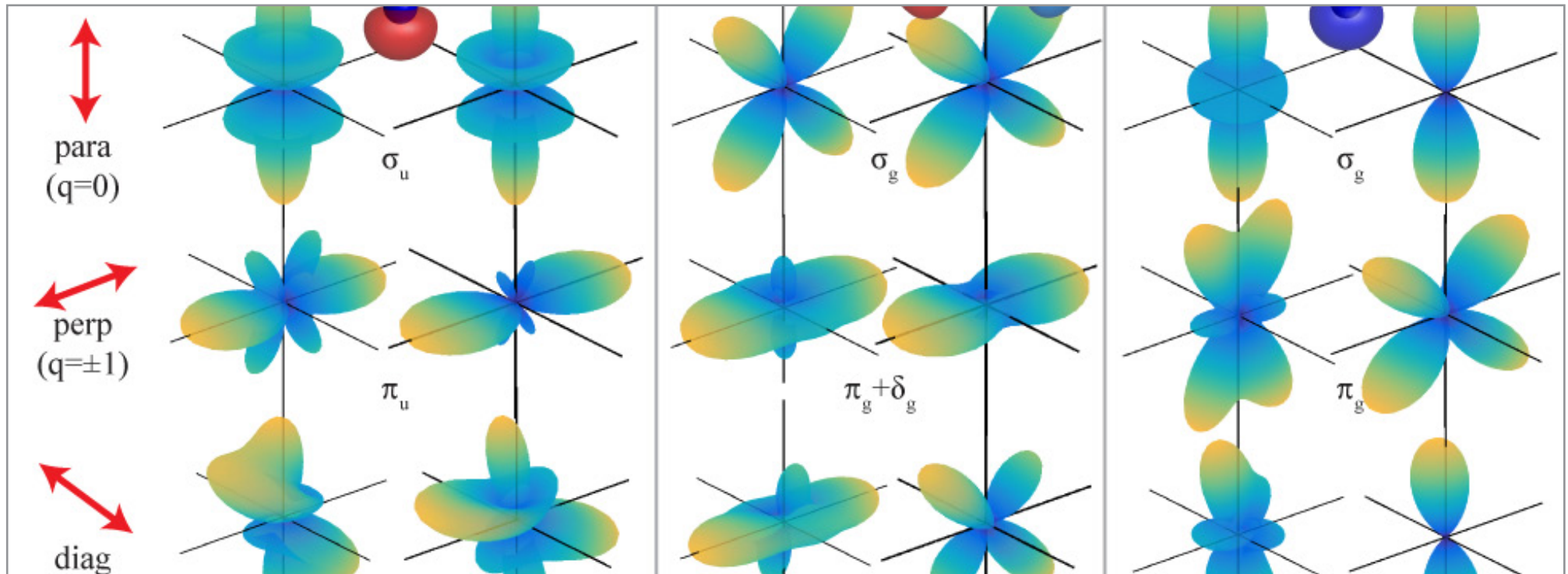


# Bootstrapping (Ultrafast) Photoionization Dynamics



Paul Hockett

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*National Research Council of Canada, Ottawa*

Available via Figshare, DOI: [10.6084/m9.figshare.5645509](https://doi.org/10.6084/m9.figshare.5645509)

