



Universidad  
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Latin American Webinars on Physics

# Plaiting Dark Matter and neutrino phenomenologies

Roberto A. Lineros

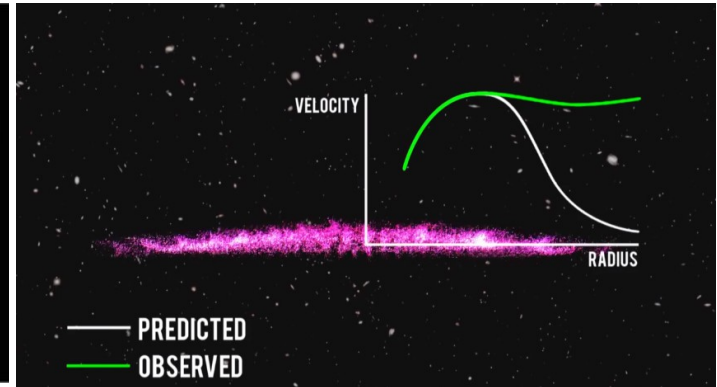
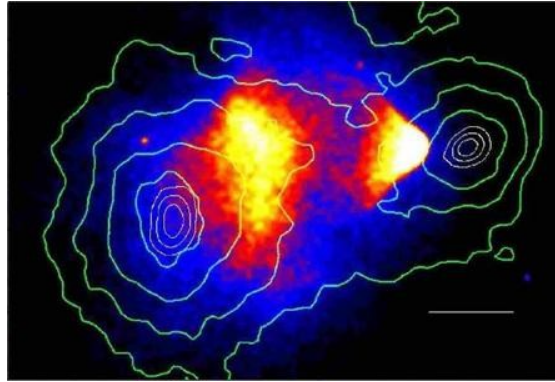
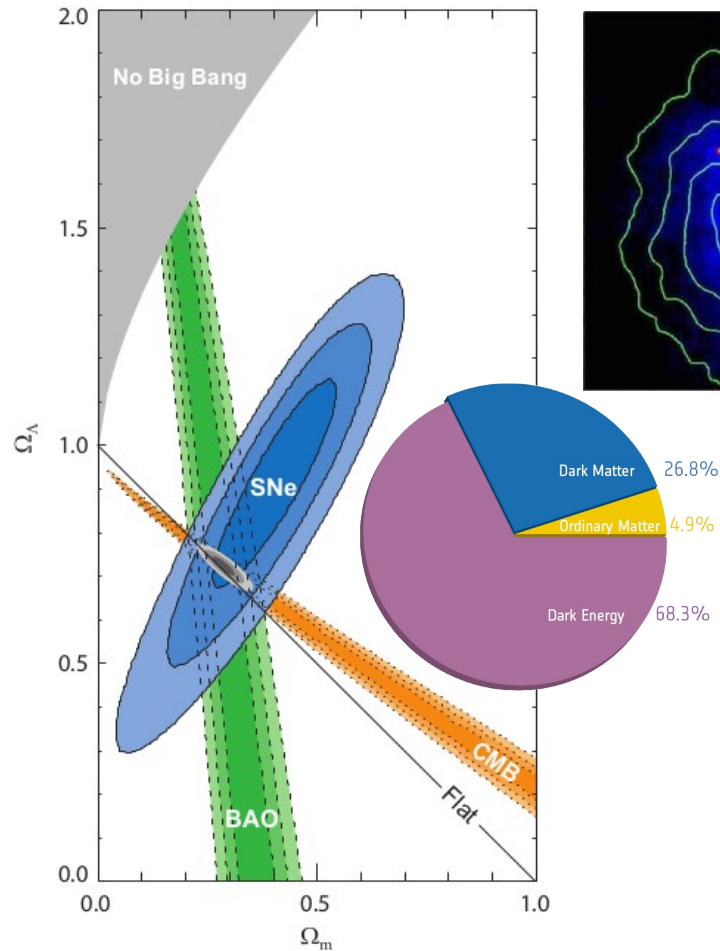
Departamento de Física, Universidad Católica del Norte

UTFSM San Joaquín – 13 September 2018

# Outline



# Dark Matter

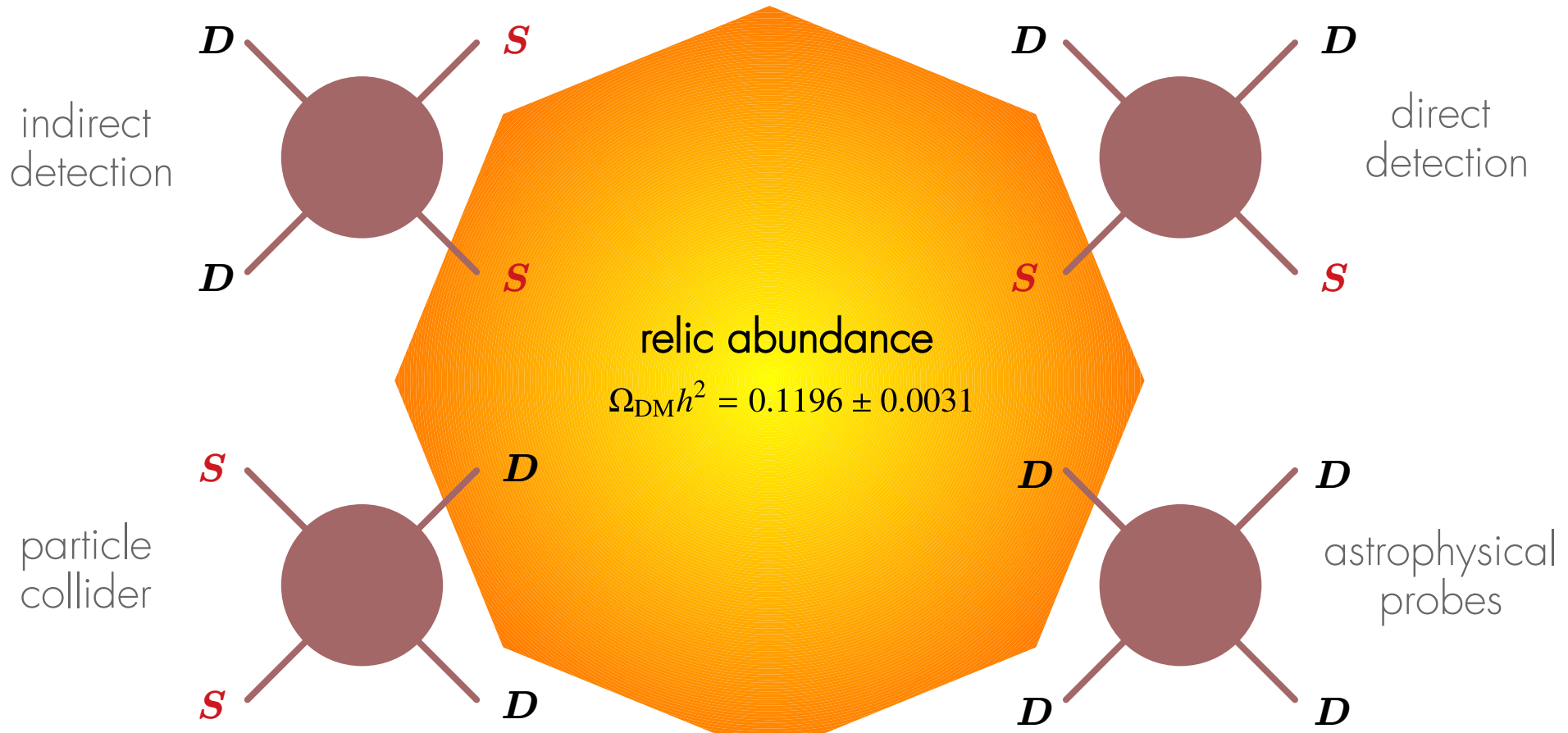


Observations support Dark Matter

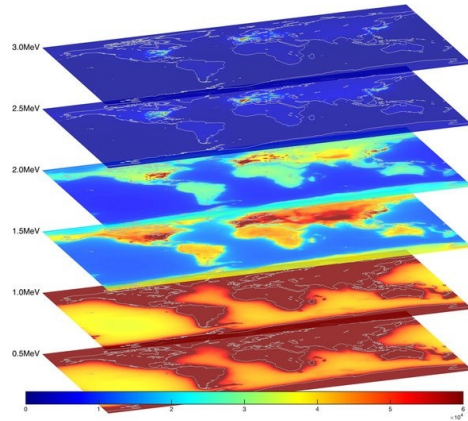
- Dynamics of clusters and galaxies
- Structure formation
- CMB anisotropies
- Baryon Acoustic Oscillation

$$\Omega_{\text{DM}} h^2 = 0.1196 \pm 0.0031$$

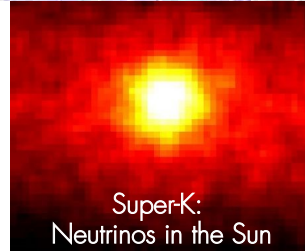
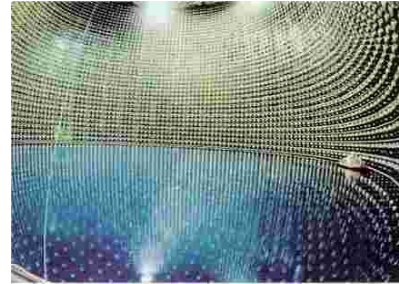
# Dark Matter Searches



# Neutrinos

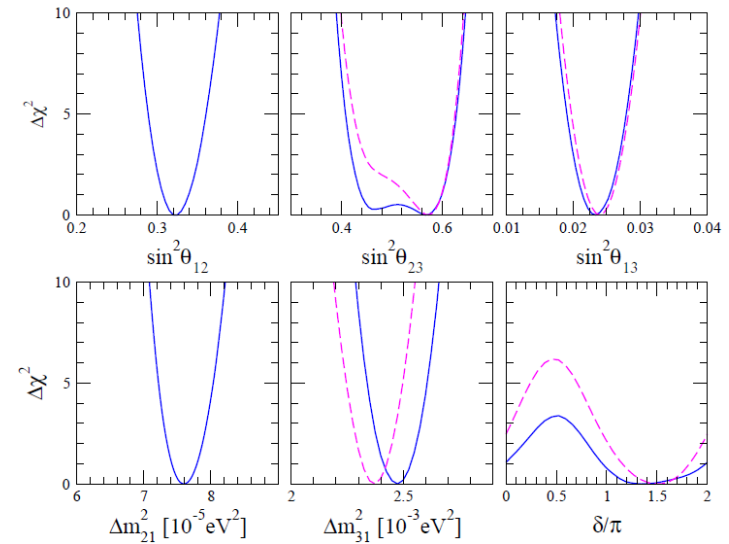


AGM2015: Antineutrino Global Map 2015



Super-K:  
Neutrinos in the Sun

Forero, Tortola and Valle PRD 90 (2014) 093006



The **SM** predicts zero neutrino mass

**Beyond SM** physics is required to explain  
mass spectrum and mixing angles

# Example 1

(light) Dark Matter candidate  
and neutrino masses

Majoron dark matter from a spontaneous inverse seesaw model.  
N. Rojas, R. A. Lineros, F. Gonzalez-Canales. [[arxiv:1703.03416](#)]

# Neutrino mass mechanisms

A large fraction of the models uses the 5-dim **Weinberg operator** to generate **majorana** neutrino masses

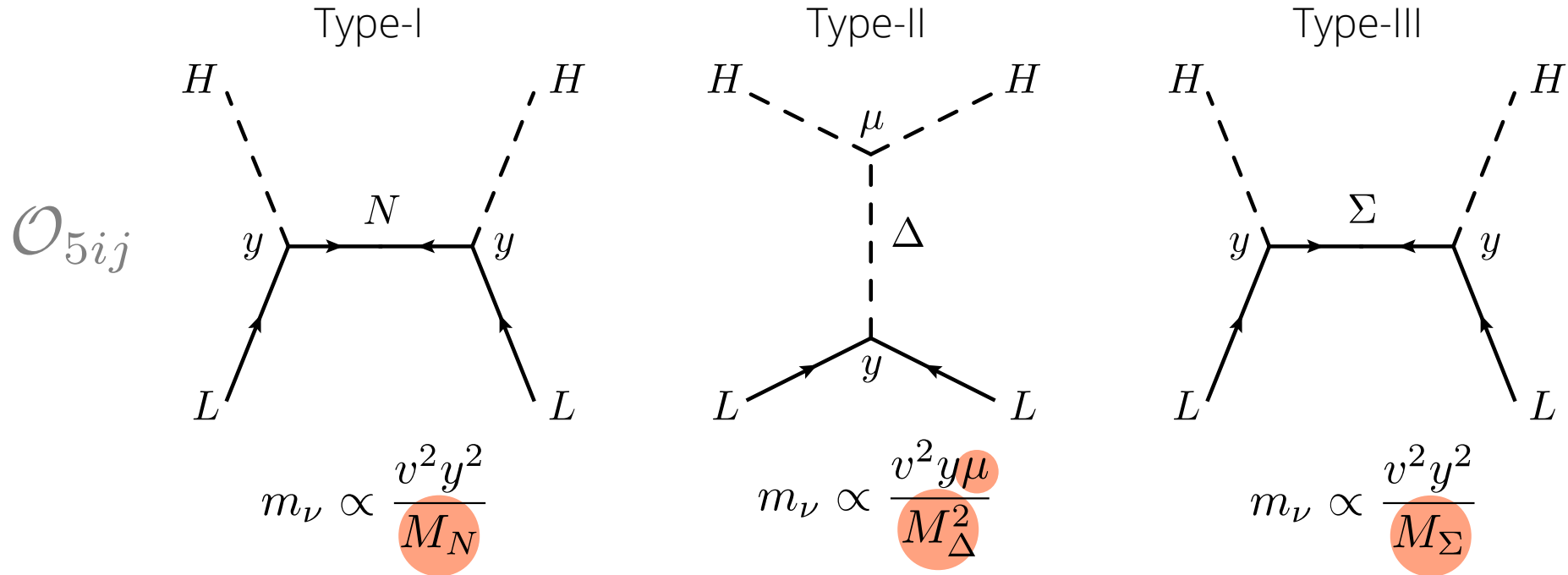
$$\mathcal{O}_{5ij} = \frac{1}{\Lambda} (L_i H)^T (L_j H)$$

