

## S5 Posterior Eulerian dynamics

IBMLib comes along with an experimental template for posterior advection-diffusion-reaction (ADR) modelling, which has been tested in a real study [58]. Posterior refers the fact that feedback on physics is not supported, whether online or offline. The IBMLib ADR module has the advantage that it can scoop out a sub region of the physical model domain and only apply the ADR module here, allowing to speed up the calculation.

Since Eulerian simulations are fundamentally different from Lagrangian simulations, the basic IBMLib configuration diagram Fig 1 is also a little different, see Fig S4. The main difference is that the biology module is replaced by a Eulerian module. The Eulerian module has a closer relation to the physics module and should be considered to be a shell around the physics module, for reasons of efficiency and because strict mass conservation must be obeyed in Eulerian dynamics, if the state variables form a closed system. The biology module becomes a point production module, which is not accessed from the task module, but only via the Eulerian module. The point-production module can contain arbitrary complex reaction processes. It should be emphasized that the physics API is still fully accessible in the task module. The Eulerian API (accessed in the task module) is given in Table 4. It shows that a class describing an Eulerian field must be provided, along with constructors/destructors and updaters. `update_eulerian_field` will trigger a call of `update_physical_field`. A folder `eulerian_providers` in the IBMLib distribution organizes templates for Eulerian simulations, and `task_providers` has an Eulerian simulation template illustrating the usage. At some point in the future a fusion between Eulerian and Lagrangian mode may be enabled, since there is no fundamental limitations on that.

**Table 4.** Eulerian interface in IBMLib, defining Eulerian states and dynamics.

service	type	summary
<code>eulerian_field</code>	derived type definition	definition of Eulerian field
<code>init_advection_diffusion</code>	subroutine	init this module
<code>close_advection_diffusion</code>	subroutine	close this module
<code>init_eulerian_field</code>	subroutine	constructor for <code>eulerian_field</code>
<code>close_eulerian_field</code>	subroutine	destructor for <code>eulerian_field</code>
<code>interpolate_eulerian_field</code>	subroutine	interpolate at a given position
<code>update_eulerian_field</code>	subroutine	Eulerian field forward step
<code>update_eulerian_auxillaries</code>	subroutine	updates auxillaries for Eulerian dynamics
<code>dump_2Dframe</code>	subroutine	dump field to file
<code>get_data</code>	subroutine	export pointer to data

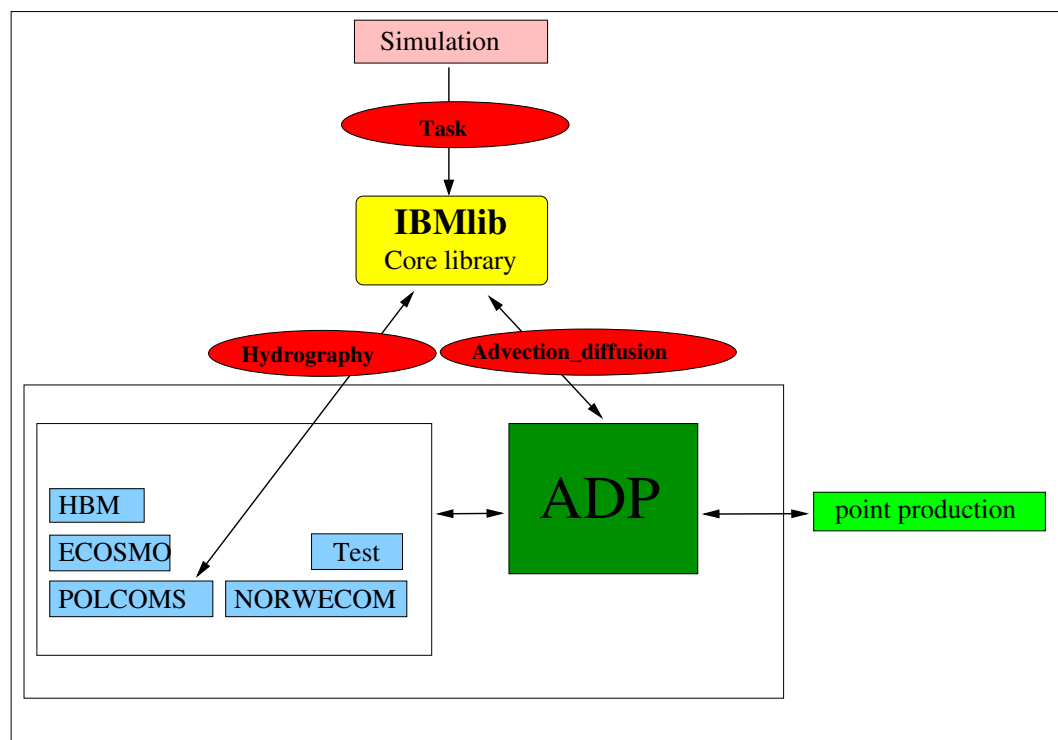


Fig S4. IBMlib in Eulerian configuration.