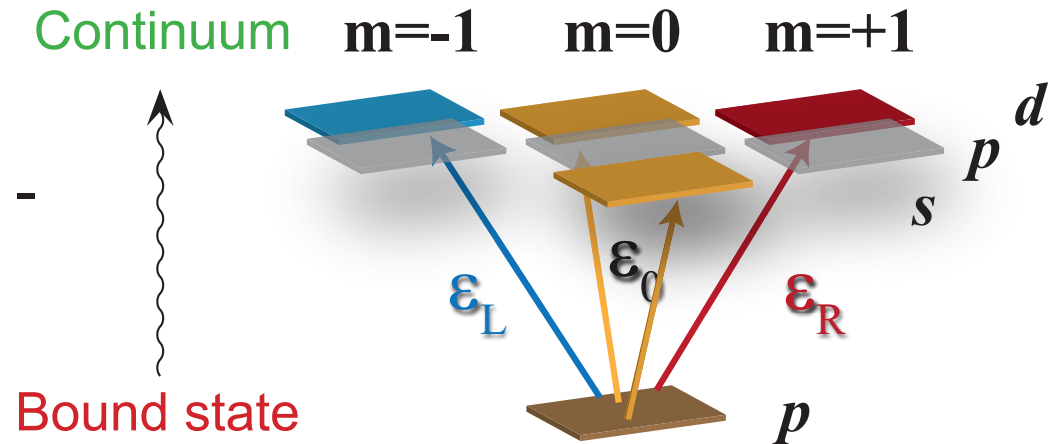
*femtolab.ca*



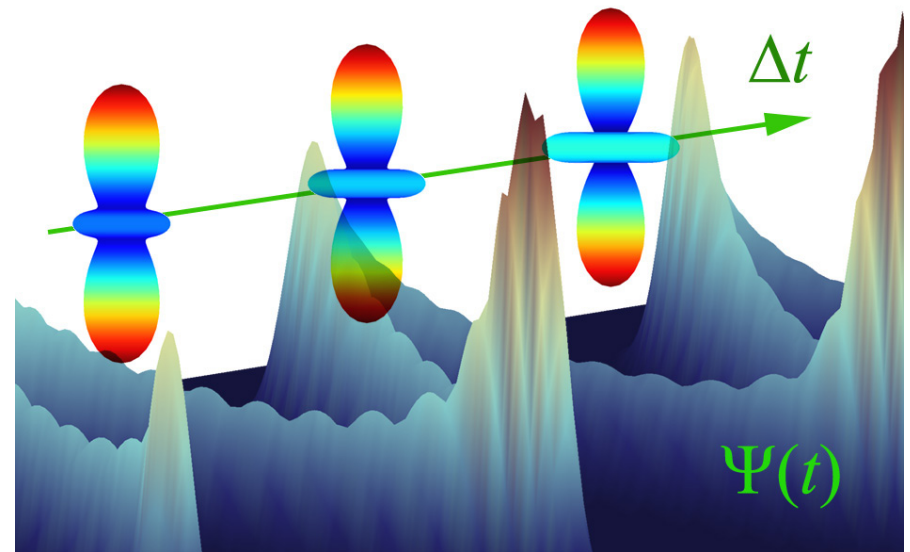
# photoionization interferometry

Photoionization is an interferometric process, in which multiple paths can contribute to the final continuum photoelectron state.

**(1) Intrinsic:** interferences between final (continuum) states - photoionization dynamics.



**(2) Extrinsic/dynamic:** additional pathways due to, e.g., prepared wavepacket, control fields, etc. etc.



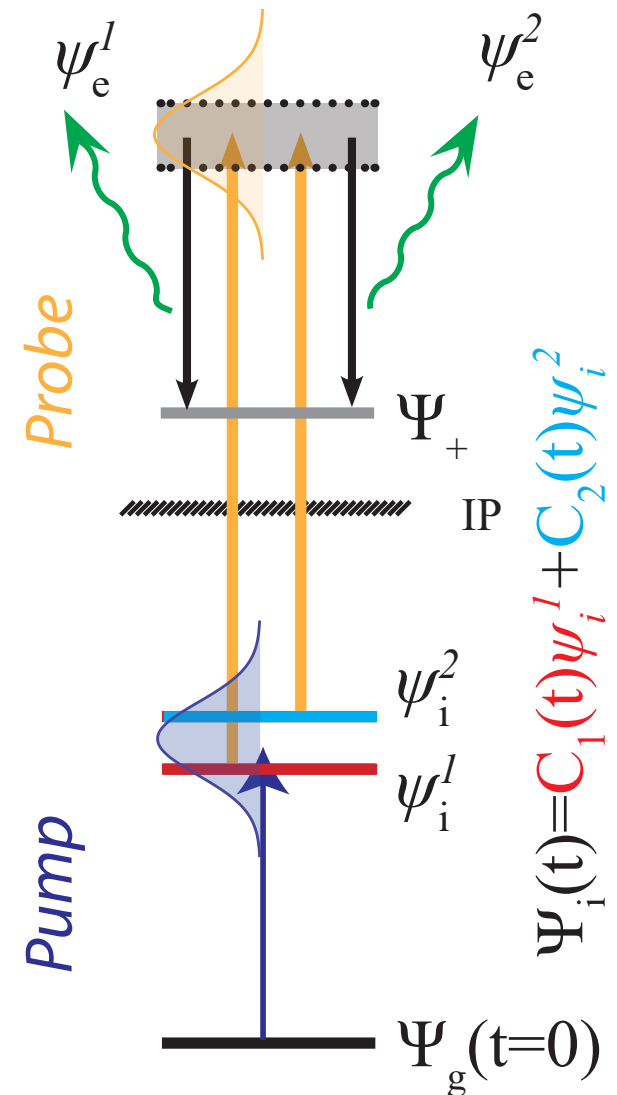
*For an early discussion along these lines, see:*  
Cohen, H., & Fano, U. (1966).  
Interference in the Photo-Ionization of Molecules.  
Physical Review, 150(1), 30–33.  
<http://doi.org/10.1103/PhysRev.150.30>