This operator breaks lepton number in **2 units**

$$\mathcal{O}_{5ij} = \frac{v^2}{\Lambda} \nu_i \nu_j$$

# Neutrino mass mechanisms

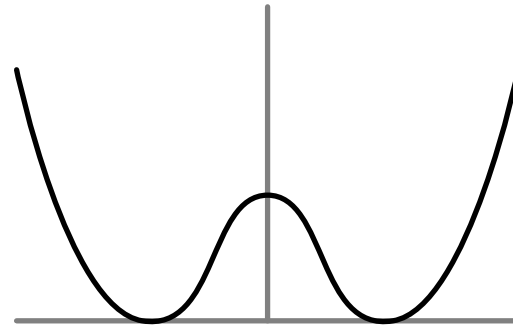
The commonly known schemes are **see-saw mechanisms**



# Enters the Majoron

The Type-I seesaw can be generated by the **spontaneous** breaking of the **U(1) lepton number** symmetry

$$S = \frac{v_S + \sigma + iJ}{\sqrt{2}}$$



$$\mathcal{L} \supset -y_L \bar{L} H N^c - \frac{y_S}{2} S \bar{N}^c N + h.c.$$

-1 0 1                      2 -1 -1

# Enters the Majoron

$$m_D = \frac{y_L v_H}{\sqrt{2}}$$

$$M_N = \frac{y_S v_S}{\sqrt{2}}$$

After the SSB, we get the Type-I seesaw

$$\mathcal{L} \supset -m_D \bar{\nu}_L N^c - \frac{M_N}{2} \overline{N^c} N + h.c.$$

and 2 scalars:  $\sigma$  and  $J$

$$m_\sigma \simeq v_S \quad m_J = 0$$

# Enters the Majoron

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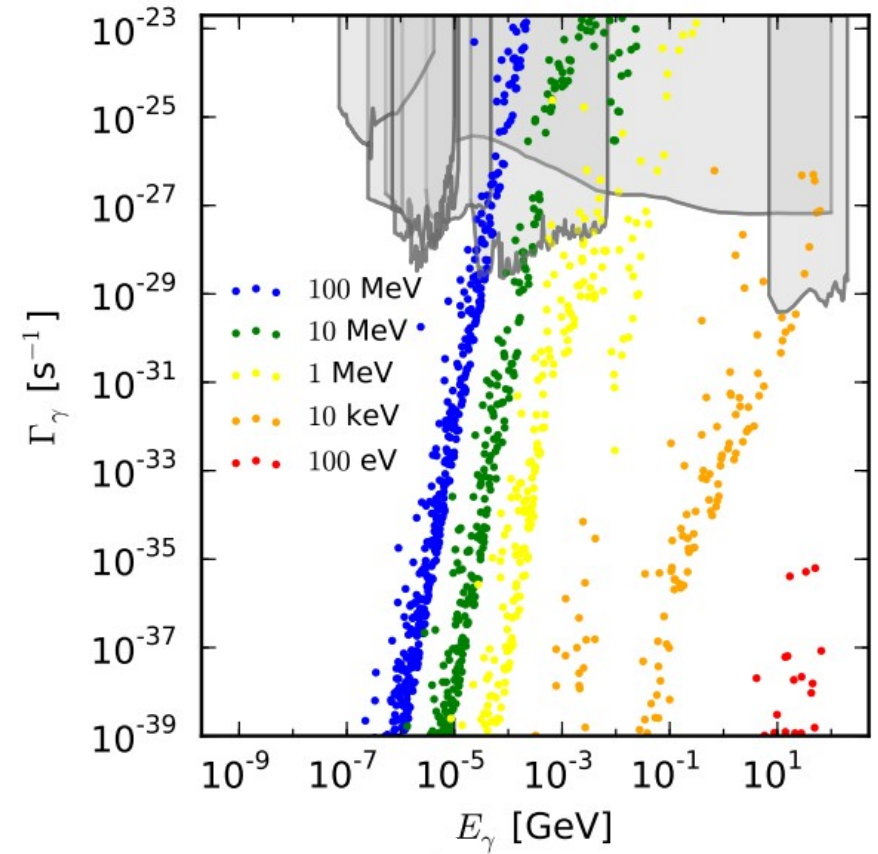
$$\mathcal{L} \supset -m_D \bar{\nu}_L N^c - \frac{M_N}{2} \overline{N^c} N + h.c.$$

and 2 scalars:  $\sigma$  and  $J$   DM candidate

$$m_\sigma \simeq v_S \quad m_J = 0$$

# Majoron as DM <sub>(pros)</sub>

- Neutral
- Weakly coupled to the SM
- Long lived



Details in arxiv: 1406.0004

$$\Gamma_{J \rightarrow \nu\nu} = \frac{m_J}{32\pi} \frac{\sum_i (m_i^\nu)^2}{2v_1^2} \quad \Gamma_{J \rightarrow \gamma\gamma} = \frac{\alpha^2 m_J^3}{64\pi^3} \left| \sum_f N_f Q_f^2 \frac{2v_3^2}{v_2^2 v_1} (-2T_3^f) \frac{m_J^2}{12m_f^2} \right|^2$$

# Majoron as DM <sub>(cons)</sub>

$$m_J = 0 \quad !!!!!$$

... but global symmetries are not protected under gravity effects

Therefore

$$m_J \neq 0$$

... and the majoron DM is just a **pseudo Nambu-Goldstone boson**

# Majoron as DM (our proposal)

ArXiv:1703.03416

What defines a **majoron DM**?

- It is a (pseudo)scalar
- It is part of the neutrino mass mechanism
- Its signature is the decay into neutrinos
- It is massive

# Inverse seesaw

The **standard** inverse seesaw

$$\mu \ll m_D \ll M$$

$$\mathcal{L} = -\frac{1}{2}n_L^T C \mathcal{M} n_L + h.c.$$

$$n_L^T = (\nu_L, N_1^c, N_2)$$

$$\mathcal{M} = \begin{pmatrix} 0 & m_D & 0 \\ m_D^T & 0 & M \\ 0 & M^T & \mu \end{pmatrix}$$

# Inverse seesaw

The **standard** inverse seesaw

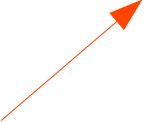
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$$\mu \ll m_D \ll M$$

$$\mathcal{M} = \begin{pmatrix} 0 & m_D & 0 \\ m_D^T & 0 & M \\ 0 & M^T & \mu \end{pmatrix}$$

Lepton number  
violating term



# Inverse seesaw

The **standard** inverse seesaw

$$\mu \ll m_D \ll M$$

Active neutrinos

$$m_\nu = \left( \frac{m_D}{M} \right)^2 \mu$$

Heavy neutrinos

$$m_{\mathcal{N}'} = M - \frac{m_D^2}{M} + \frac{\mu}{2}$$
$$m_{\mathcal{N}} = M - \frac{m_D^2}{M} - \frac{\mu}{2}$$

# Inverse seesaw

The usual inverse seesaw hierarchy:

$$\mu \ll m_D \ll M$$

Some numerology:

$$M \sim 100 \text{ TeV} \quad m_D \sim 10 \text{ GeV} \quad \mu \sim 10 \text{ MeV}$$

$$m_\nu \sim 0.1 \text{ eV}$$

$$\alpha = \frac{\mu}{M} \sim 10^{-7}$$

# Spontaneous Inverse seesaw

To generate the **inverse seesaw** scheme we need **2 complex scalars**

$$\mathcal{L} = -y_L \bar{L} H N_1^c - y_S S^\dagger \bar{N}_2 N_1^c - \frac{y_X}{2} X^\dagger \bar{N}_2^c N_2 + h.c.$$

$$m_D = \frac{y_L v_h}{\sqrt{2}}, \quad M = \frac{y_S v_S}{\sqrt{2}}, \quad \text{and} \quad \mu = \frac{y_X v_X}{\sqrt{2}}$$

# Spontaneous Inverse seesaw

To generate the **inverse seesaw** scheme we need **2 complex scalars**

$$\mathcal{L} = -y_L \bar{L} H N_1^c - y_S S^\dagger \bar{N}_2 N_1^c - \frac{y_X}{2} X^\dagger \bar{N}_2^c N_2 + h.c.$$

$$v_S > 50 \text{ TeV} \quad v_X > 5 \text{ MeV}$$

# Spontaneous Inverse seesaw

But the **charge assignments** do not follow the typical one of the ISS

|           | $L$ | $N_1$ | $N_2$ | $S$     | $X$  |
|-----------|-----|-------|-------|---------|------|
| $SU(2)_L$ | 2   | 1     | 1     | 1       | 1    |
| $U(1)_Y$  | 1/2 | 0     | 0     | 0       | 0    |
| $U(1)_I$  | 1   | -1    | $x$   | $1 - x$ | $2x$ |

$$x = 3/5$$

$$\mathcal{L} = -y_L \bar{L} H N_1^c - y_S S^\dagger \bar{N}_2 N_1^c - \frac{y_X}{2} X^\dagger \bar{N}_2^c N_2 + h.c.$$

# Scalar potential

The **assignment** fixes the potential

$$\omega = \frac{v_X}{v_S}$$

$$V_{\text{scalar}} = V_{XS} + V_{HXS} + V_I$$

$$V_I = \lambda_{\text{cp}} e^{i\delta} X S^{\dagger 3} + h.c.$$

$$S = \frac{v_S e^{i\theta} + \sigma_S + i\chi_S}{\sqrt{2}}$$

$$X = \frac{v_X e^{i\tau} + \sigma_X + i\chi_X}{\sqrt{2}}$$

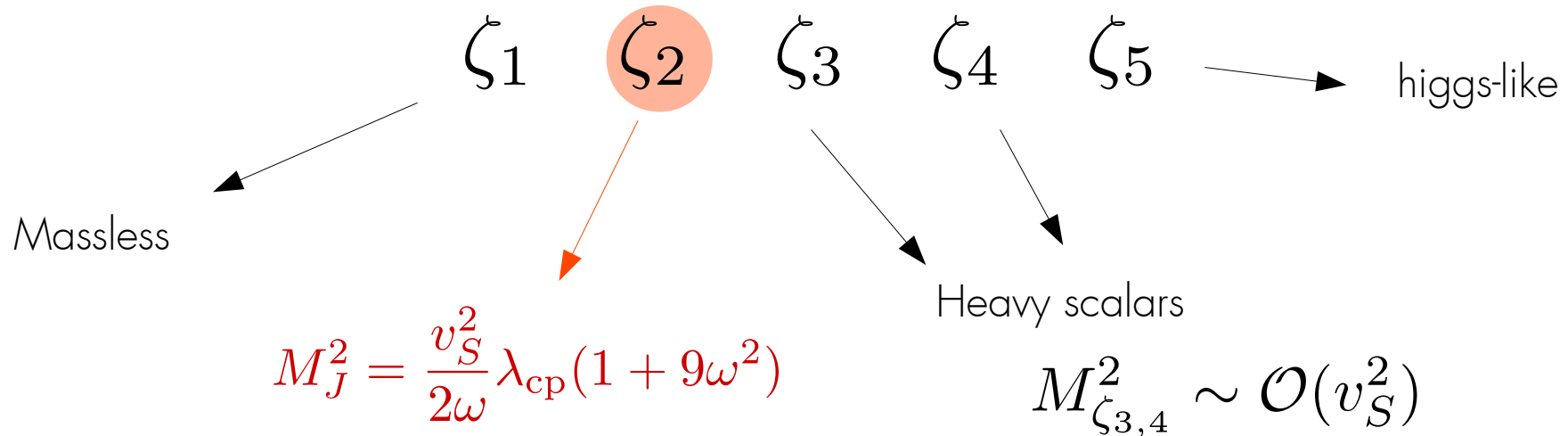
The tadpole equations relate the CP phases:

$$\tau = 3\theta - \delta - \pi$$

# Mass spectrum

$$\omega = \frac{v_X}{v_S}$$

Now we have 5 spin-0 fields: 4 related to L breaking  
1 related to EW breaking



# Majoron DM stability

The only candidate is the *lightest massive scalar* i.e.

