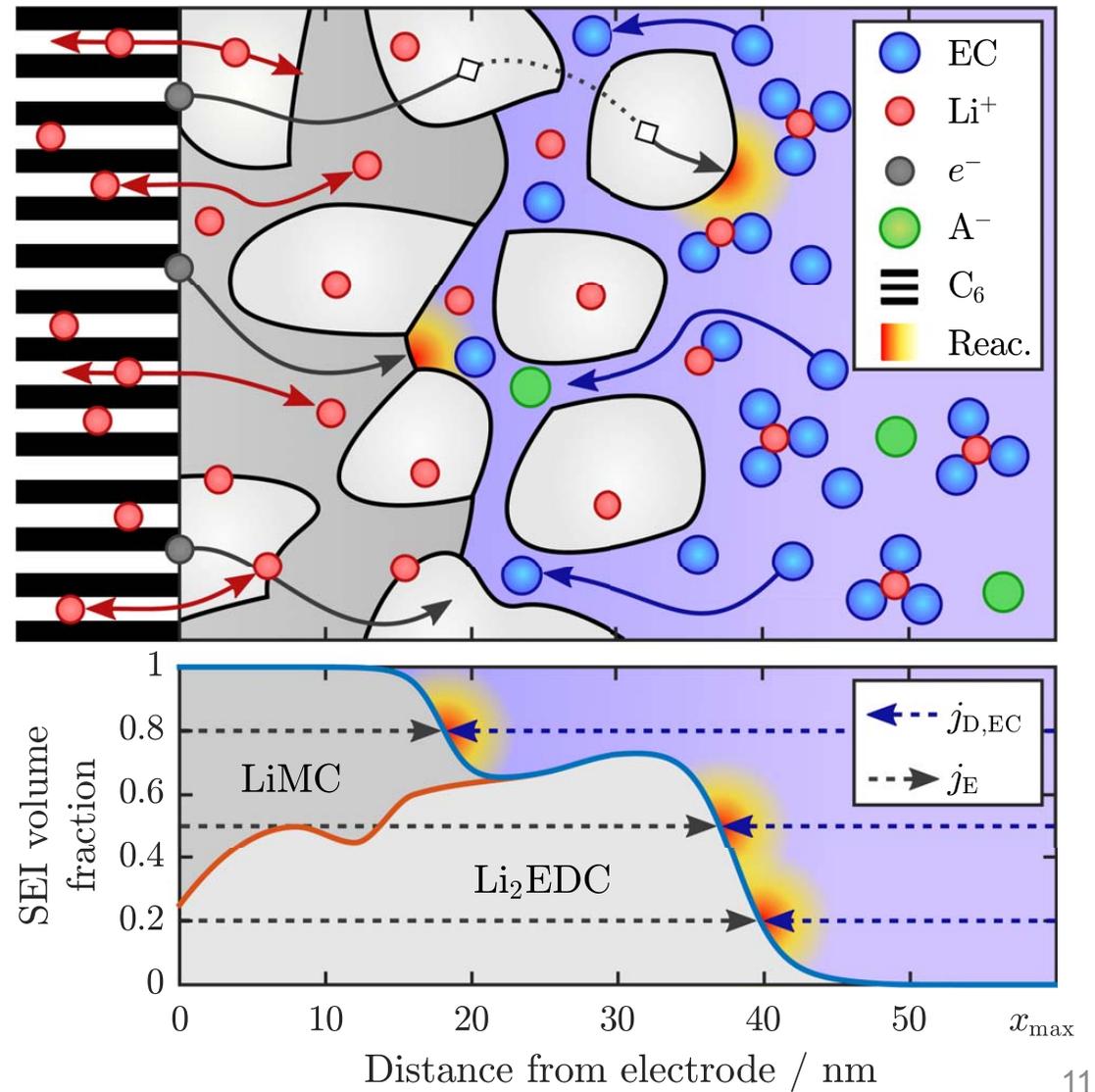
Kupper and Bessler, JECS 2017

Layer	Phase	Initial volume fraction ϵ	Density $\rho/\text{kg} \cdot \text{m}^{-3}$	Species (initial mole fraction X)
Cathode	Cathode active material	0.67 ¹⁰¹	1510 ¹⁰¹	Li[LFP] (0.01), V[LFP] (0.99)
	Electrolyte	0.28 ^{**101}	1130 ¹⁰¹	C ₃ H ₄ O ₃ (l) (0.6), C ₄ H ₆ O ₃ (0.2), Li ⁺ (solv) (0.1), PF ₆ ⁻ (solv) (0.1)
	Gas phase cathode	0.05 ^{**}	1.14 ¹⁰⁴	N ₂ (0.999), C ₃ H ₄ O ₃ (g) (1.0 · 10 ⁻⁸), C ₂ H ₄ (1.0 · 10 ⁻⁸), O ₂ (1.0 · 10 ⁻⁸), CO ₂ (1.0 · 10 ⁻⁸), H ₂ O (1.0 · 10 ⁻⁸), H ₂ (1.0 · 10 ⁻⁸)
Separator	Separator	0.5 ¹⁰⁵	200 ¹⁰⁶	Separator (1.0)
	Electrolyte	0.5 ¹⁰⁵	1130 ¹⁰¹	C ₃ H ₄ O ₃ (l) (0.6), C ₄ H ₆ O ₃ (0.2), Li ⁺ (solv) (0.1), PF ₆ ⁻ (solv) (0.1)
Anode	Anode active material	0.72 ¹⁰¹	2540 ¹⁰¹	Li[C ₆] (0.57), V[C ₆] (0.43)
	Electrolyte	0.22 ^{**101}	1130 ¹⁰¹	C ₃ H ₄ O ₃ (l) (0.6), C ₄ H ₆ O ₃ (0.2), Li ⁺ (solv) (0.1), PF ₆ ⁻ (solv) (0.1)
	SEI	0.01 [*]	1300 ¹⁰⁷	(CH ₂ OCO ₂ Li) ₂ (1.0)
	Gas phase anode	0.05 ^{**}	1.14 ¹⁰⁴	N ₂ (0.999), C ₃ H ₄ O ₃ (g) (1.0 · 10 ⁻⁸), C ₂ H ₄ (1.0 · 10 ⁻⁸), O ₂ (1.0 · 10 ⁻⁸), CO ₂ (1.0 · 10 ⁻⁸), H ₂ O (1.0 · 10 ⁻⁸), H ₂ (1.0 · 10 ⁻⁸)

Liu, et al., J Power Sources, 2014



J. Electrochem. Soc. (2017)



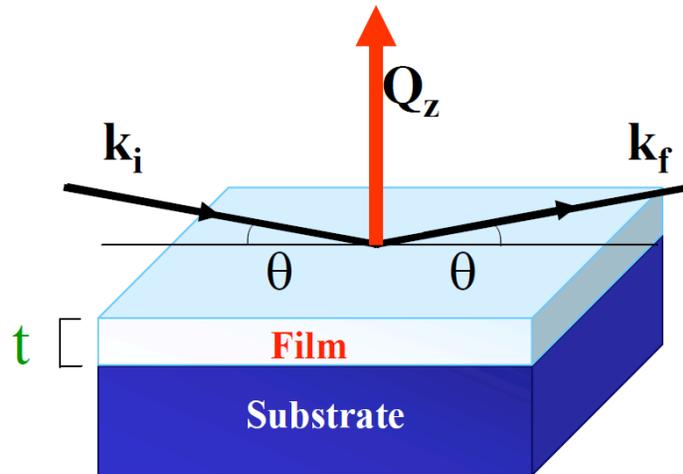
SEI Chemistry Models

- Compared to other fields, “large” SEI mechanisms are small, do not yet reflect the considerable chemical, structural complexity.
- Limited development of detailed chemistry is understandable.
 - Materials constantly evolving
 - Computational tools not widely adopted; each new model must “reinvent the wheel.”
 - Limited *in situ* / *in operando* chemical data available for validation of simulation results.