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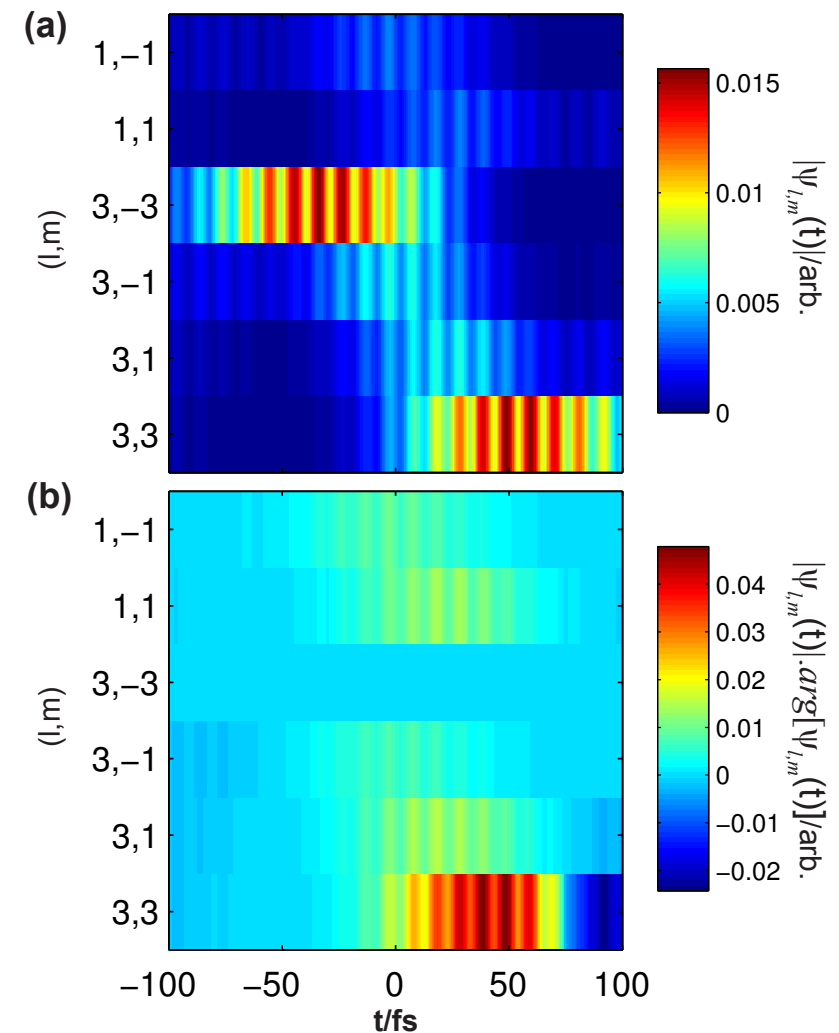
# photoelectron metrology

Photoelectron spectroscopy with a focus on (quantitative) photoionization dynamics.

With sufficient experimental information content, photoionization matrix elements (magnitudes & phases) can be retrieved.

cf.

- “complete” photoionization and scattering experiments
- quantum process & state tomography



Hockett, P., Wollenhaupt, M., & Baumert, T. (2015).  
Coherent control of photoelectron wavepacket angular interferograms.  
Journal of Physics B: Atomic, Molecular and Optical Physics, 48(21), 214004.  
<http://doi.org/10.1088/0953-4075/48/21/214004>

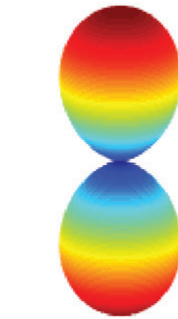


# matrix element reconstruction

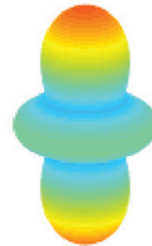
Requires:

(1) A phase-sensitive observable... photoelectron angular distributions (PADs) are angle-resolved photoelectron interferograms.