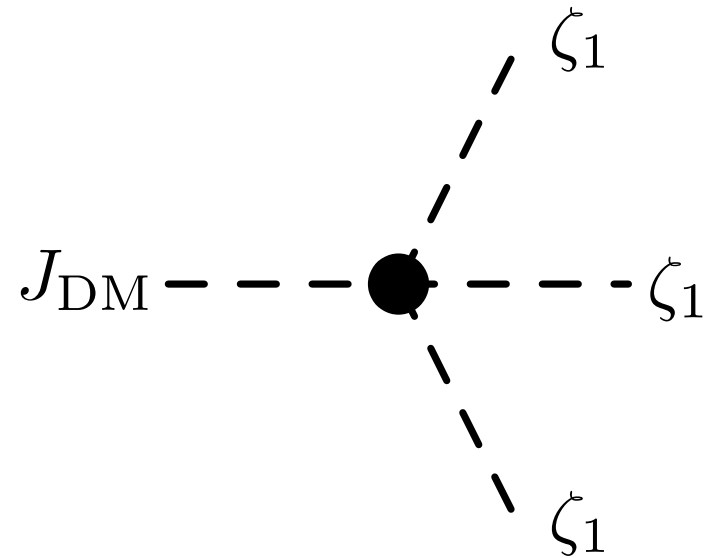
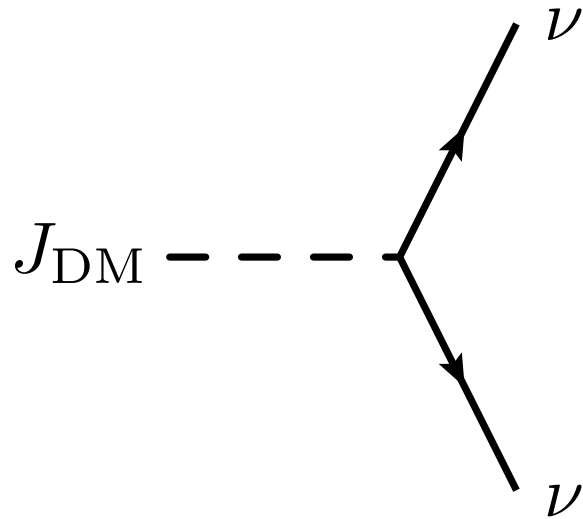
$$\zeta_2 = J_{\text{DM}}$$

We still has to satisfy the stability condition:

$$\Gamma_{\text{DM}} < 10^{-52} \text{ GeV}$$

# Decay modes

There are potentially dangerous decay modes:



# Decay into neutrinos

$$\alpha = \frac{\mu}{M} \sim 10^{-7}$$

The decay rate vanishes for:

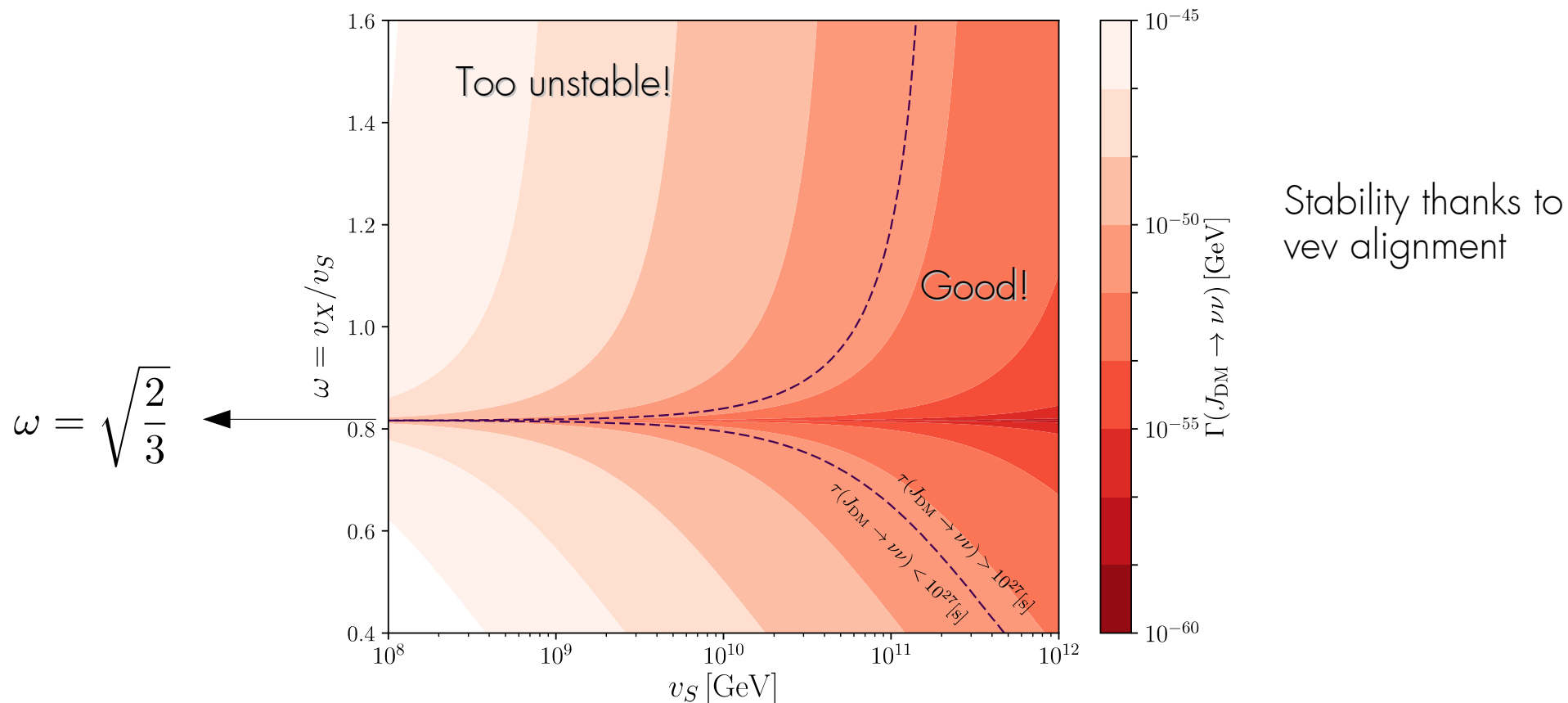
$$\omega_0 = \sqrt{2/3}$$

$$\Gamma_\nu = \Gamma_{0\nu}(\omega_0) 4\alpha^2$$

$$\Gamma_{0\nu}(\omega_0) \simeq 10^{-40} \text{ GeV} \left( \frac{m_\nu}{0.1 \text{ eV}} \right)^2 \left( \frac{M_J}{1 \text{ keV}} \right) \left( \frac{v_S}{100 \text{ TeV}} \right)^{-2}$$

# Decay into neutrinos

$$J_{\text{DM}} \rightarrow \nu\nu$$



# Decay into scalars

$$J_{\text{DM}} \rightarrow \zeta'_{\text{S}}$$

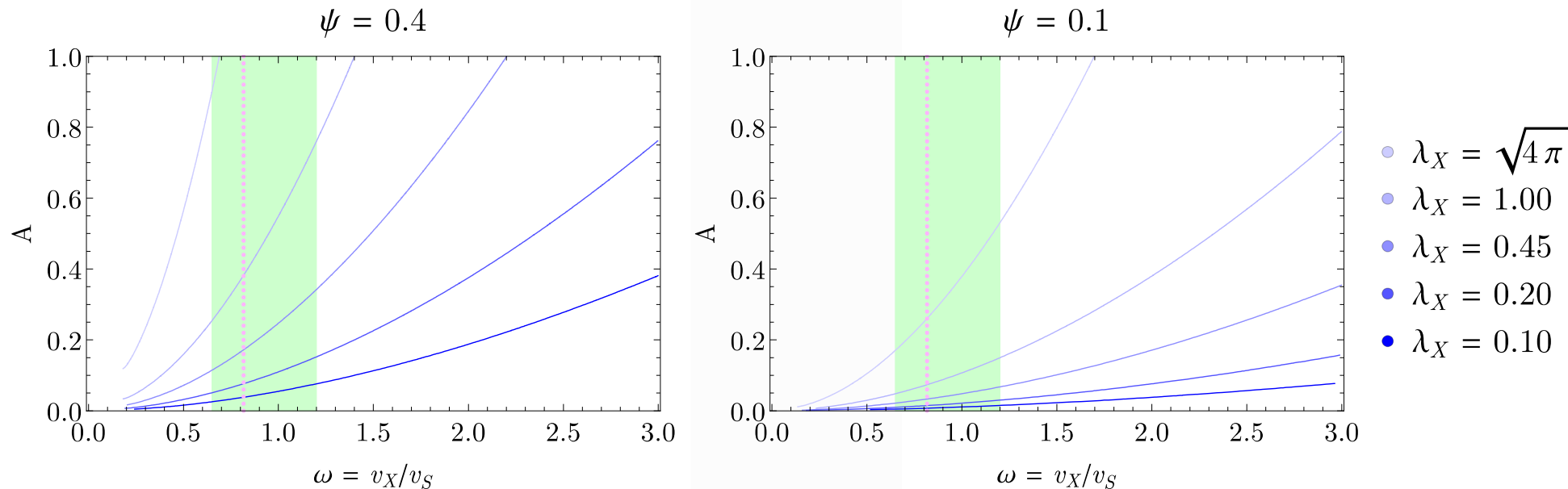
Without a protective symmetry, this channel is not suppressed

However we can find the parameter space where the **mode vanishes**

$$J_{\text{DM}} \text{---} \lambda_{2111}^{\text{eff}} \begin{array}{c} \nearrow \zeta_1 \\ \text{---} \zeta_1 \\ \searrow \zeta_1 \end{array} = J_{\text{DM}} \text{---} \lambda_{2111} \begin{array}{c} \nearrow \zeta_1 \\ \text{---} \zeta_1 \\ \searrow \zeta_1 \end{array} + \sum_{k=3,4,5} J_{\text{DM}} \text{---} \lambda_{12k} \begin{array}{c} \nearrow \zeta_1 \\ \text{---} \zeta_k \\ \searrow \lambda_{11k} \begin{array}{c} \nearrow \zeta_1 \\ \searrow \zeta_1 \end{array} \end{array}$$

# Decay into scalars

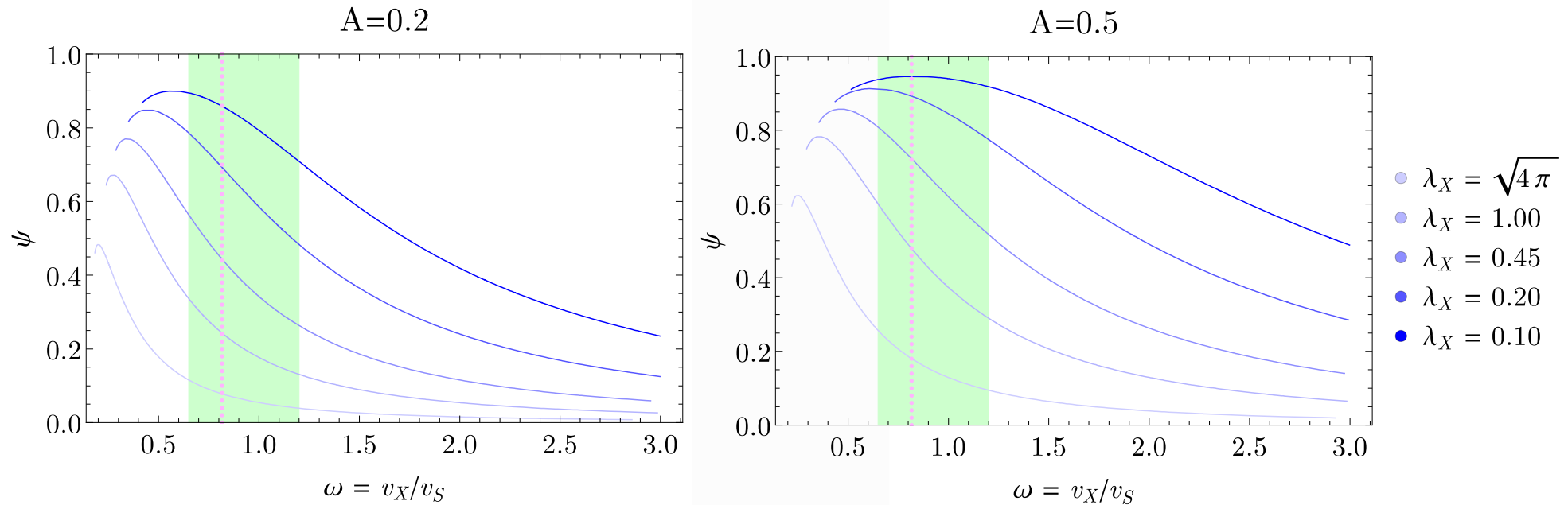
$$J_{\text{DM}} \rightarrow \zeta' \text{'s}$$



The interplay of different diagrams allows to vanish the decay mode

# Decay into scalars

$$J_{\text{DM}} \rightarrow \zeta' \text{'s}$$



There is a whole volume that satisfy this condition

# Conclusions (of this part)

- The **spontaneous inverse seesaw** provides a well suited majoron DM candidate
- Our **majoron DM** is phenomenologically equivalent to the PNGB
- The **vev alignment** has a relevant role in the DM stability

# Example 2

## Dark Matter interaction with neutrinos

Neutrino propagation in the galactic dark matter halo.  
P.F. de Salas, R.A. Lineros, M. Tórtola. [[arxiv:1601.05798](#)]

# Neutrino oscillations

Flavor and mass eigenstates **do not coincide**  $|\nu_\alpha\rangle = \sum_k U_{\alpha k}^* |\nu_k\rangle$