Outline

- Introduction: Current understanding of the SEI
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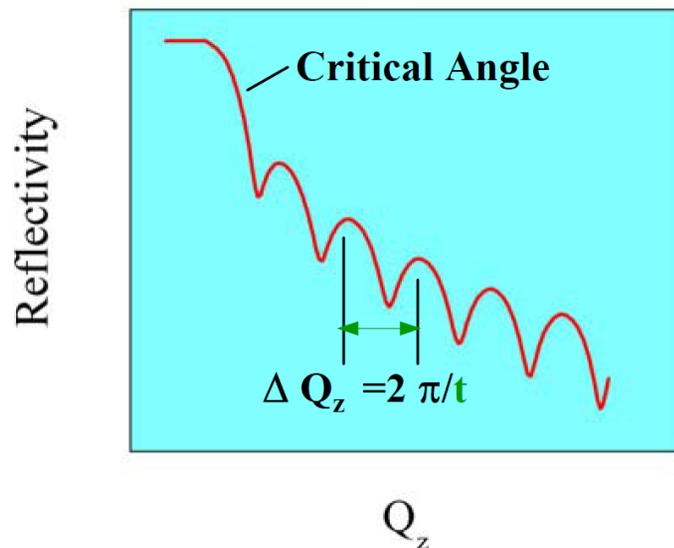
Neutron Reflectometry Overview



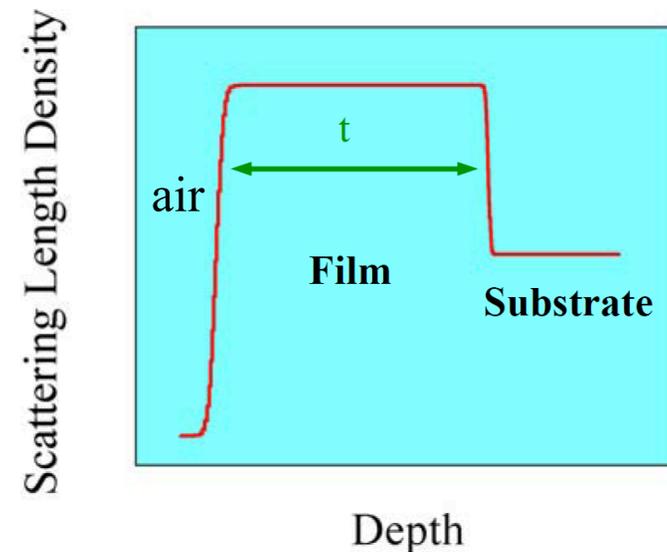
- Measures Reflected Intensity vs. grazing angle θ
- Oscillations with period $2\pi / \text{layer thickness}$
- NR Provides Depth Profile of the SLD
- SLD related to Composition:

$$\text{SLD}(z) = \sum_j \text{SLD}_j V_j$$

$$\text{SLD}(z) = \sum_i b_i n_i$$



Fitting

- **Non-intercalating working electrode (WE)**

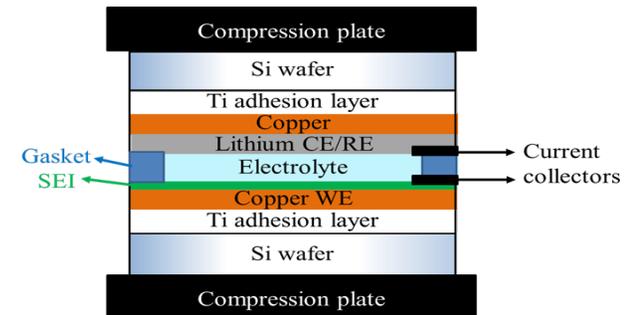
- All charge attributed to SEI chemistry.
- Minimal WE change during experiments.

- **Li metal counter/reference electrode.**

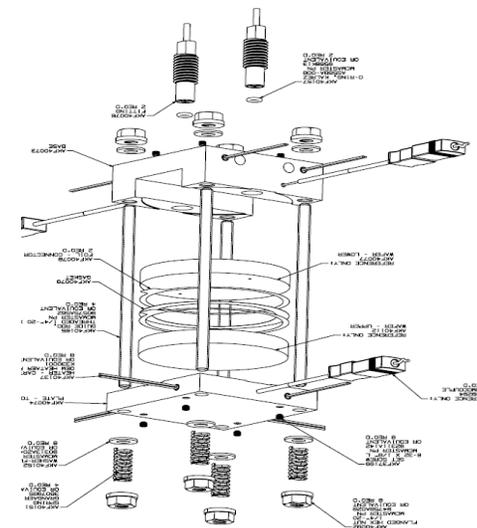
- **Substrate: 5 mm thick polished Si.**

- **Thick (100-500 μm) liquid electrolyte reservoir:**

- Deuteration increases SLD, better contrast with lithiated compounds in SEI.