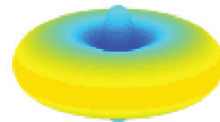
$$\psi_e = Y_{00} + Y_{20}e^{-i\eta}$$



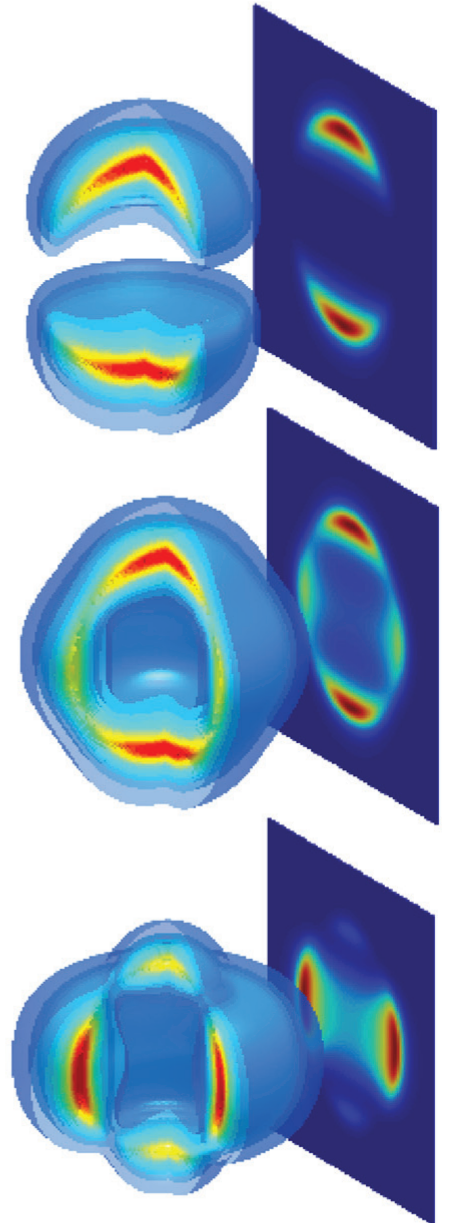
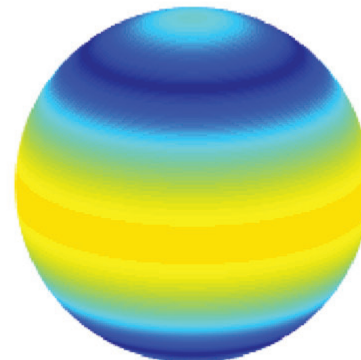
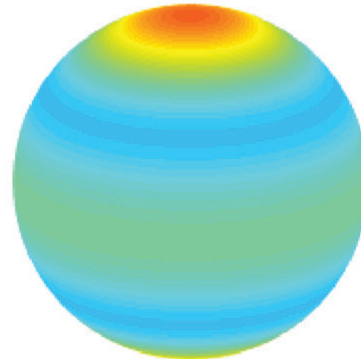
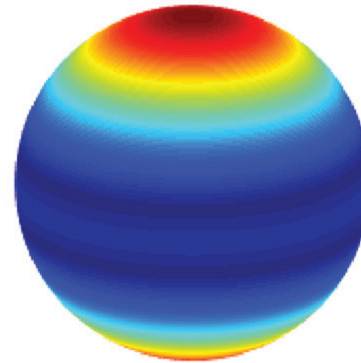
$\eta=0$