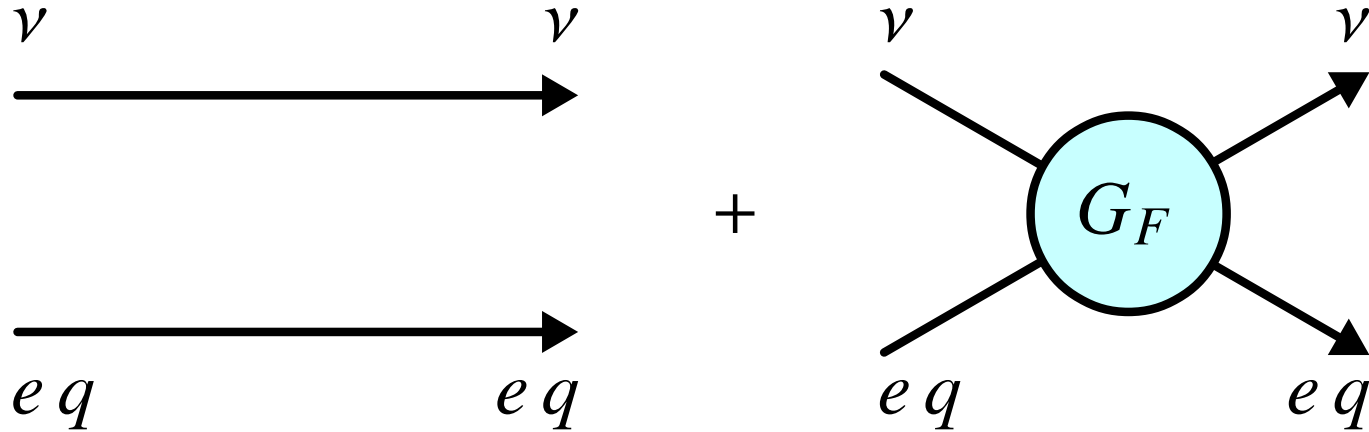
Mass eigenstates  
**evolve** according to:

$$\left| \begin{aligned} i \frac{\partial \Psi}{\partial t} &= \mathcal{H} \Psi \\ \mathcal{H}_{\text{vac}} &= \frac{1}{2E} U \begin{pmatrix} 0 & 0 & 0 \\ 0 & \Delta m_{21}^2 & 0 \\ 0 & 0 & \Delta m_{31}^2 \end{pmatrix} U^\dagger \end{aligned} \right.$$

The final  $\nu$  flavor depends on: **Initial state, Source distance, Neutrino energy**

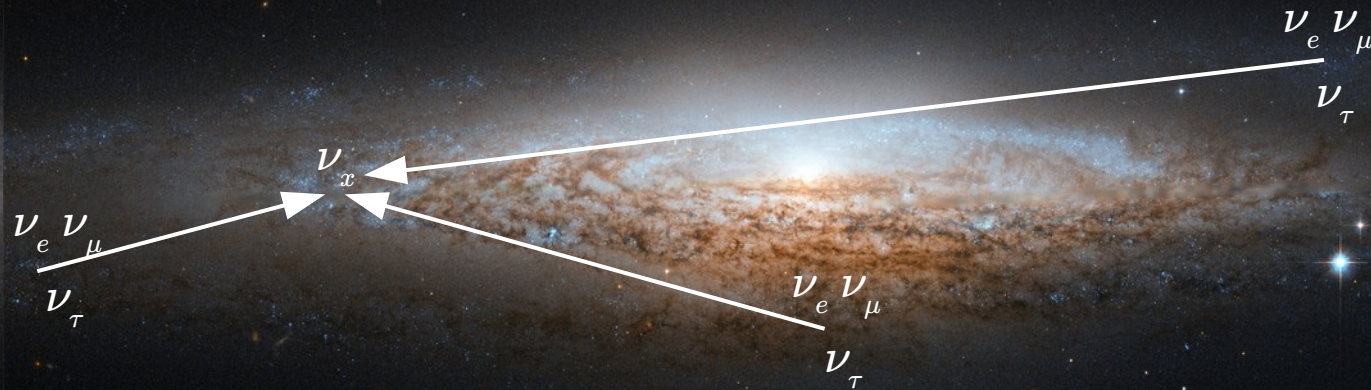
# Matter effects (a.k.a. MSW effect)

The interaction with a medium modifies the oscillation patterns w.r.t. vacuum



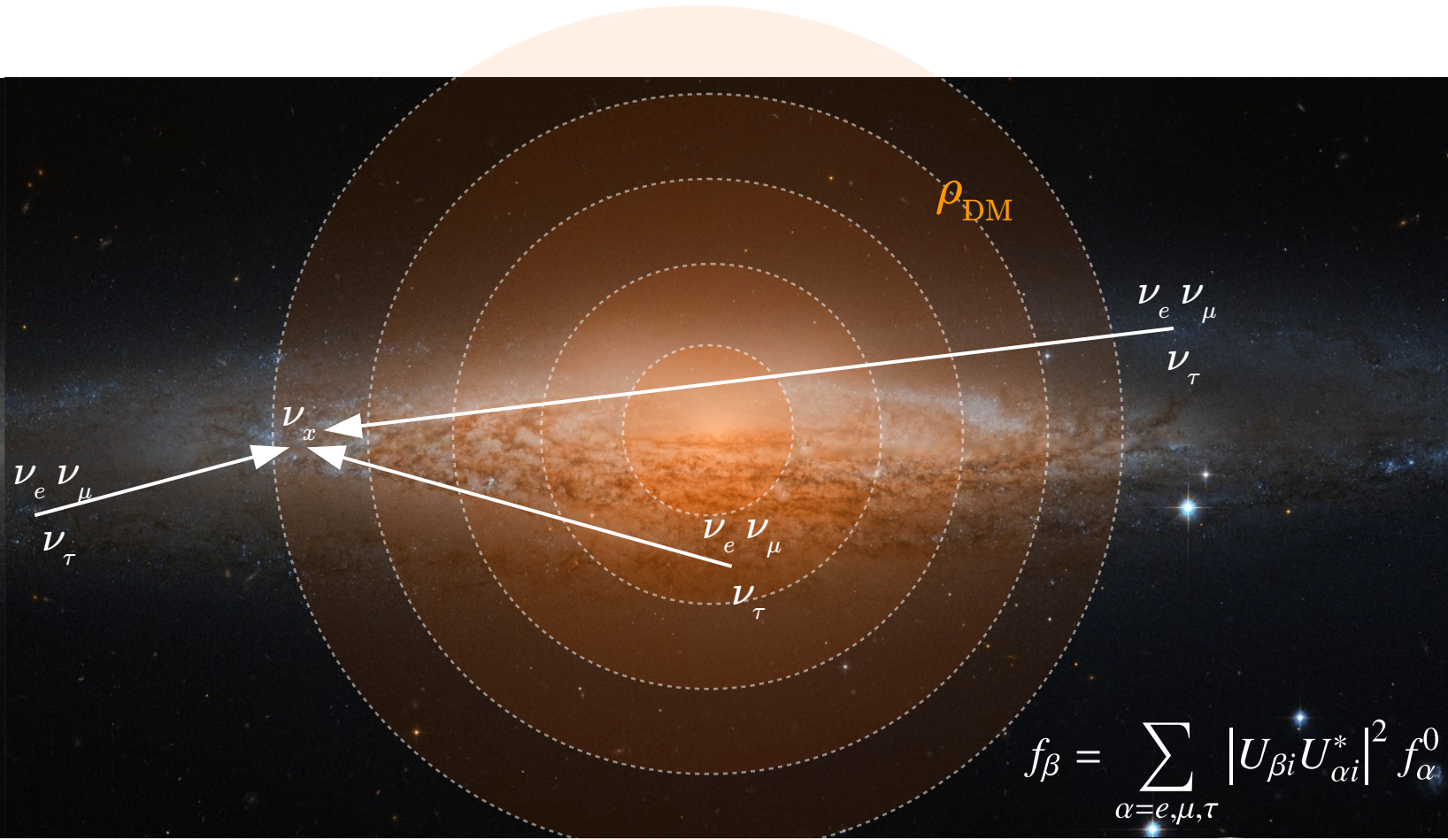
$$\mathcal{H}_{\text{tot}} = \mathcal{H}_{\text{vac}} + \mathcal{V}$$

# Dark Matter effects

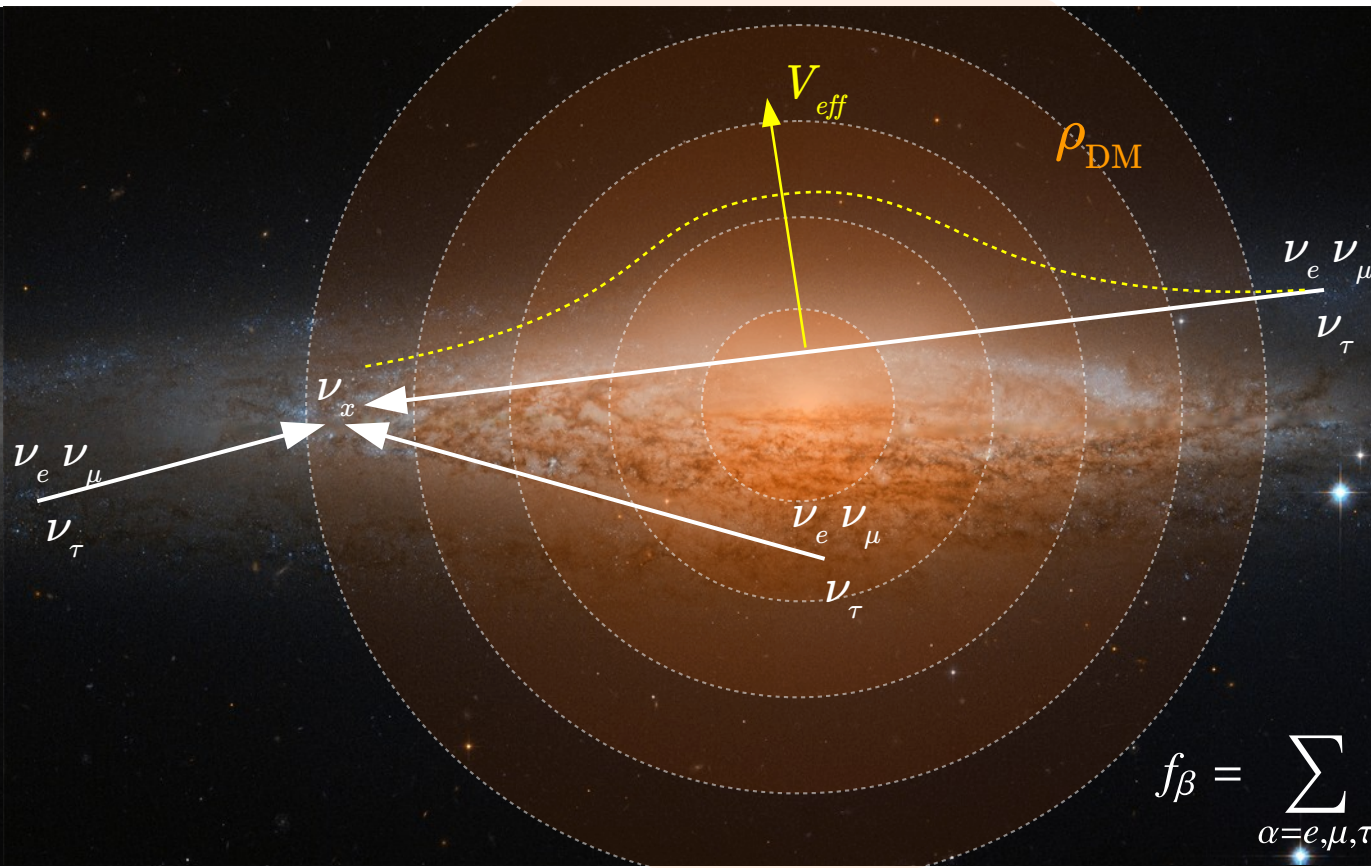


$$f_\beta = \sum_{\alpha=e,\mu,\tau} |U_{\beta i} U_{\alpha i}^*|^2 f_\alpha^0$$

# Dark Matter effects



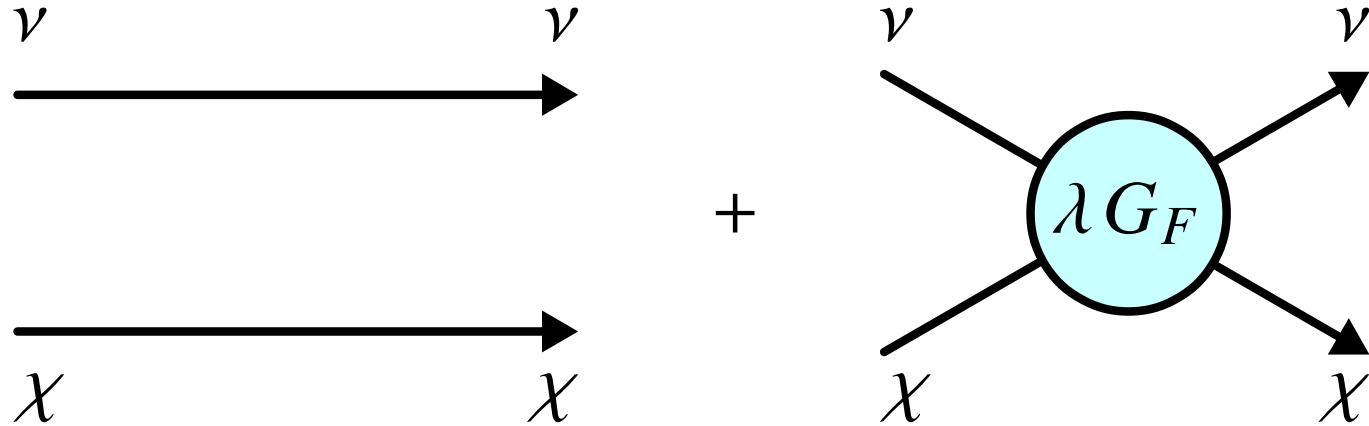
# Dark Matter effects



$$f_\beta = \sum_{\alpha=e,\mu,\tau} |U_{\beta i} U_{\alpha i}^*|^2 f_\alpha^0$$

# Dark Matter effects

The interaction with DM might modify the oscillation patterns w.r.t. vacuum



$$\mathcal{H}_{\text{tot}} = \mathcal{H}_{\text{vac}} + \mathcal{V}$$

# Dark Matter effects

We parameterized the effective potential using a “weak interaction” form:

$$\mathcal{V}_{\alpha\beta} = \lambda_{\alpha\beta} G_F N_\chi(\vec{x})$$

But also spatial dependency:

$$\mathcal{V}_{\alpha\beta} = \mathcal{V}_{\alpha\beta}^\oplus \times f(\vec{x})$$