n



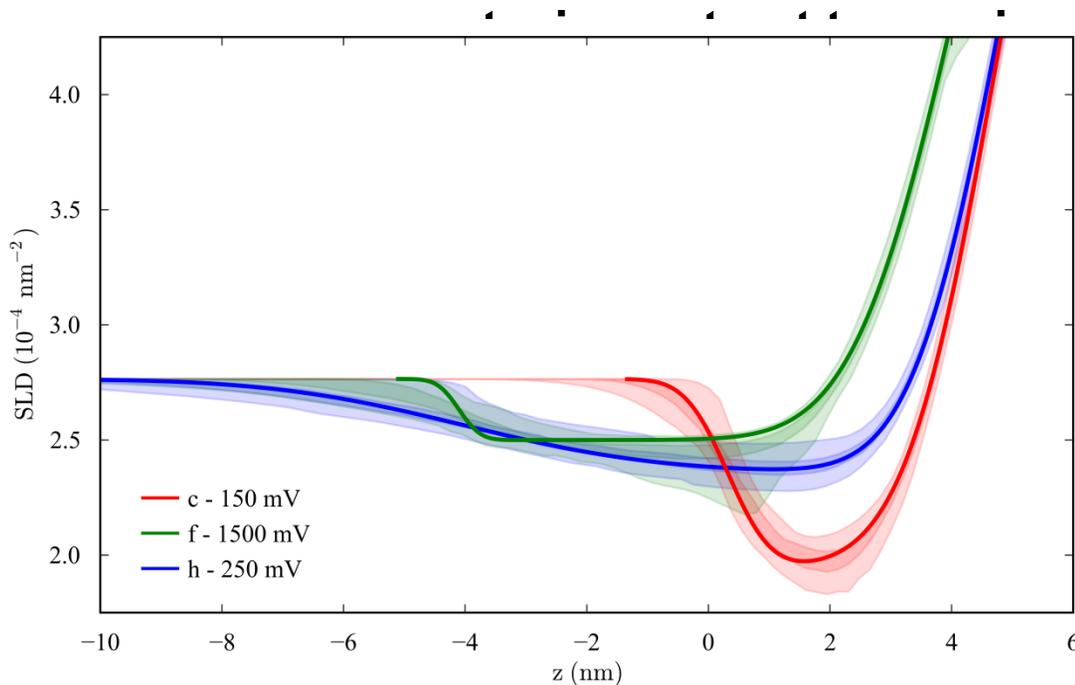
NR of SEI on Cu at Varying Potentials

■ NR results during potentiostatic holds reveal changes to the SEI thickness, composition, and structure with cycling.

-SLD decreases (Li increases) with decreasing WE potential.

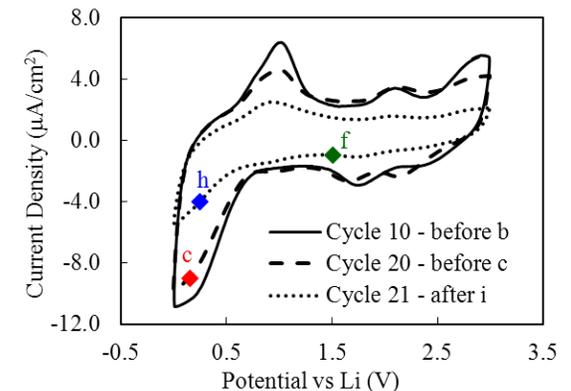
-SEI thickness continues to increase with additional processing.

-Some test points show composition gradients; others show mixing of SEI



assumptions from *ex situ* data.

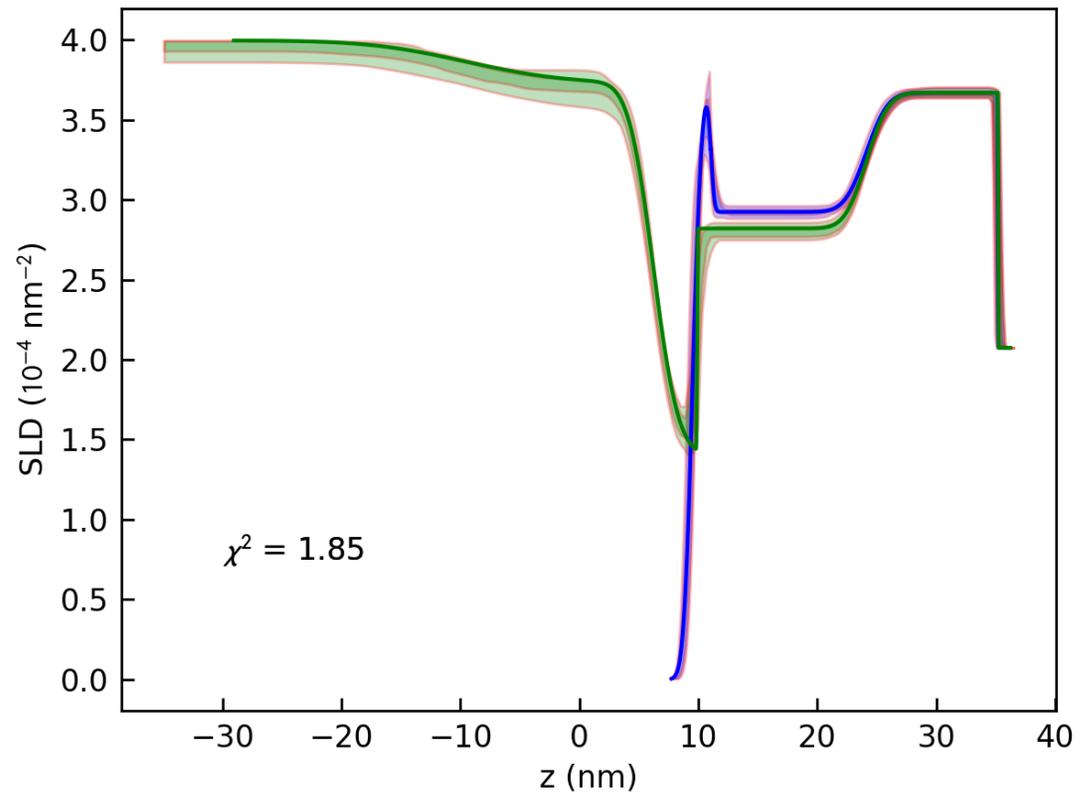
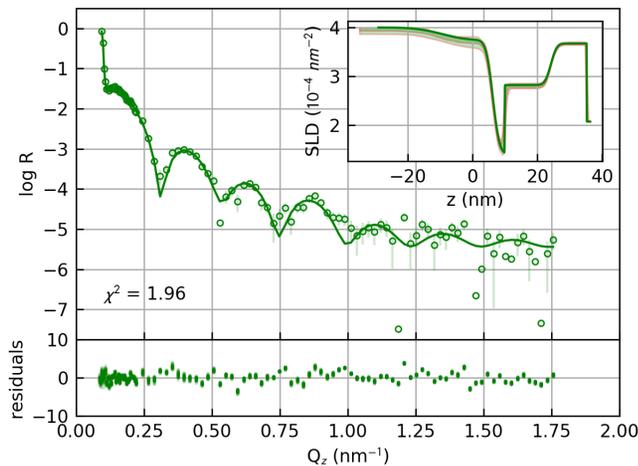
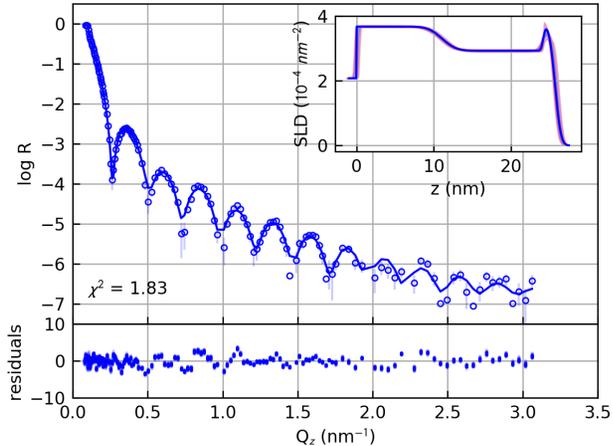
V vs. Li/Li