$\eta=\pi/2$



$\eta=\pi$

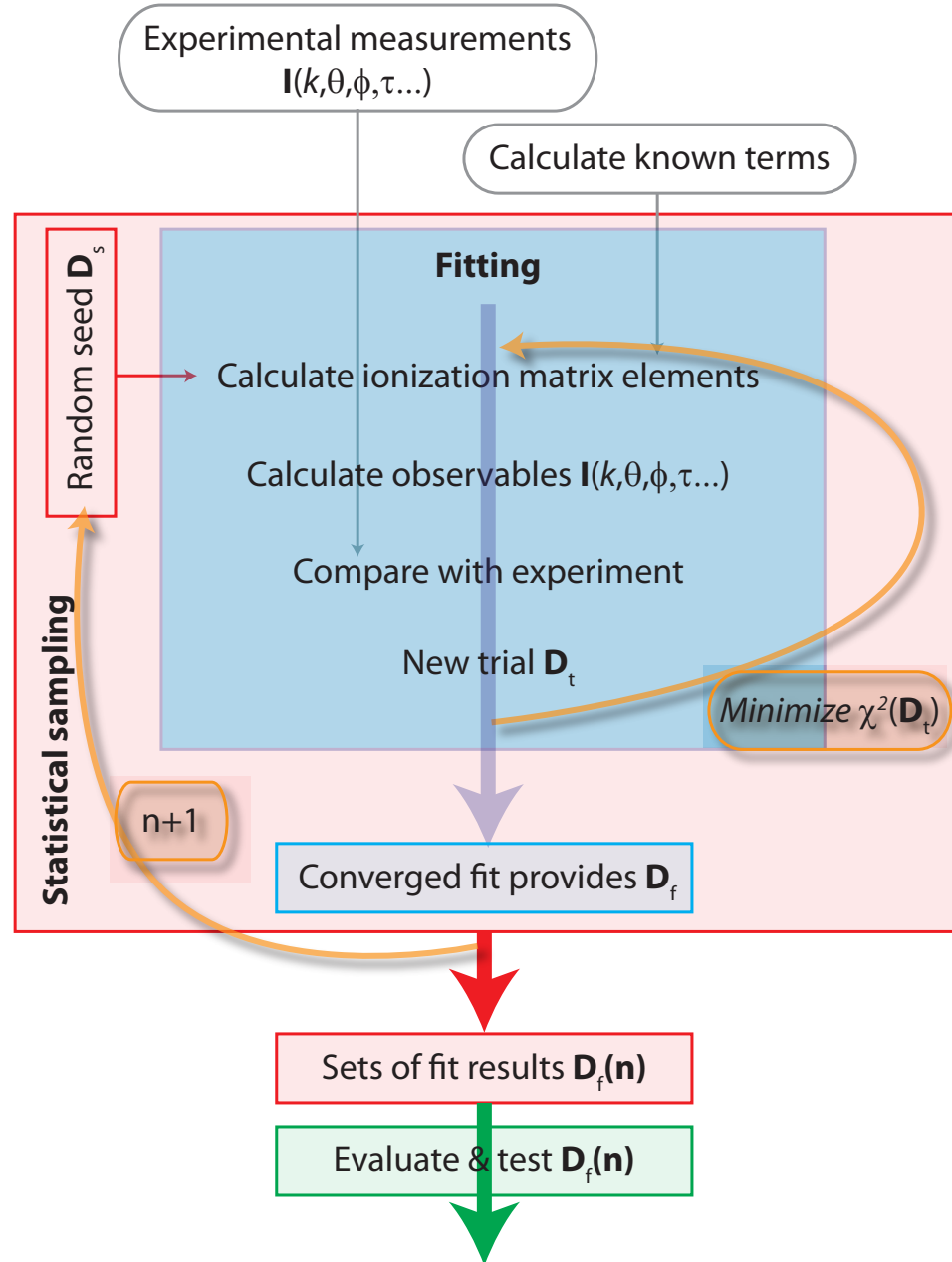


# matrix element reconstruction

## Requires:

(1) A phase-sensitive observable... photoelectron angular distributions (PADs) are angle-resolved photoelectron interferograms.

(2) Reconstruction/retrieval technique for the system properties of interest (matrix elements, density matrix etc.).



# bootstrapping references

## Bootstrapping to the Molecular Frame with Time-domain Photoionization Interferometry

[Alt. title: *Molecular Frame Reconstruction Using Time-Domain Photoionization Interferometry*]

Claude Marceau, Varun Makhija, Dominique Platzter, A. Yu. Naumov, P. B. Corkum, Albert Stolow, D. M. Villeneuve and Paul Hockett

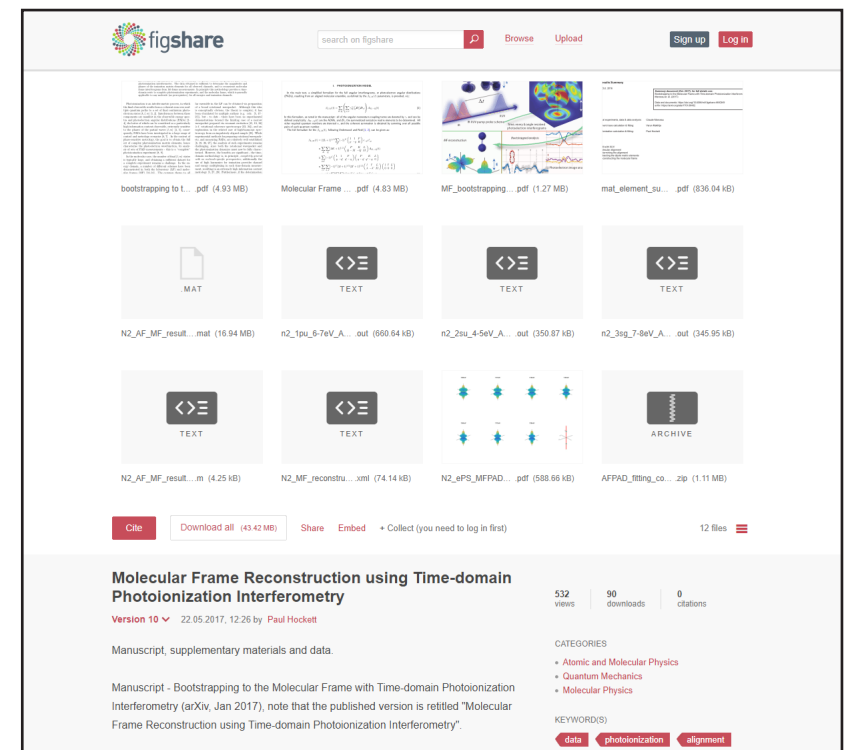
*Phys. Rev. Lett.*, 119(8), 83401. <http://doi.org/10.1103/PhysRevLett.119.083401>