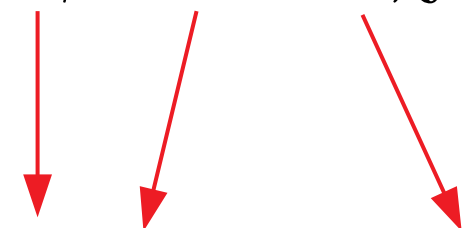
$$N_\chi(\vec{x}) = \frac{\rho_\chi(\vec{x})}{m_\chi}$$

# Dark Matter effects

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$$\mathcal{V}_{\alpha\beta} = \lambda_{\alpha\beta} G_F N_{\chi}(\vec{x})$$

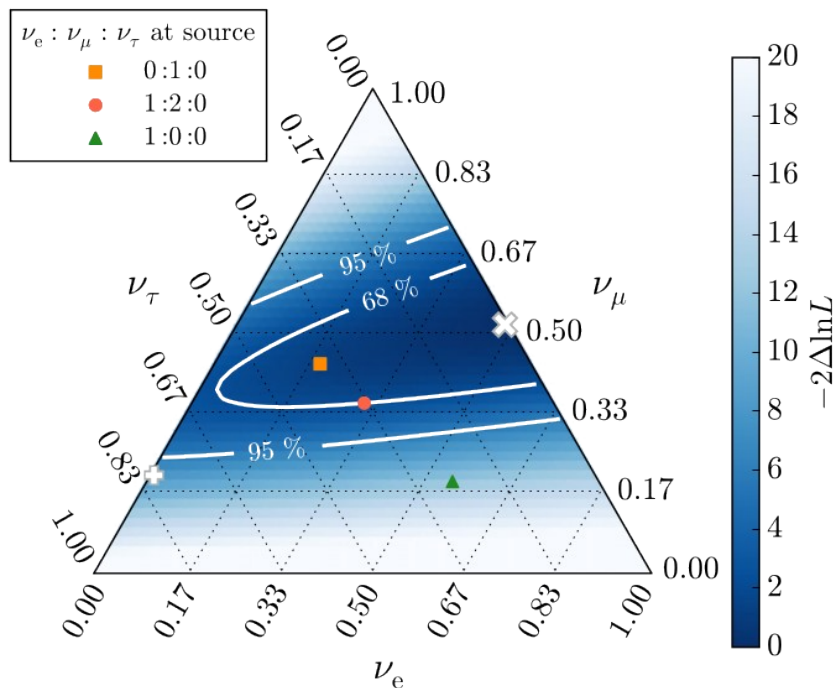
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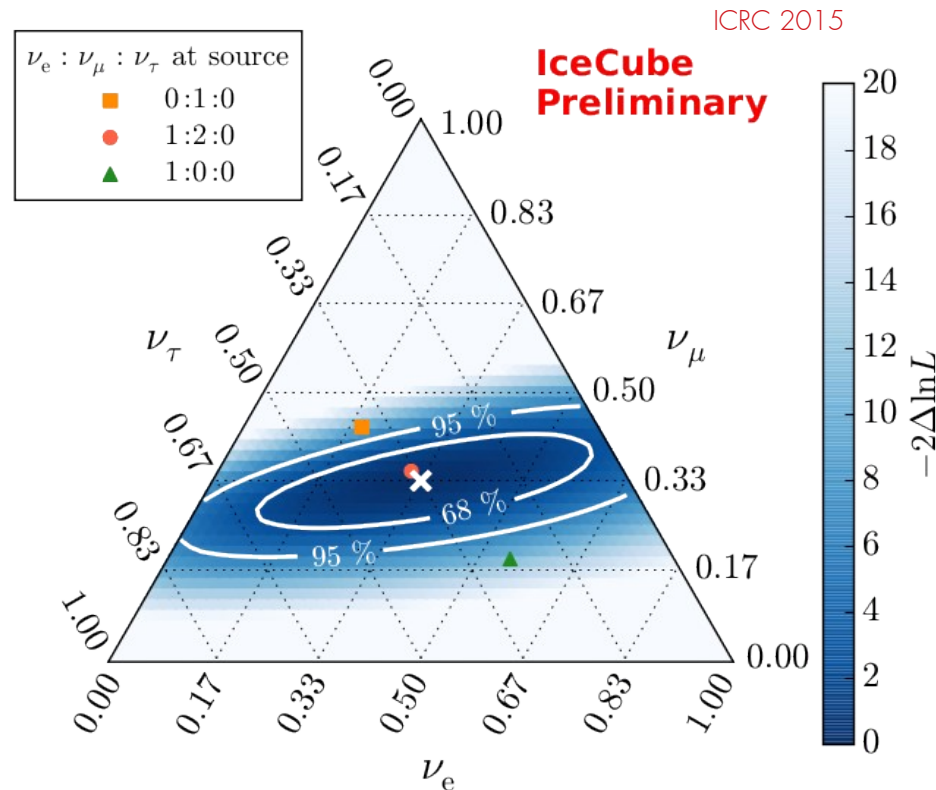
$$N_{\chi}(\vec{x}) = \frac{\rho_{\chi}(\vec{x})}{m_{\chi}}$$

# Flavor composition in IceCube

THE ASTROPHYSICAL JOURNAL, 809:98 (15pp), 2015 August 10



Latest result on flavor composition

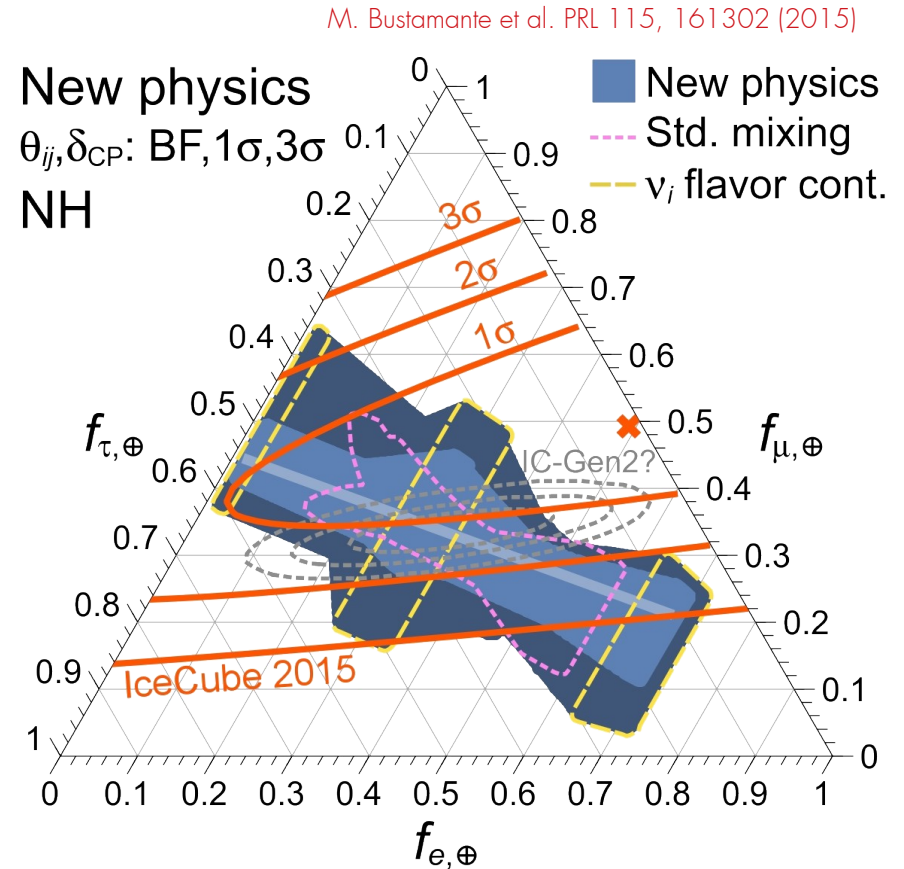
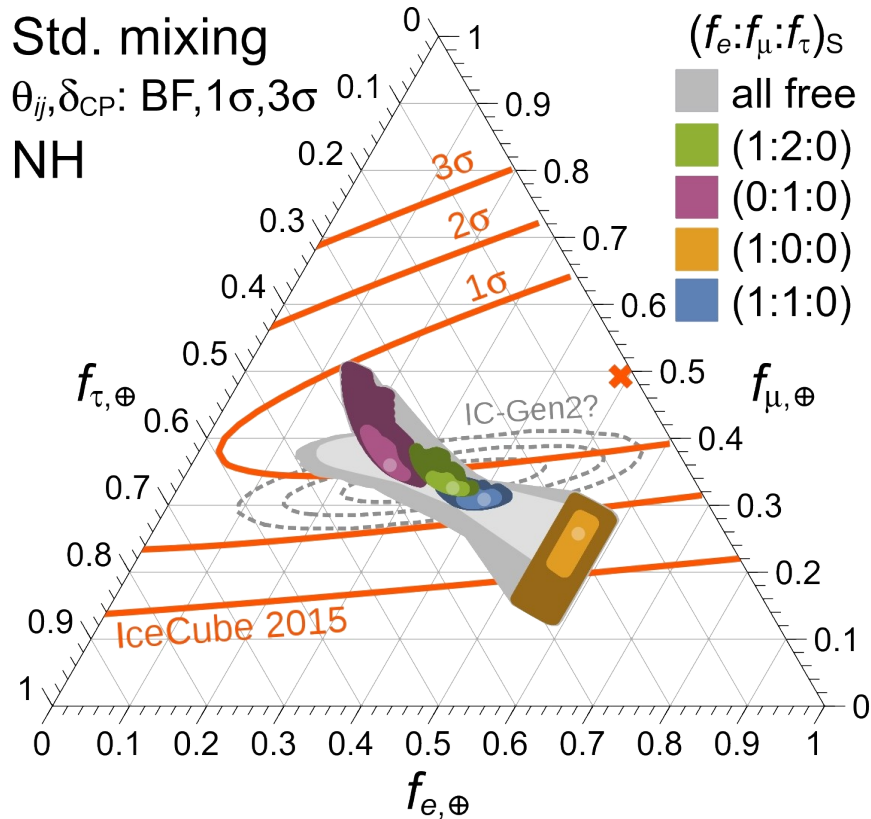


Sensitivity after 10 years

ICRC 2015

**IceCube Preliminary**

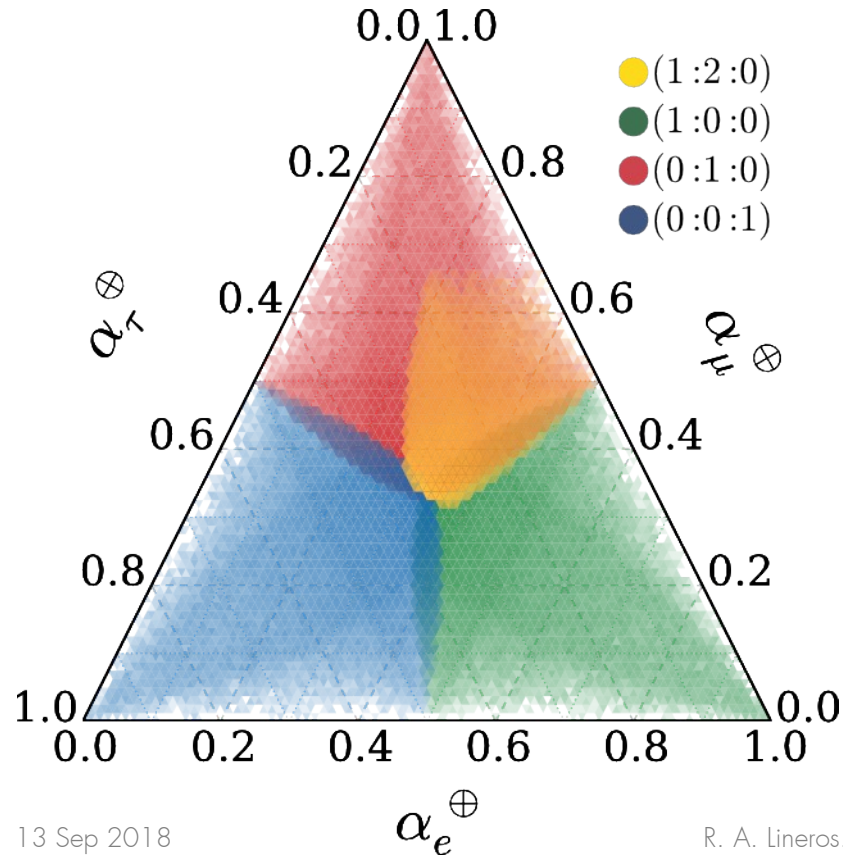
# What we expect?