NR of SEI on Tungsten Directly Reveals Hypothesized Two-layer Structure

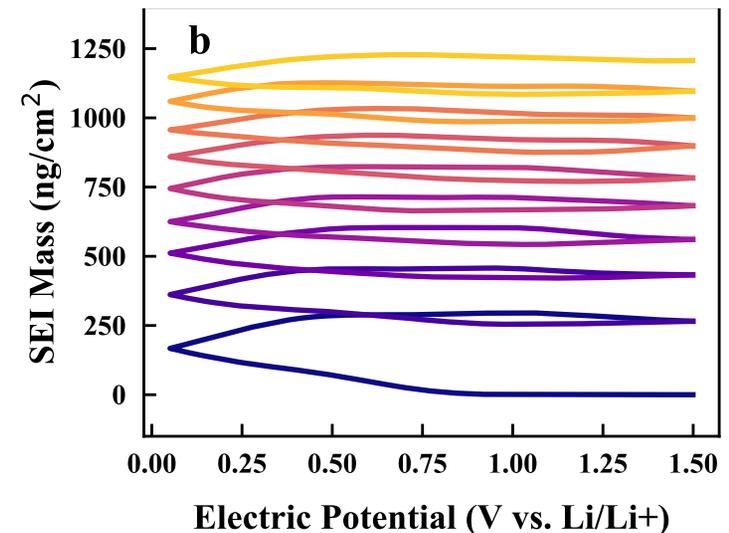
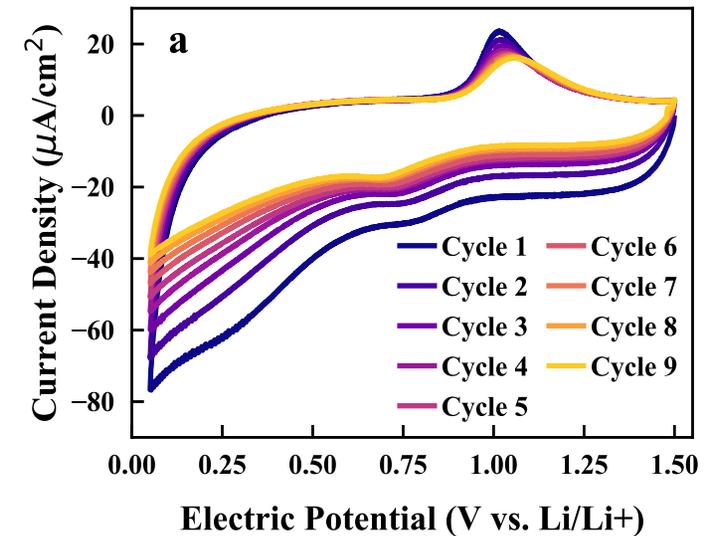
■ Two layer SEI structure

- Denser "inner" SEI – 3.7 nm
- Porous "outer" SEI – 15.3 nm



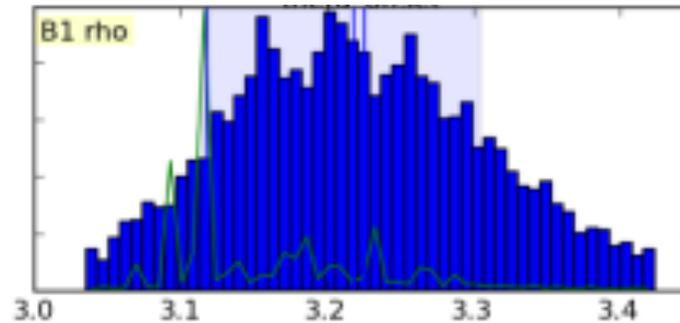
EQCM-D Shows Growth, Re-dissolution of SEI

- Reduction peak at 800 mV: electrolyte decomposition
- Reduction peak at 275 mV, oxidation peak at 1.1 V: lithium underpotential deposition, stripping
- Decrease in mass gain per cycle – passivation and partial SEI dissolution



NR + QCM Provides Detailed Look at SEI Chemistry

- NR gives thickness and SLD



- EQCM-D determines SEI mass
- Monte Carlo model of SEI chemical composition
 - Randomly generate mole fractions, choose thickness from fitted distribution
 - Calculate SLD and Mass for the generated composition and thicknesses (inner & outer layer).
 - Mass must fall within uncertainty window of QCM data
 - Compare SLD values to probability distribution function from NR, use Metropolis Algorithm to choose “likely” models.

Inner SEI:

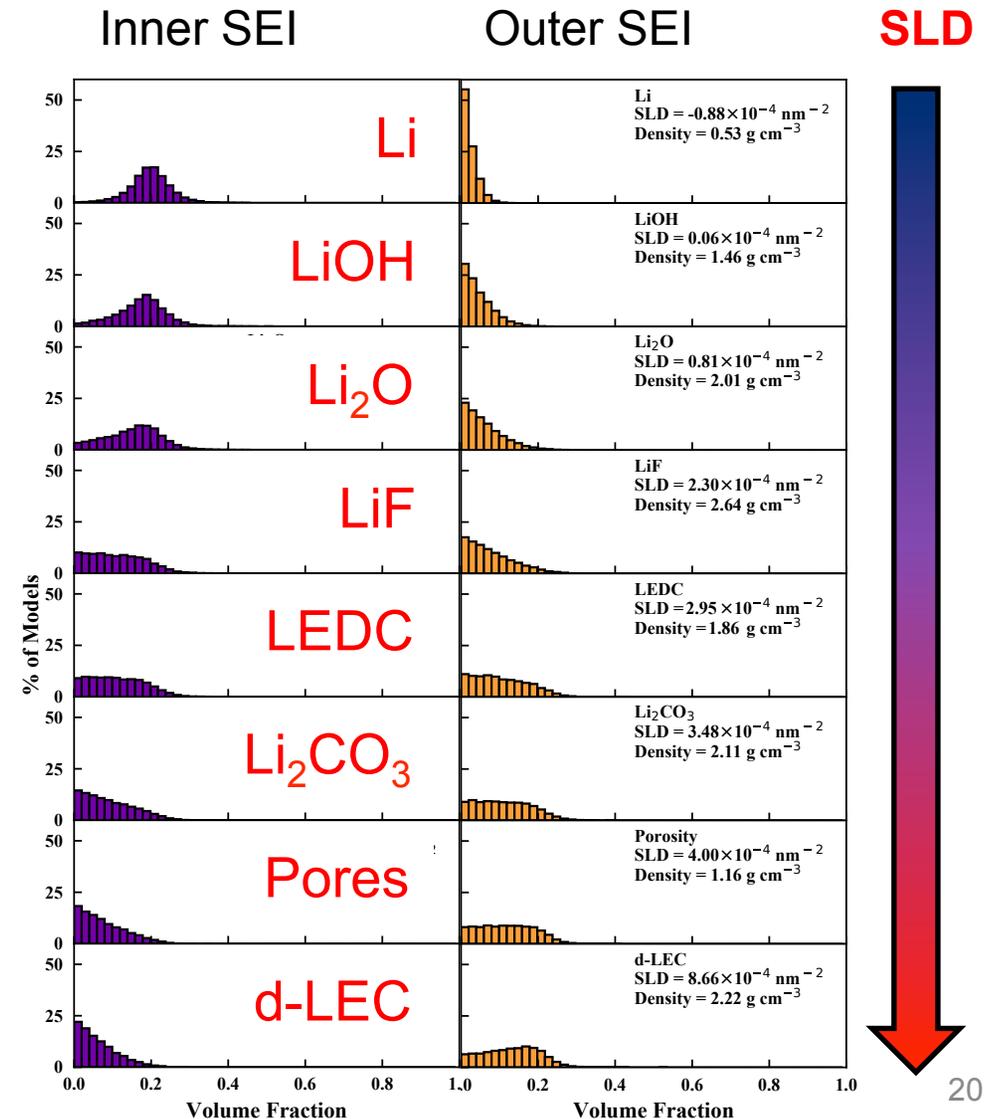
Low-SLD components most prominent
Li, LiOH, Li₂O, but all below 30%.