*arXiv 1701.08432* (<https://arxiv.org/abs/1701.08432>).

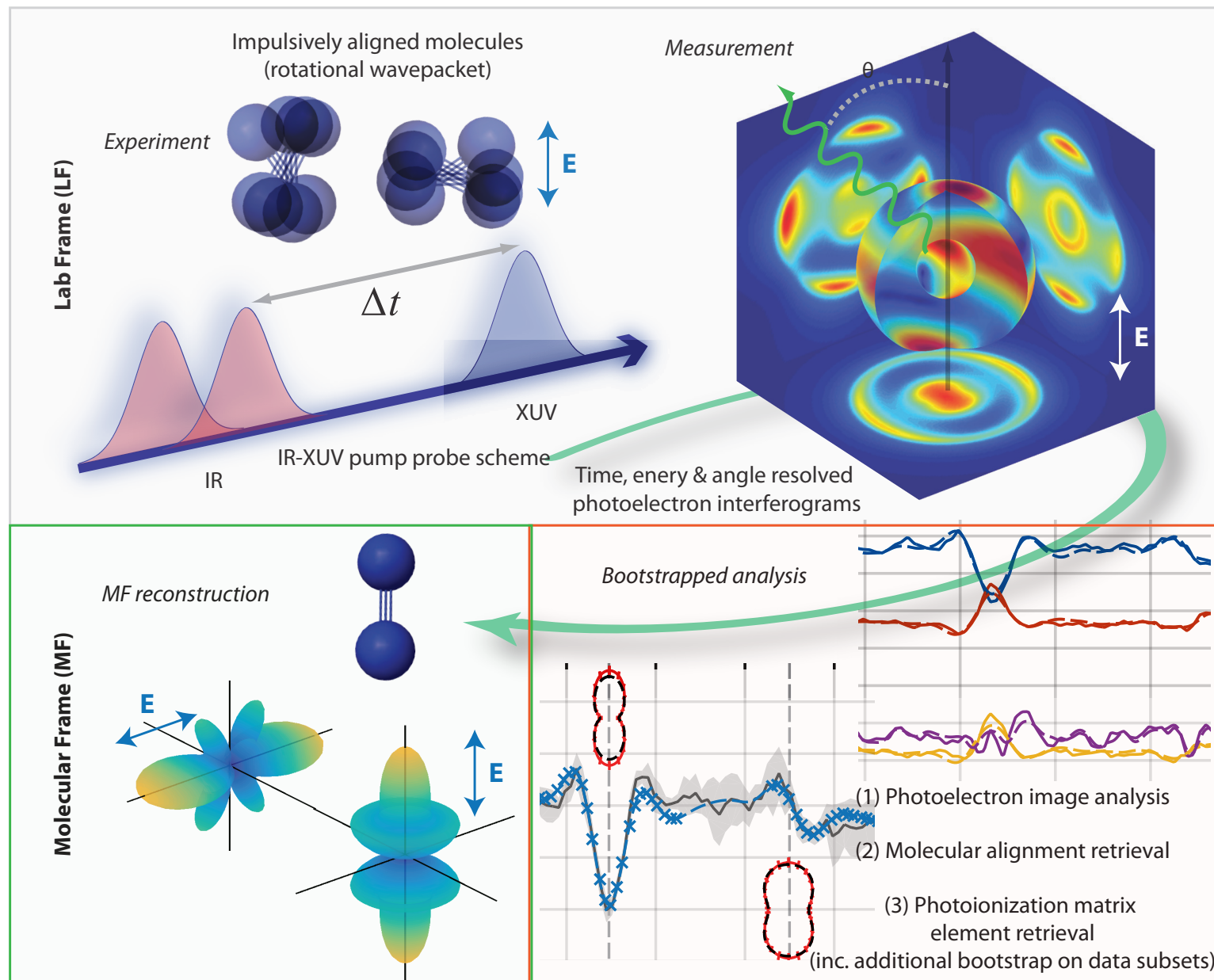
## Docs, data & code repository (figshare)