M. Bustamante et al. PRL 115, 161302 (2015)

# Effects from New Physics

Argüelles et al. PRL 115, 161303 (2015)

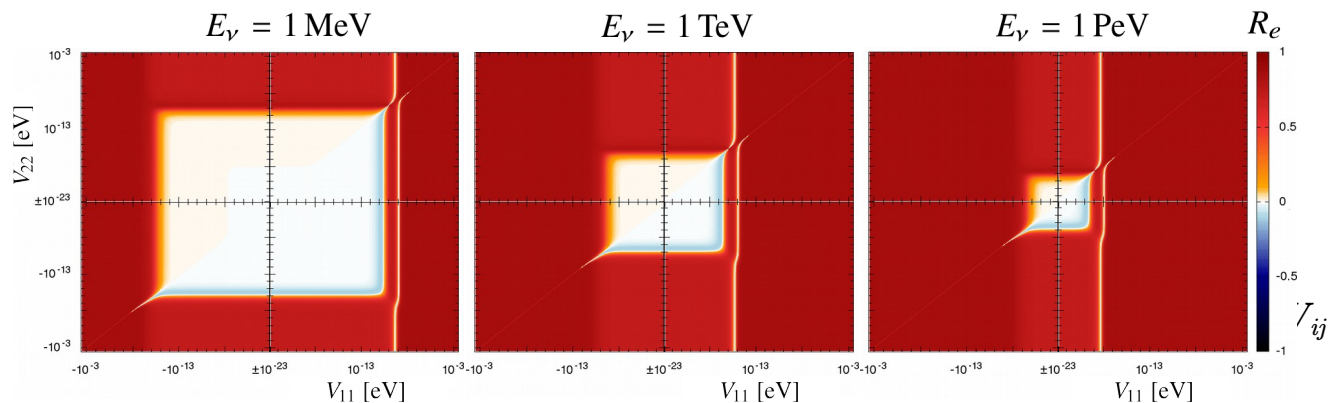


Sources of New Physics:

- Space torsion
- CPT - Lorentz violation

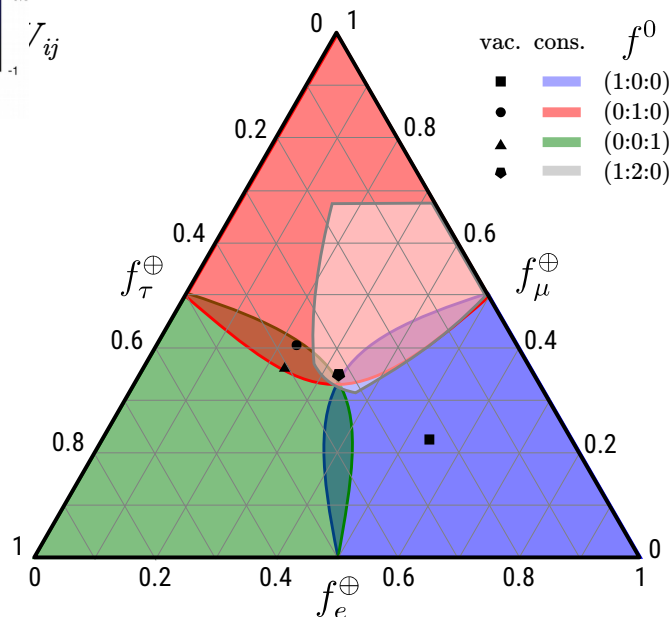
All NP effects are **homogeneous** in space

# Composition in a homogeneous halo



Homogeneous DM distribution can mimic  
New Physics effects

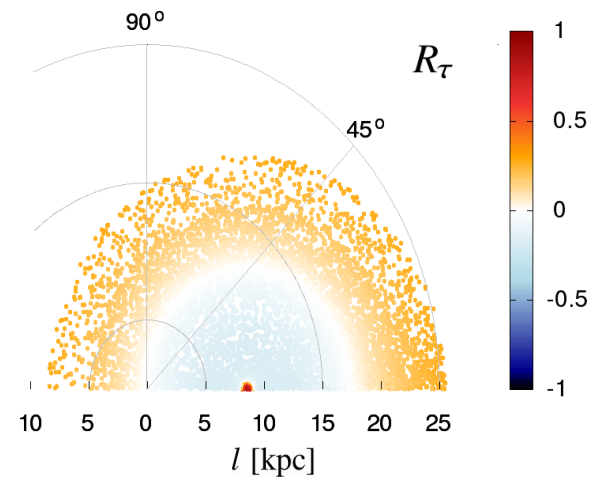
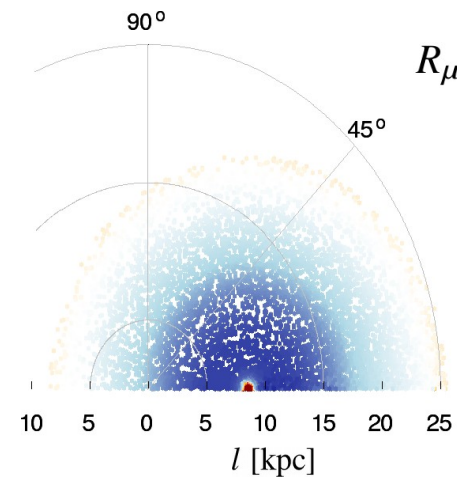
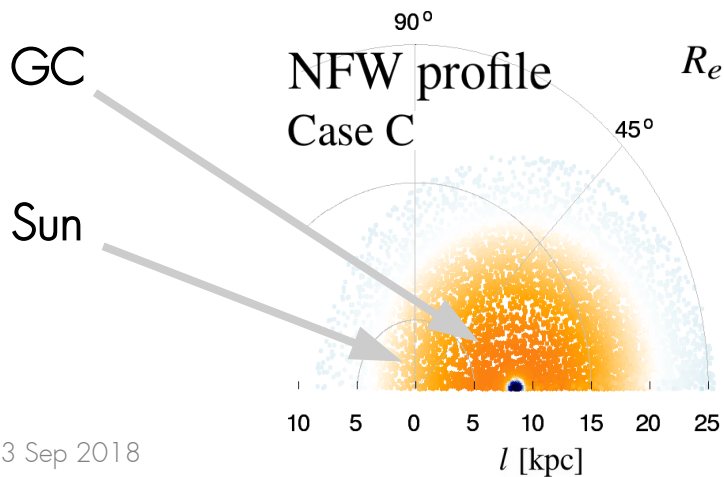
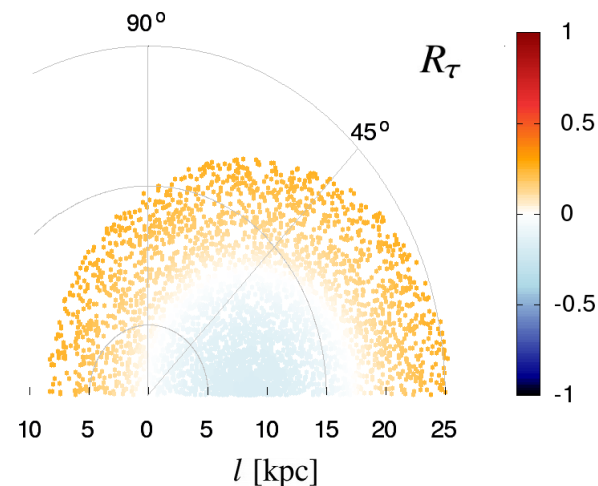
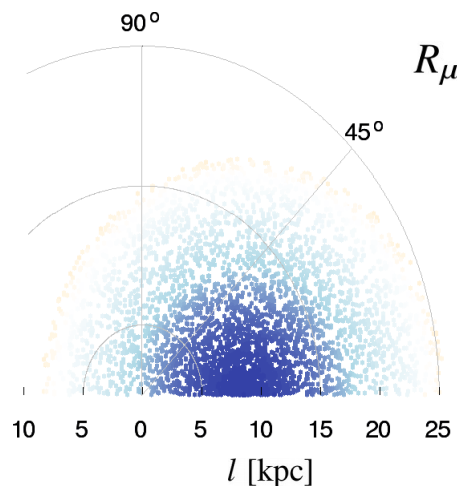
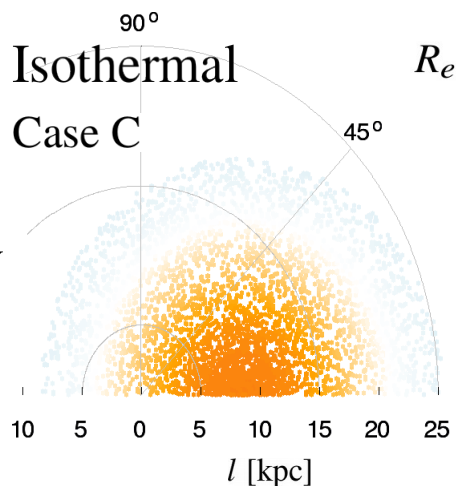
Higher  $\nu$ -energy, smaller potential are accessible



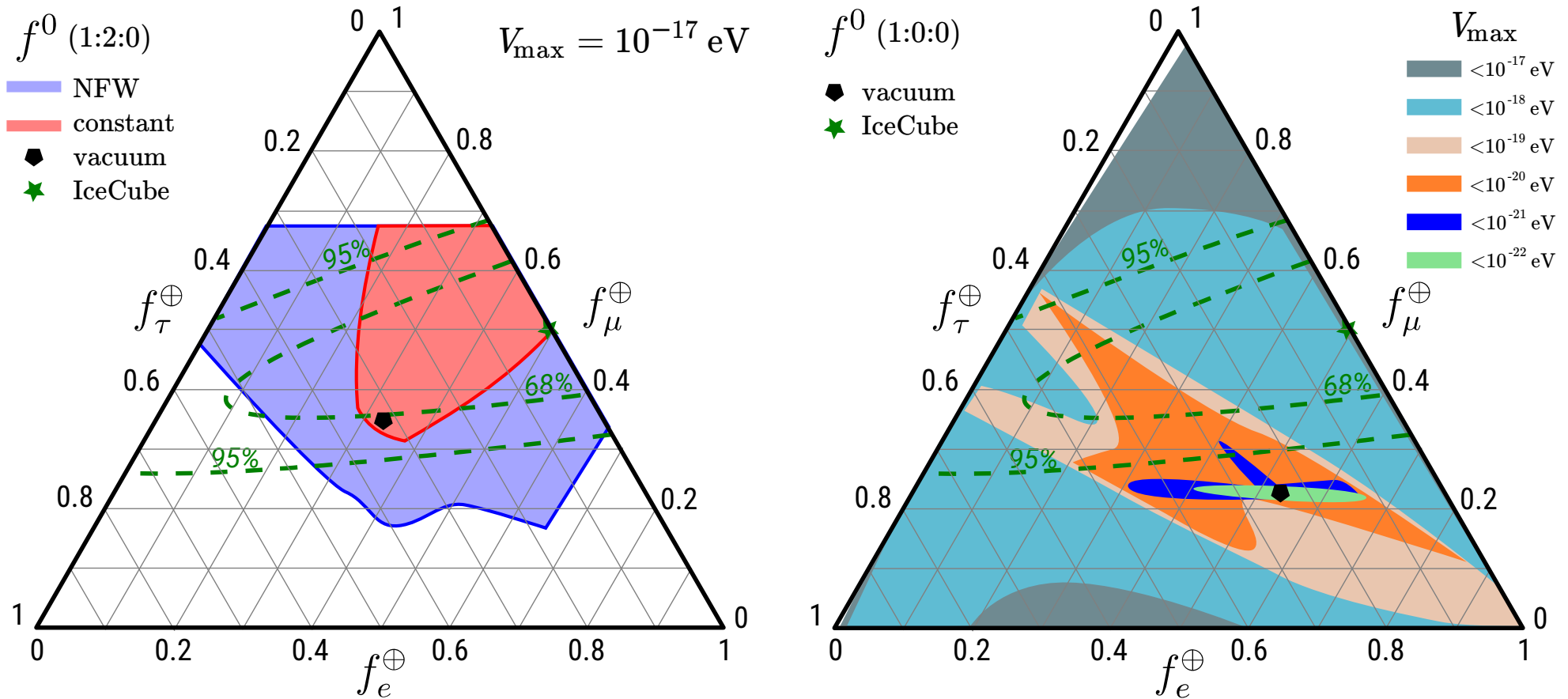
# Spatial dependence

$$\mathcal{V}_{\alpha\beta} = \mathcal{V}_{\alpha\beta}^{\oplus} \times f_{\text{DM}}(r)$$

$$\mathcal{V}_{11}^{\oplus} = 40 \times 10^{-21} \text{ eV}$$

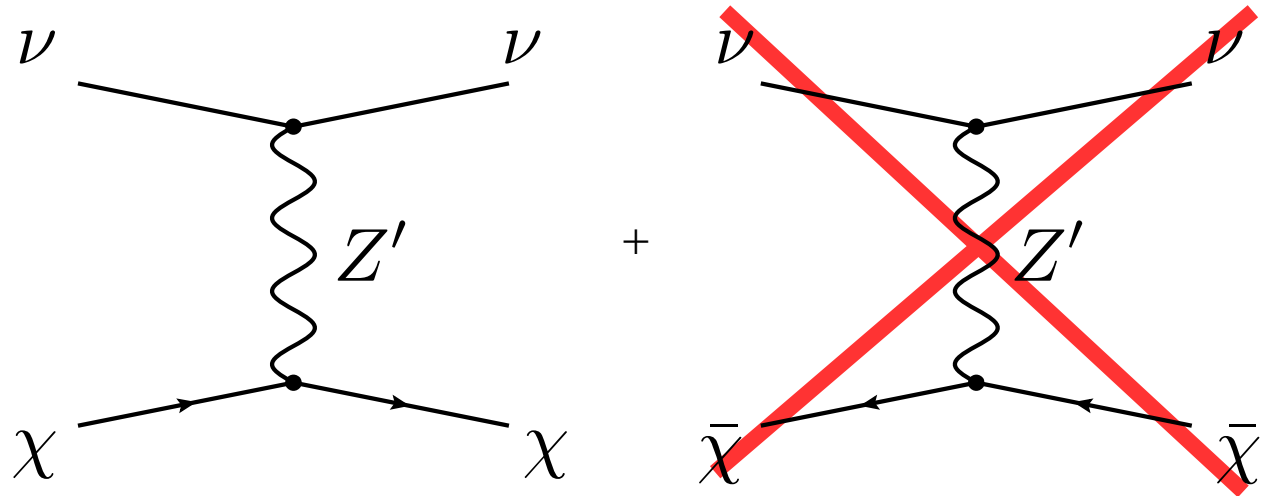
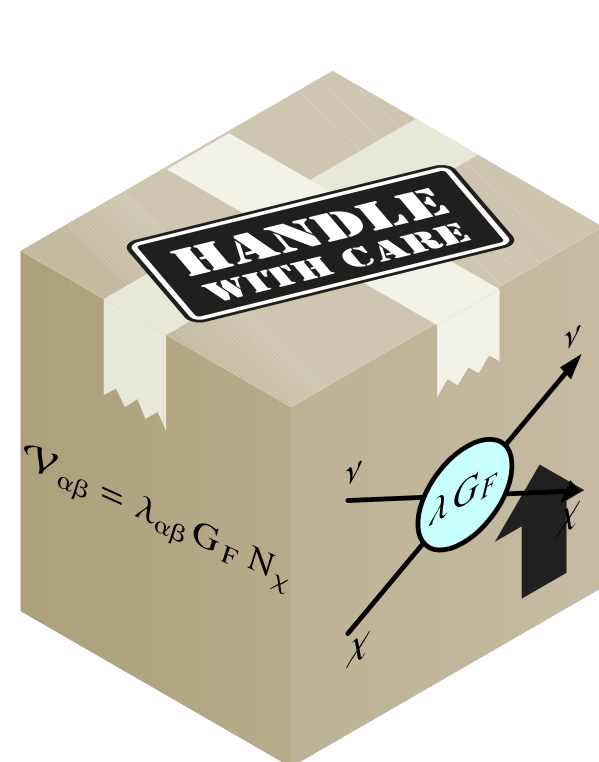