Outer SEI:

High-SLD components most prominent
Li Ethyl Carbonate, Electrolyte/
pores

Intermediate SLD components: not really discriminated

Lower noise in QCM-D needed to determine composition with greater resolution.



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- Growth of SEI modeled via elementary electrochemistry:

$$\dot{q}_i = k_{\text{fwd}} \prod_j a_j^{v_{j,i,\text{fwd}}} - k_{\text{rev}} \prod_j a_j^{v_{j,i,\text{rev}}}$$

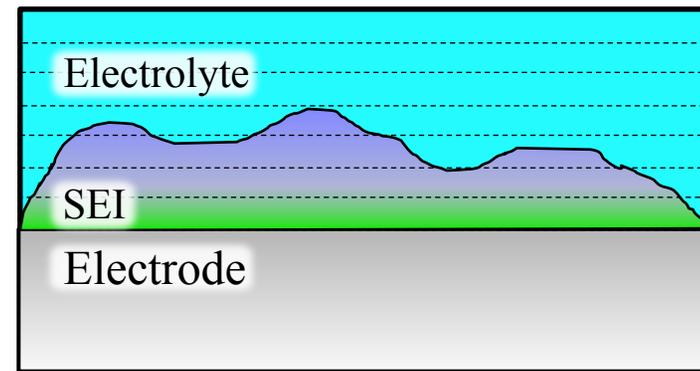
where:

$$k_{\text{fwd}} = k_{\text{fwd}}^\circ \exp\left(\frac{nF\beta\Delta\phi}{RT}\right)$$

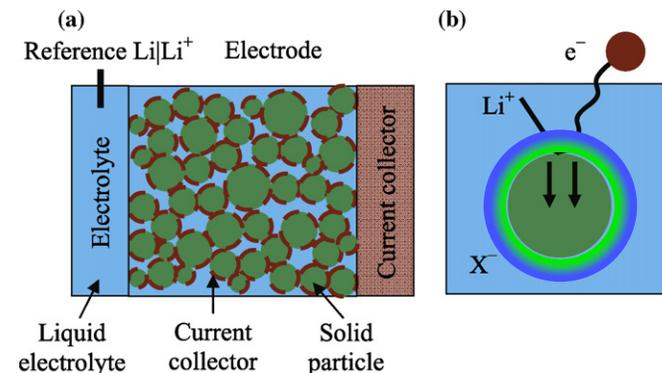
$$k_{\text{rev}} = k_{\text{rev}}^\circ \exp\left(\frac{nF(1-\beta)\Delta\phi}{RT}\right)$$

- Initial model: planar, non-intercalating “model” electrode
- Depth profiling enabled by dividing electrolyte at electrode surface into volumes.

Step 1: Model electrode

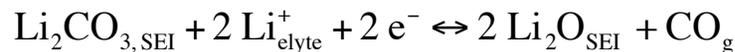
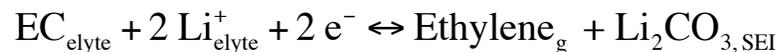
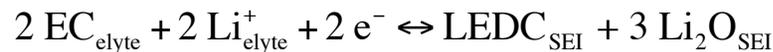


Step 2: Newman-type model



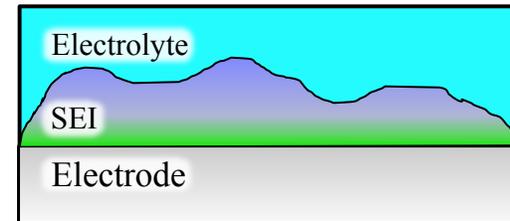
W. Lai, F. Ciucci, Electrochimica Acta, 2011

■ Simple SEI chemistry:



- Charge transfer capacitance, (electro)chemical reaction rates, SEI resistance all are tunable parameters.

- Simulate a simple CV curve between 1.0 V and 0.05 V, at a scan rate of 10 mV/s.



SEI Growth Rate:

$$\frac{\partial \phi_{\text{SEI}}}{\partial t} = \sum_{k,\text{SEI}} \frac{W_k}{\rho_k \Delta z} \dot{s}_k$$

Charge Transfer:

SEI / W anode:

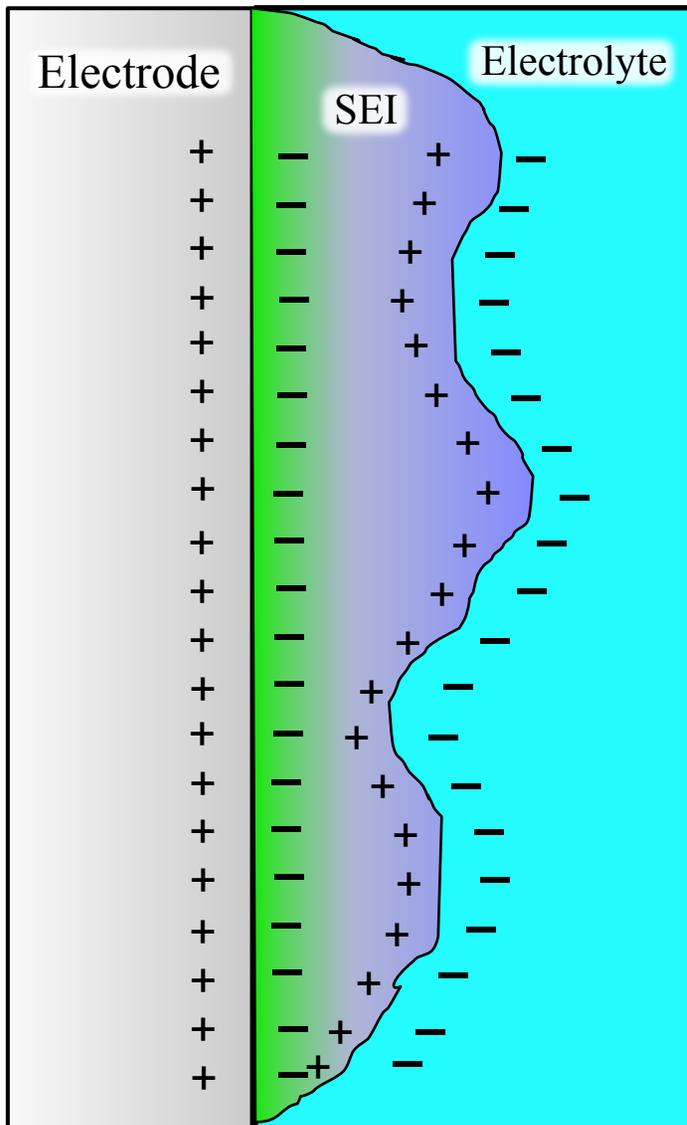
$$\dot{q}_{\text{SEI/W}} = k_{\text{fwd}} \prod_j a_j^{v_{j,\text{SEI/W},\text{fwd}}} - k_{\text{rev}} \prod_j a_j^{v_{j,\text{SEI/W},\text{rev}}}$$