DOI: 10.6084/m9.figshare.4480349

<https://dx.doi.org/10.6084/m9.figshare.4480349>.



# bootstrapping concept



# bootstapping scheme

## Pump-probe scheme

$$|\Psi_g\rangle \xrightarrow{E_1^{IR}(t)+E_2^{IR}(t)} |\Psi_g(t)\rangle \xrightarrow{E^{XUV}(t)} |\Psi_+^\Gamma; \Psi_e^\Gamma(k)\rangle$$

Pump: rotational wavepacket for geometric control

$$|X^1\Sigma_g^+\rangle|v_X\rangle|J_XM_X\rangle \xrightarrow{E_1^{IR}(t)+E_2^{IR}(t)} |X^1\Sigma_g^+\rangle|v_X\rangle \sum_{J_XM_X} C_{J_XM_X}(t)|J_XM_X\rangle$$

Ensemble alignment:  $P(\theta, \phi, t) = \sum_{K,Q} A_{K,Q}(t) Y_{K,Q}(\theta, \phi)$

Probe: photoelectron + photoion products

$$\xrightarrow{E^{XUV}(t)} |\mathbf{k}, \Gamma l \lambda m\rangle |\Gamma\rangle |v_\Gamma\rangle \sum_{J_\Gamma M_\Gamma} C_{J_\Gamma M_\Gamma}(t) |J_\Gamma M_\Gamma\rangle$$

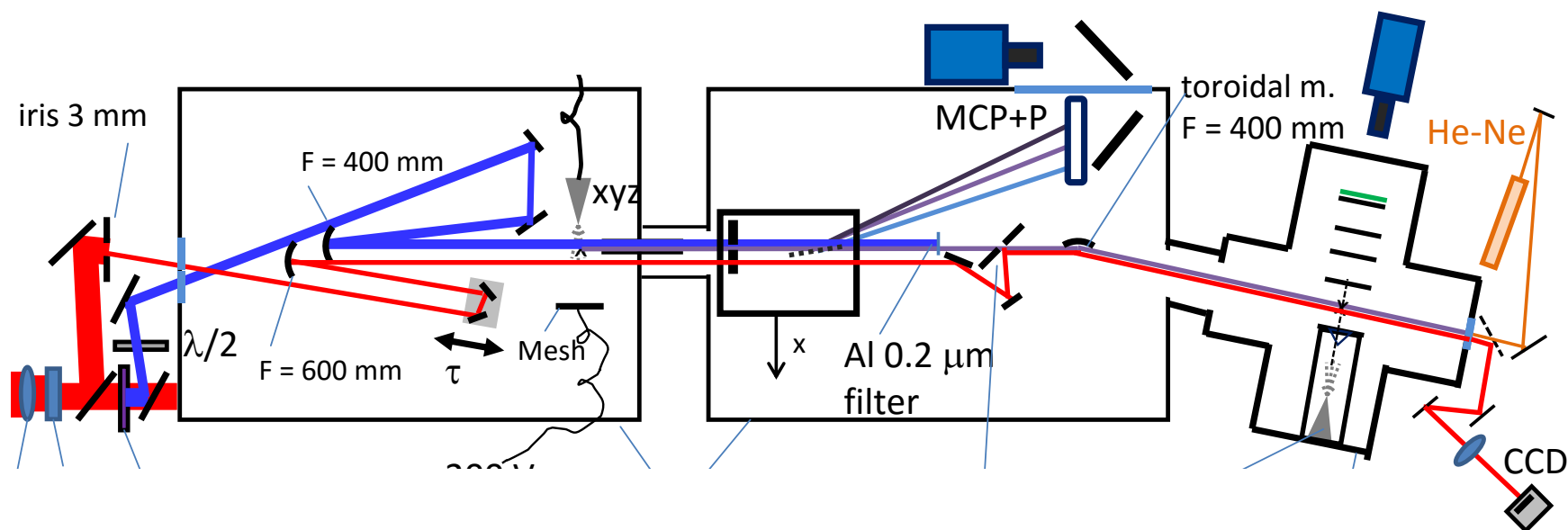


# experiment

- High harmonic generation, driven with 400 or 267nm.
- Single or multiple IR pulses for impulsive molecular alignment (rotational wavepacket).