# Composition in a NFW halo



# Particle physics interpretation

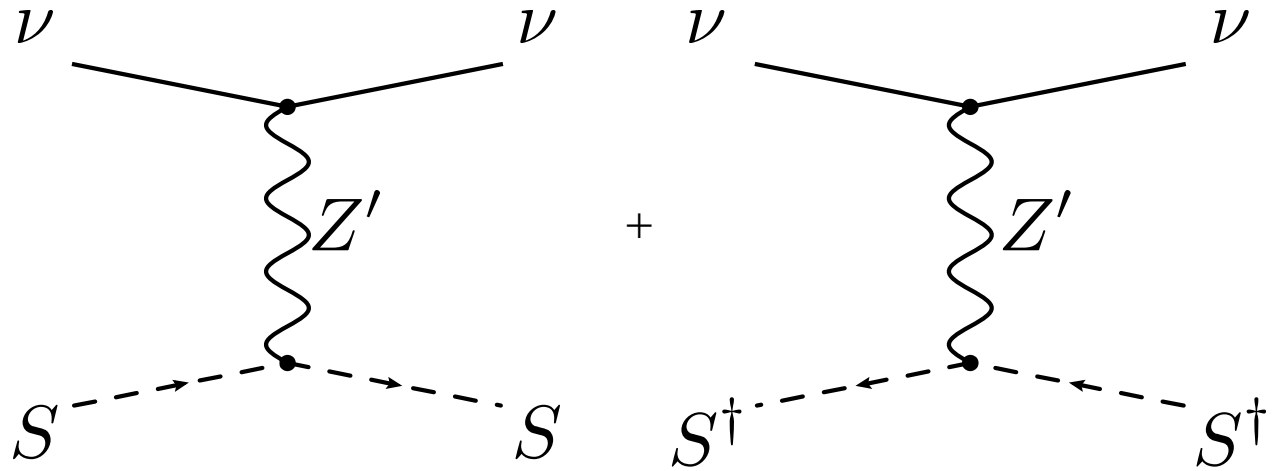
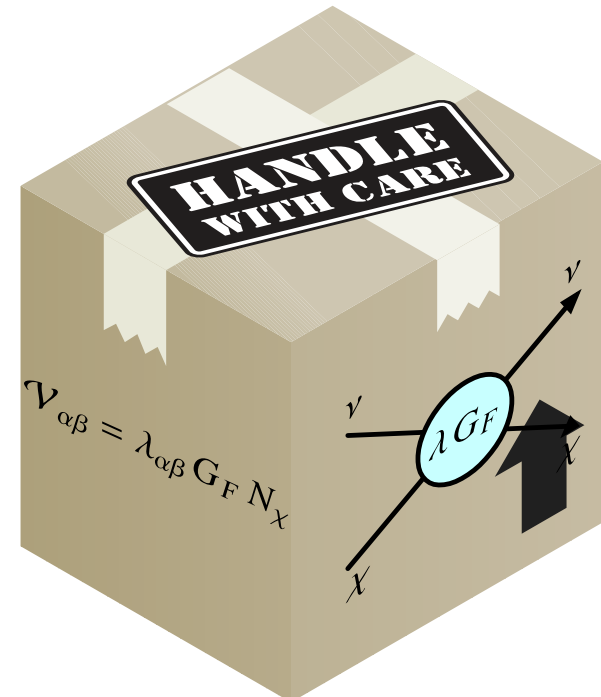
The simplest scenarios are models with asymmetric DM



$$\mathcal{V}_{\alpha\beta} = \lambda_{\alpha\beta} G_F N_\chi$$

# Particle physics interpretation

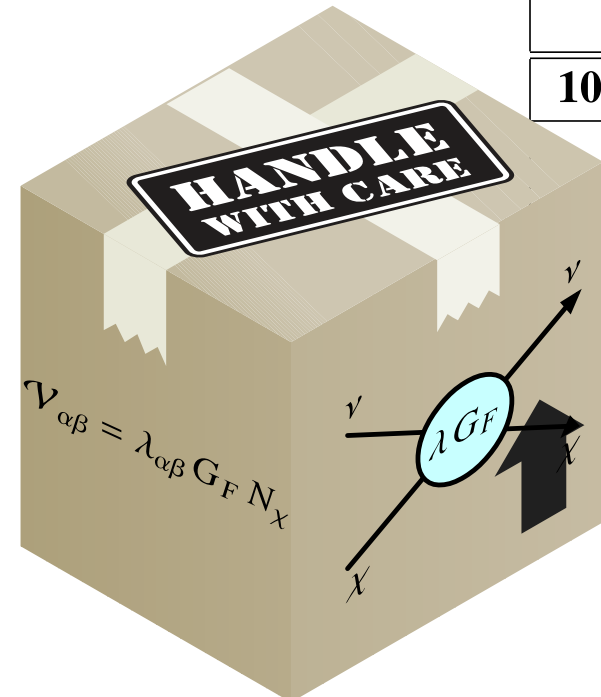
Or with scalar DM



$$\mathcal{V}_{\alpha\beta} = \lambda_{\alpha\beta} G_F N_\chi$$

# Particle physics interpretation

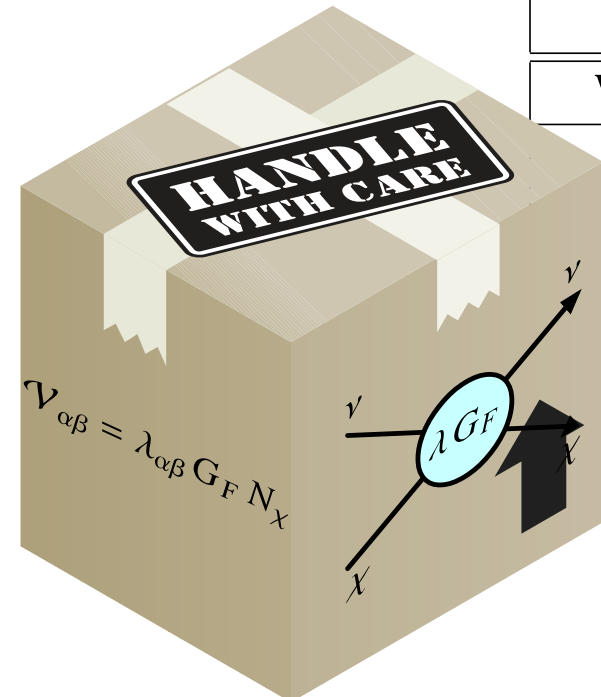
|                                                                                              |            |            |            |
|----------------------------------------------------------------------------------------------|------------|------------|------------|
| $V_{11}^{\oplus}$ [eV]                                                                       | $10^{-21}$ | $10^{-19}$ | $10^{-17}$ |
| <b>Weak scale (a) assumptions:</b> $G'_F = G_F, \lambda_{11} = 1$                            |            |            |            |
| $m_{\text{DM}}$ [eV]                                                                         | $10^{-8}$  | $10^{-10}$ | $10^{-12}$ |
| $l_\nu$ [pc]                                                                                 | $10^{-2}$  | $10^{-4}$  | $10^{-6}$  |
| <b>100 GeV DM (a) assumptions:</b> $m_{\text{DM}} = 100 \text{ GeV}, l_\nu = 50 \text{ kpc}$ |            |            |            |
| $\lambda_{11}$                                                                               | $10^{-7}$  | $10^{-9}$  | $10^{-11}$ |
| $m_{Z'}$ [eV]                                                                                | $10^{-2}$  | $10^{-4}$  | $10^{-6}$  |
| <b>1 keV DM (a) assumptions:</b> $m_{\text{DM}} = 1 \text{ keV}, l_\nu = 50 \text{ kpc}$     |            |            |            |
| $\lambda_{11}$                                                                               | $10^{-7}$  | $10^{-9}$  | $10^{-11}$ |
| $m_{Z'}$ [eV]                                                                                | $10^2$     | 1          | $10^{-2}$  |



One can try to explain the effective potential  
in terms of **particle physics scales**

# Particle physics interpretation

|                                                                           |            |            |            |
|---------------------------------------------------------------------------|------------|------------|------------|
| $V_{11}^{\oplus}$ [eV]                                                    | $10^{-21}$ | $10^{-19}$ | $10^{-17}$ |
| <b>Weak scale (a) assumptions:</b> $G'_F = G_F, \lambda_{11} = 1$         |            |            |            |
| $m_{\text{DM}}$ [eV]                                                      | $10^{-8}$  | $10^{-10}$ | $10^{-12}$ |
| $l_{\nu}$ [pc]                                                            | $10^{-2}$  | $10^{-4}$  | $10^{-6}$  |
| <b>Weak scale (b) assumptions:</b> $G'_F = G_F, l_{\nu} = 50 \text{ kpc}$ |            |            |            |
| $\lambda_{11}$                                                            | $10^{-7}$  | $10^{-9}$  | $10^{-11}$ |
| $m_{\text{DM}}$ [eV]                                                      | $10^{-15}$ | $10^{-19}$ | $10^{-23}$ |

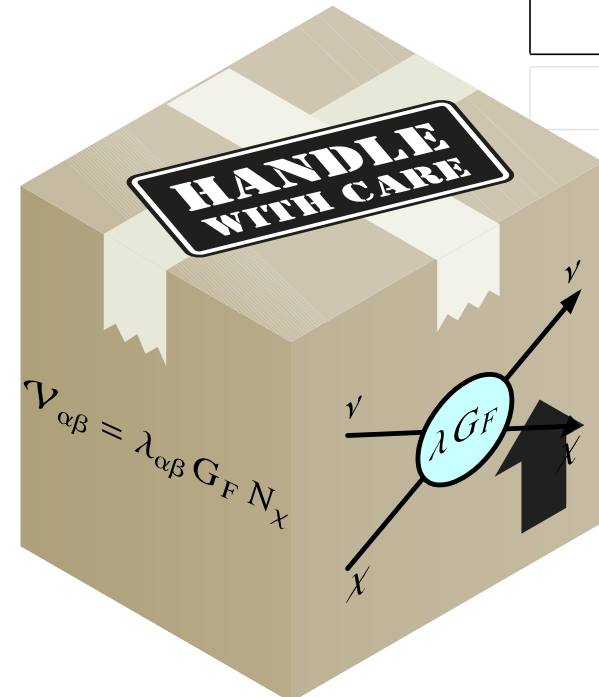


Assuming **weak scale** couplings and mediators DM has to be **extremely light**. Fuzzy DM, Bose-Einstein DM?

For  $\lambda=1$ , the mean free path is sub-pc :-|

# Particle physics interpretation

| $V_{11}^{\oplus}$ [eV]                                                                         | $10^{-21}$ | $10^{-19}$ | $10^{-17}$ |
|------------------------------------------------------------------------------------------------|------------|------------|------------|
| <b>100 GeV DM (a) assumptions:</b> $m_{\text{DM}} = 100 \text{ GeV}, l_{\nu} = 50 \text{ kpc}$ |            |            |            |
| $\lambda_{11}$                                                                                 | $10^{-7}$  | $10^{-9}$  | $10^{-11}$ |
| $m_{Z'} \text{ [eV]}$                                                                          | $10^{-2}$  | $10^{-4}$  | $10^{-6}$  |
| <b>1 keV DM (a) assumptions:</b> $m_{\text{DM}} = 1 \text{ keV}, l_{\nu} = 50 \text{ kpc}$     |            |            |            |
| $\lambda_{11}$                                                                                 | $10^{-7}$  | $10^{-9}$  | $10^{-11}$ |
| $m_{Z'} \text{ [eV]}$                                                                          | $10^2$     | 1          | $10^{-2}$  |



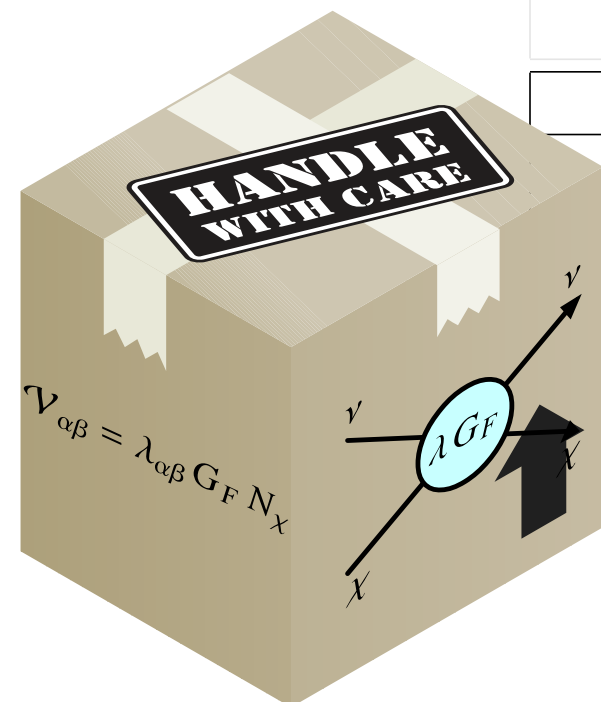
100 GeV DM

sub-eV mediators,  $g \sim \lambda^{1/2} = 10^{-3} - 10^{-6}$

$$\sigma_{\nu\chi} = 1.62 \times 10^{-23} (m_{\text{DM}}/\text{GeV}) \text{ cm}^2$$