SEI / Electrolyte

$$\dot{q}_{\text{SEI/elyte}} = k_{\text{fwd}} \prod_j a_j^{v_{j,\text{SEI/elyte},\text{fwd}}} - k_{\text{rev}} \prod_j a_j^{v_{j,\text{SEI/elyte},\text{rev}}}$$

Finite electronic conductivity.

Simulation Approach



Charge neutrality:

$$i_{\text{SEI,elyte}} = i_{\text{SEI,cond}} = i_{\text{SEI,W}}$$

$$i_{\text{SEI,elyte}} = \sum_{k,\text{SEI}} z_k F v_{k,\text{SEI/elyte}} \dot{q}_{\text{SEI/elyte}}$$

$$i_{\text{SEI,cond}} = \frac{R_{\text{SEI}}}{\Delta\phi_{\text{SEI}}}$$

$$i_{\text{SEI,W}} = - \sum_{k,\text{SEI}} z_k F v_{k,\text{SEI/W}} \dot{q}_{\text{SEI/W}}$$

$$\phi_{\text{W}} - \phi_{\text{SEI}} = \Delta\phi_{\text{W/SEI}} + \Delta\phi_{\text{SEI}} + \Delta\phi_{\text{SEI/elyte}}$$

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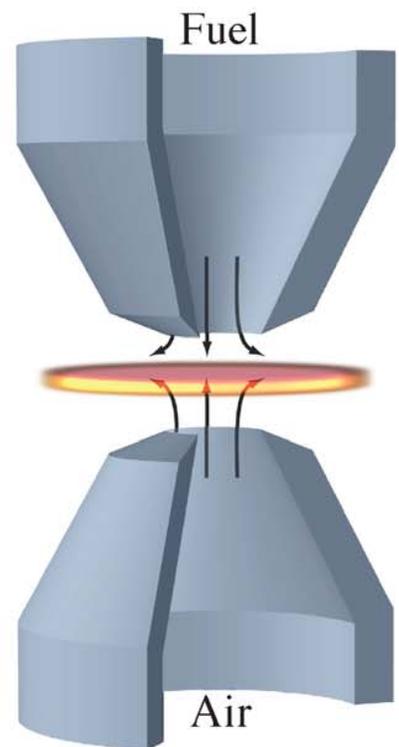
Cantera: Chemical Kinetics, Thermodynamics, Transport

Cantera input file (CTI)

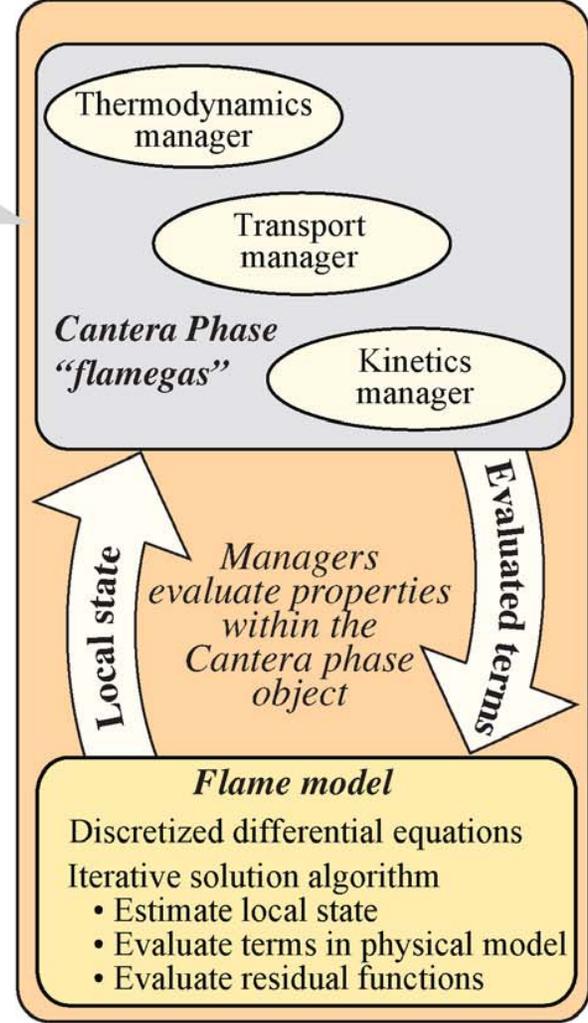
```

species(name = "H2",
  atoms = " H:2 ",
  thermo = (NASA( [200.00, 1000.00],
    [ 2.344E+00, ... , 6.83E-01] ), ... ),
  transport = gas_transport (
    geom = "linear",
    diam = 2.92,
    well_depth = 38.00 )
species (name="CO", .....
...
reaction( "O + H2 <=> H + OH",
  [3.87000E+04, 2.7, 6260]
three_body_reaction ( "2 O + M <=> O2 + M",
  [1.20000E+17, -1, 0],
  efficiencies = "H2:2.4 H2O:15.4 ")
reaction( "H + O2 <=> O + OH",
  [1.0E+14, 0.0, 7700]
...
ideal_gas (name = "flamegas",
  elements = "O H C N Ar",
  species = "" H2 H O O2 OH
    H2O HO2 H2O2 C ... """,
  transport = 'Mix',
  reactions = 'all' )
  
```

Import phase



Computational model



Cantera: Chemical Kinetics, Thermodynamics, Transport

Cantera input file (CTI)

```

Gas phase object:
  ideal_gas(name = 'fuelGas',
  ...)
Interface object:
  ideal_interface(name='Ni_surface',
  elements = "Ni H O C",
  species = """"Ni(s) H(s) ...""",
  phases = "fuelGas Ni_bulk",
  reactions = "all",
  site_density = 2.7e-9)
Reactions:
  surface_reaction("H2 + 2 Ni(s) <=> 2 H(s)",
  stick(0.8, 0, 0))
  surface_reaction("O2 + 2 Ni(s) <=> 2 O(s)",
  ...)
  
```

Import phases

Computational model

```

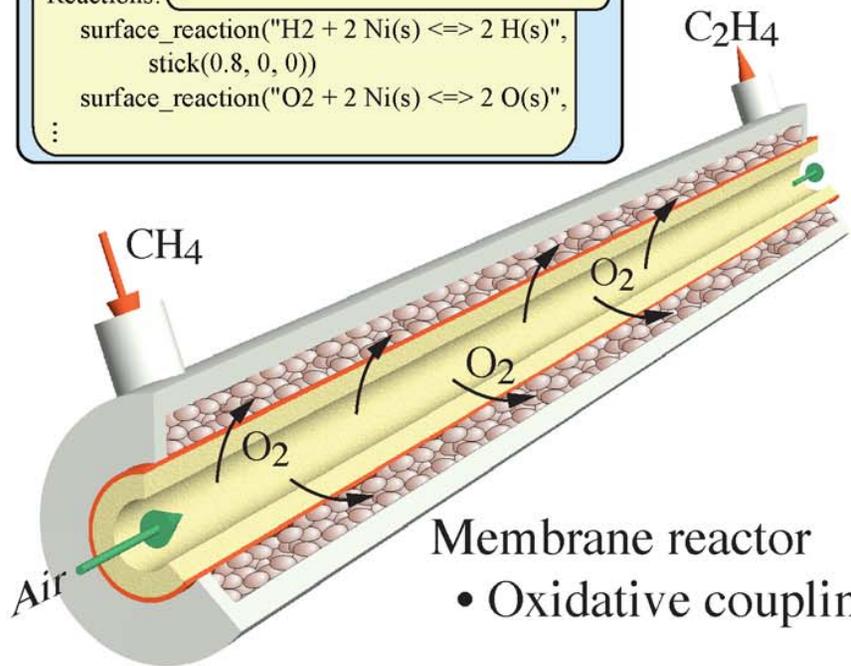
Initialize Cantera Objects:
  Import gas and surface phases:
  gas = importPhase ('OCMcat.cti', 'fuelGas');
  bulk = importPhase ('OCMcat.cti', 'Ni_bulk');
  surface = importInterface ('OCMcat.cti', 'Ni-surface', gas, bulk);

Solve Discretized ODEs:
  Set local states for gas and surface objects:
  set(gas, 'T', T_reactor, 'P', pressure, 'X', X_k)
  setCoverages (surface, Theta_k)
  setTemperature (surface, T_reactor)

  Evaluate residual functions:
  
$$\frac{d(\phi_g \rho Y_k)}{dt} = -\nabla \cdot (\rho Y_k \mathbf{v} - D_k W_k \nabla [X_k]) + W_k (\dot{\omega}_k + a_{\text{surf}} \dot{s}_k)$$


  Retrieve Diffusion Coefficients:
  D_k = mixDiffCoeffs(gas);

  Retrieve Reaction Rates:
  omega_gas = netProdRates(gas);
  sdot_surf = netProdRates(surface);
  
```



Membrane reactor

- Oxidative coupling of methane

Cantera website: cantera.org

**Repository on GitHub:
<https://github.com/cantera>**

**Users' Group:
<https://groups.google.com/forum/#!forum/cantera-users>**

**Demonstration:
https://github.com/decaluwe/ECS_2018_materials/blob/master/ECS_2018.ipynb**



On the Fundamental and Practical Aspects of Modeling Complex Electrochemical Kinetics and Transport

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Numerous technologies, such as batteries and fuel cells, depend on electrochemical kinetics. In some cases, the responsible electrochemistry and charged-species transport is complex. However, to date, there are essentially no general-purpose modeling capabilities that facilitate the incorporation of thermodynamic, kinetic, and transport complexities into the simulation of electrochemical processes. A vast majority of the modeling literature uses only a few (often only one) global charge-transfer reactions, with the rates expressed using Butler–Volmer approximations. The objective of the present paper is to identify common aspects of electrochemistry, seeking a foundational basis for designing and implementing software with general applicability across a wide range of materials sets and applications. The development of new technologies should be accelerated and improved by enabling the incorporation of electrochemical complexity (e.g., multi-step, elementary charge-transfer reactions and as well as supporting ionic and electronic transport) into the analysis and interpretation of scientific results. The spirit of the approach is analogous to the role that Chemkin has played in homogeneous chemistry modeling, especially combustion. The Cantera software, which already has some electrochemistry capabilities, forms the foundation for future capabilities expansion.

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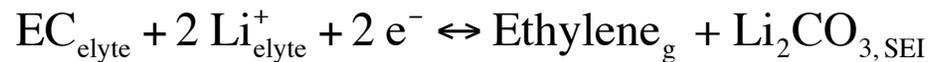
Manuscript submitted July 12, 2018; revised manuscript received August 30, 2018. Published September 15, 2018.

Outline

- Introduction: Current understanding of the SEI
- Chemical models of SEI growth
- Experimental data for validation
- Numerical Simulation of SEI Chemistry (1)
- Interlude: Cantera
- **Numerical Simulation of SEI Chemistry (2)**
- **Conclusions and Next Steps**

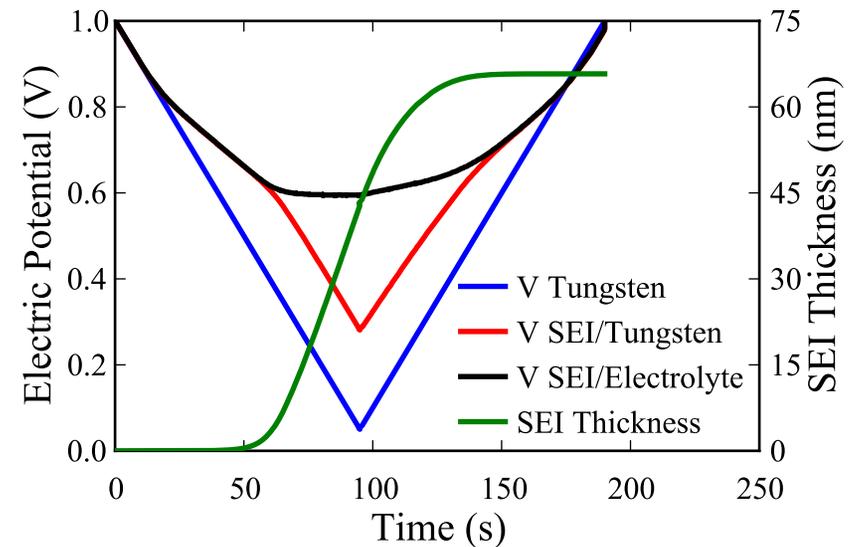
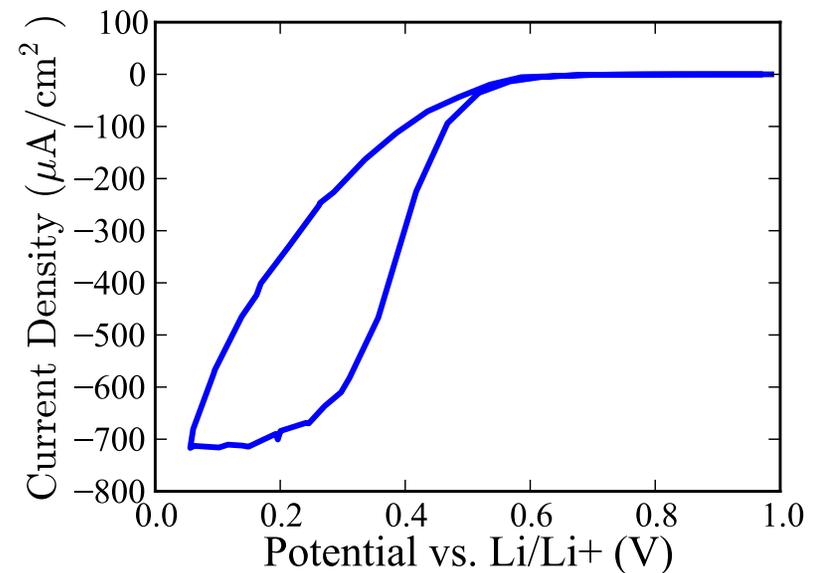
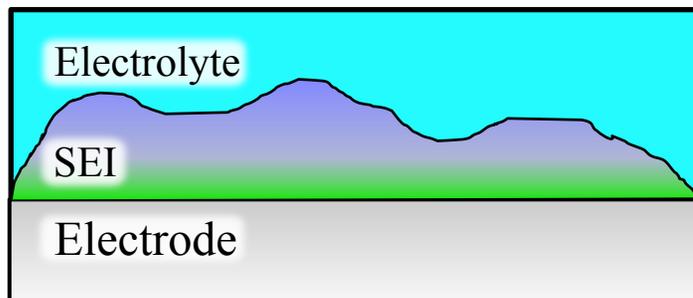
Preliminary Simulation Results