# Particle physics interpretation

| $V_{11}^{\oplus}$ [eV]                                                                         | $10^{-21}$ | $10^{-19}$ | $10^{-17}$ |
|------------------------------------------------------------------------------------------------|------------|------------|------------|
| <b>100 GeV DM (a) assumptions:</b> $m_{\text{DM}} = 100 \text{ GeV}, l_{\nu} = 50 \text{ kpc}$ |            |            |            |
| $\lambda_{11}$                                                                                 | $10^{-7}$  | $10^{-9}$  | $10^{-11}$ |
| $m_{Z'}$ [eV]                                                                                  | $10^{-2}$  | $10^{-4}$  | $10^{-6}$  |
| <b>1 keV DM (a) assumptions:</b> $m_{\text{DM}} = 1 \text{ keV}, l_{\nu} = 50 \text{ kpc}$     |            |            |            |
| $\lambda_{11}$                                                                                 | $10^{-7}$  | $10^{-9}$  | $10^{-11}$ |
| $m_{Z'}$ [eV]                                                                                  | $10^2$     | 1          | $10^{-2}$  |



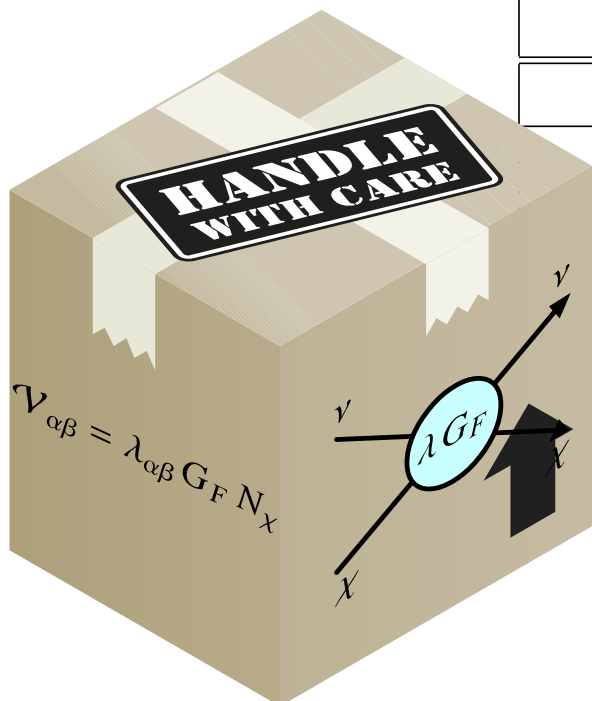
1 keV DM

eV mediators,  $g \sim \lambda^{1/2} = 10^{-3} - 10^{-6}$

$$\sigma_{\nu\chi} = 1.62 \times 10^{-23} (m_{\text{DM}}/\text{GeV}) \text{ cm}^2$$

# Particle physics interpretation

|                                                                                                  |            |            |            |
|--------------------------------------------------------------------------------------------------|------------|------------|------------|
| $V_{11}^{\oplus}$ [eV]                                                                           | $10^{-21}$ | $10^{-19}$ | $10^{-17}$ |
| <b>100 GeV DM (b) assumptions:</b> $m_{\text{DM}} = 100 \text{ GeV}, l_{\nu} = 10^6 \text{ Gpc}$ |            |            |            |
| $\lambda_{11}$                                                                                   | $10^{-17}$ | $10^{-19}$ | $10^{-21}$ |
| $m_{Z'}$ [eV]                                                                                    | $10^{-7}$  | $10^{-9}$  | $10^{-11}$ |
| <b>1 keV DM (b) assumptions:</b> $m_{\text{DM}} = 1 \text{ keV}, l_{\nu} = 10^6 \text{ Gpc}$     |            |            |            |
| $\lambda_{11}$                                                                                   | $10^{-17}$ | $10^{-19}$ | $10^{-21}$ |
| $m_{Z'}$ [eV]                                                                                    | $10^{-3}$  | $10^{-5}$  | $10^{-7}$  |



Assuming mean free path larger than the **Observable Universe**

Wilkinson et al. JCAP 1405 (2014) 011

$$\sigma_{\nu\chi} = 10^{-33} (m_{\text{DM}}/\text{GeV}) \text{ cm}^2$$

@MeV!

# Conclusions (of this part)

- Flavor composition might open a door to **New-Physics** effects
- Effects from the **DM halo** modify the **oscillation pattern** differently than in the homogeneous scenario
- (Hopefully) **Correlation** between flavor and arrival direction might serve as test of this hypothesis
- A particle physics explanation requires mediators lighter than **eV**

# Final words

- Neutrinos observables and DM are keys to unveil New Physics
- DM candidates lighter than WIMPs can affect neutrino observables
- We need to propose new way to test «unobservable» DM candidates

# Dark Matter Hunters

Digital resources for hunting the dark sector

dmhunters.org

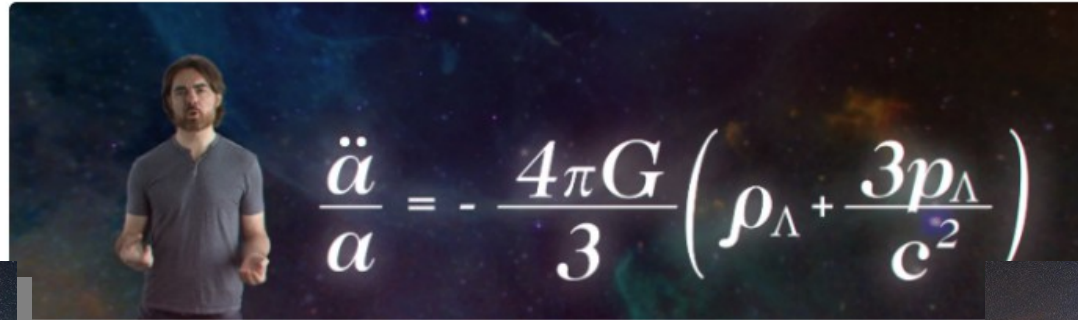
FOLLOW:



BLOG

MORE

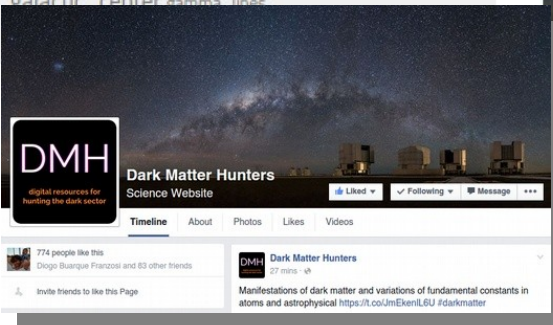
130Line AMS02\_Observatory analysis astro axion  
axion\_like\_particles BICEP2\_experiment  
black\_holes cmb constraints cosmic\_rays  
cosmology dark\_energy dark\_radiation  
direct\_detection dm\_distribution  
dynamics experimental FERMI\_LAT  
galactic\_center gamma\_lines



NEWS



Daily digest of papers about  
Dark Matter and related topics





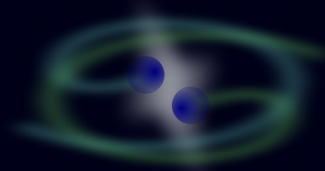
lawphysics

Latin American Webinars on Physics

# Recent detections of gravitational waves

Isabel Cordero-Carrión  
University of Valencia, Spain

Host: Joel Jones-Perez  
Wednesday 13 December 2017 15:00 GMT



 /lawphysicsw

 @lawphysics

 /lawphysics

 lawphysics.wordpress.com



# Thanks

# Backup

# Charge assignments

5 possible models

|         | $L$ | $N_1$ | $N_2$ | $S$   | $X$   |
|---------|-----|-------|-------|-------|-------|
| $n = 1$ | 1   | -1    | $1/7$ | $6/7$ | $2/7$ |
| $n = 2$ | 1   | -1    | $1/3$ | $2/3$ | $2/3$ |
| $n = 3$ | 1   | -1    | $3/5$ | $2/5$ | $6/5$ |

$$m+n = 4$$

$$V_I = \lambda_{\text{cp}} e^{i\delta} X^m S^{\dagger n}$$

$$m+n = 3$$

|         | $L$ | $N_1$ | $N_2$ | $S$   | $X$   |
|---------|-----|-------|-------|-------|-------|
| $n = 1$ | 1   | -1    | $1/5$ | $4/5$ | $2/5$ |
| $n = 2$ | 1   | -1    | $1/2$ | $1/2$ | 1     |

# The rest of the scalar potential

$$V_{SX} = -\mu_S^2 |S|^2 + \frac{\lambda_S}{4} |S|^4 - \mu_X^2 |X|^2 + \frac{\lambda_X}{4} |X|^4 + \lambda_5 |S|^2 |X|^2 + V_I$$

$$V_{HSX} = -\mu_H^2 H^\dagger H + \frac{\lambda_H}{4} (H^\dagger H)^2 + \lambda_{HS} |S|^2 H^\dagger H + \lambda_{HX} |X|^2 H^\dagger H$$

# Mass spectrum

$$m_h^2 \simeq \frac{v_h^2}{2} \left\{ \frac{\lambda_H}{2} + 2 \left( \frac{\lambda_{HX}^2 \lambda_S + \lambda_{HS}^2 \lambda_X - 4\lambda_5 \lambda_{HS} \lambda_{HX}}{4\lambda_5^2 - \lambda_S \lambda_X} \right) \right\}$$

$$M_{\zeta_3}^2 \simeq \frac{v_S^2}{2} \left( \frac{-A + A\psi + 2\lambda_X \omega \psi}{2\psi} \right)$$

$$M_{\zeta_4}^2 \simeq \frac{v_S^2}{2} \left( \frac{A + A\psi + 2\lambda_X \omega \psi}{2\psi} \right)$$

$$\lambda_S = A + \lambda_X \omega^2$$

$$\lambda_5 = -A \left( \frac{\sqrt{1 - \psi^2}}{4\omega\psi} \right)$$

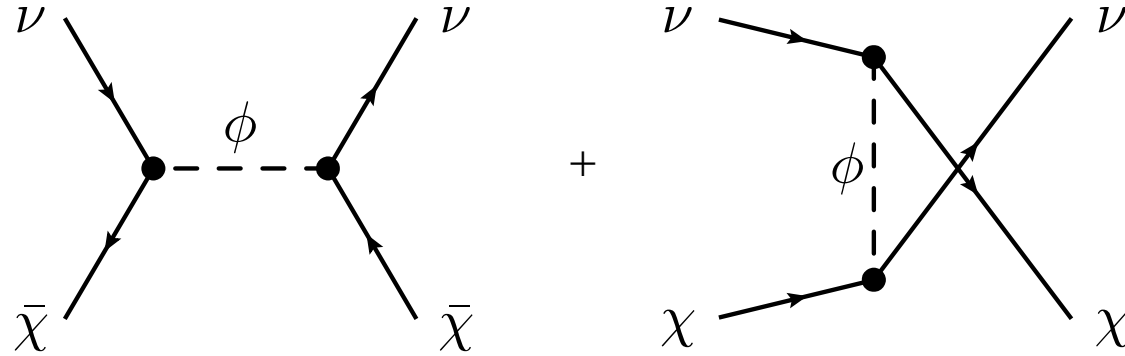
# Numerology

| Parameter | Value                |
|-----------|----------------------|
| $M$       | 100 TeV              |
| $\mu$     | 10 MeV               |
| $m_D$     | 10 GeV               |
| $v_S$     | $10^8 - 10^{12}$ GeV |
| $\omega$  | 0.4 – 1.6            |

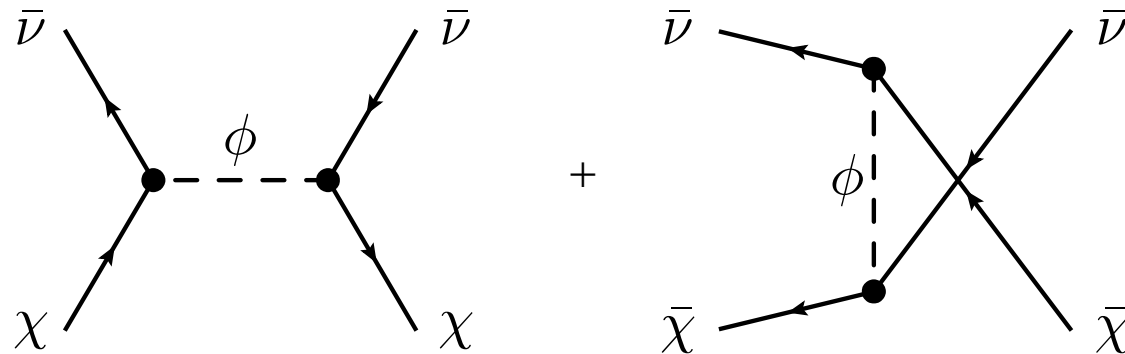
$$\lambda_{\text{cp}} \simeq \frac{M_J^2}{v_S^2} < 10^{-22}$$

# Dirac DM model

Neutrinos



Antineutrinos



No cancellation at first order due to diagrams are different