- **Simple SEI chemistry:**



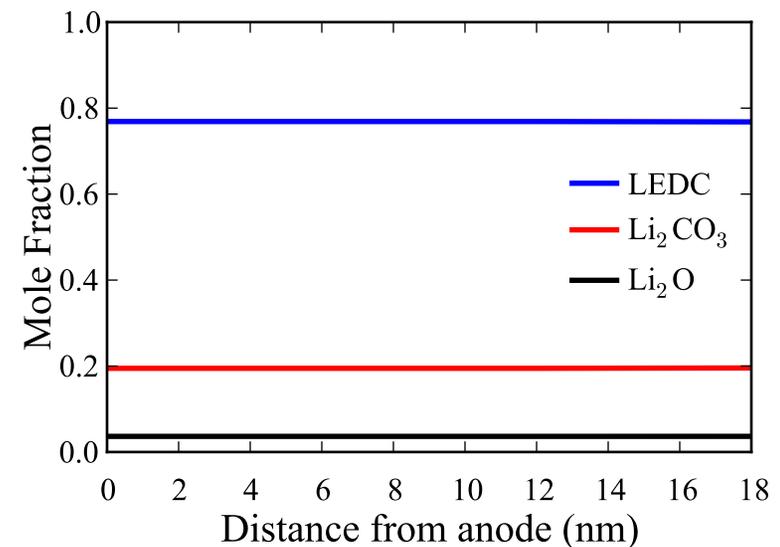
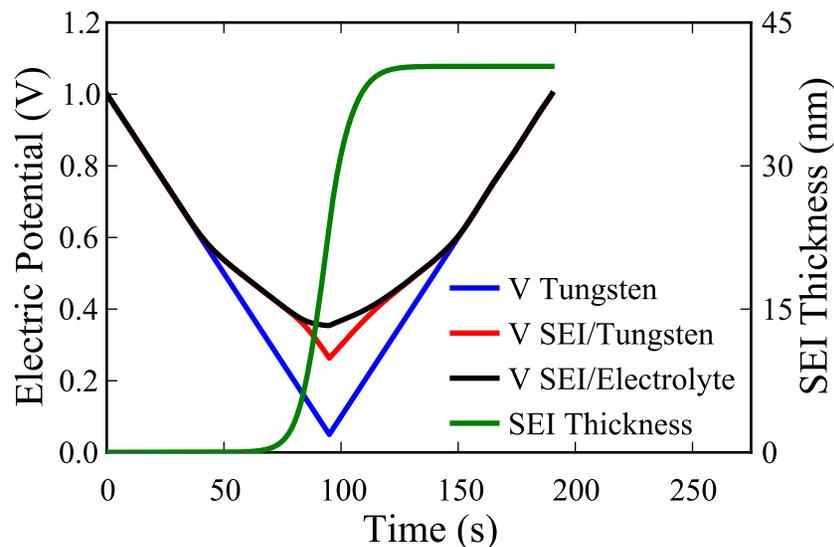
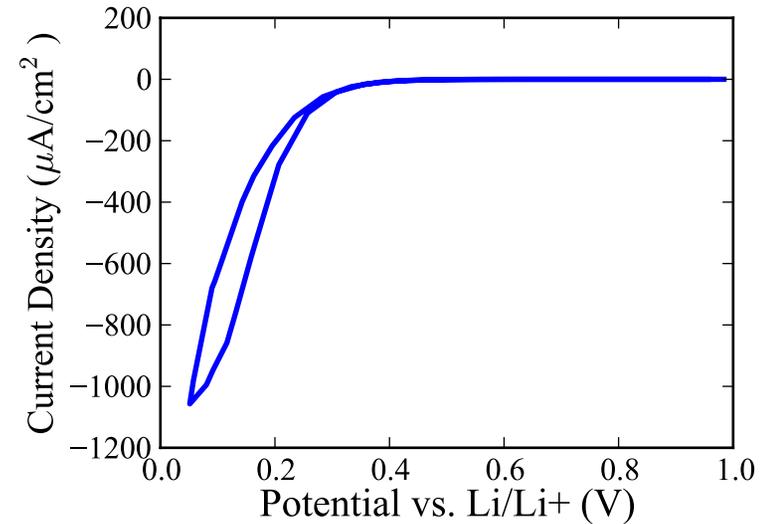
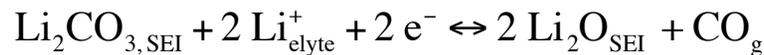
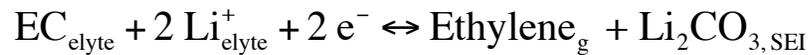
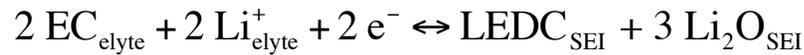
- **Charge transfer capacitance, (electro)chemical reaction rates, SEI resistance all are tunable parameters.**

- **Simulate a simple CV curve between 1.0 V and 0.05 V, at a scan rate of 10 mV/s.**



Preliminary Simulation Results

■ “Complex” SEI chemistry:



- More NR and EQCM-D
 - More realistic substrates (carbon)
 - Verify SEI mitigation / improvement strategies: additives, growth conditions.
- Additional physics for SEI growth model
 - Porosity and roughness
 - Discretized SEI electric potential
 - Local resistance function of composition
 - Ion transport in SEI – solid diffusion and diffusion in electrolyte-filled pores



Thank You.