## High harmonic generation

## VMI for photoelectron measurements

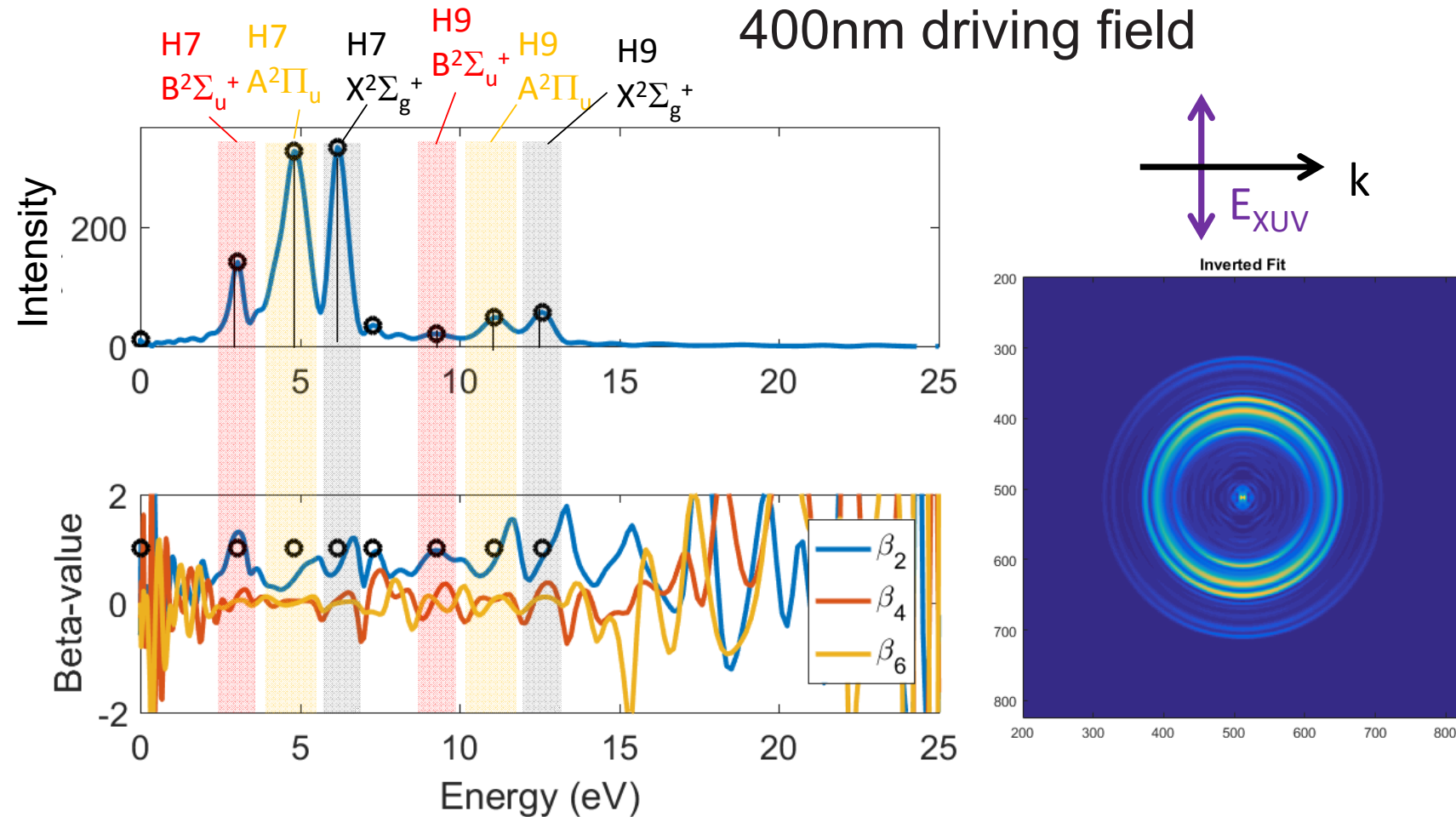


Claude Marceau & Dominique Platzer, NRC Jaslab (2016)



# (1) empirical analysis

Measurements - time, energy and angle-resolved photoelectron yields.



$$I(\theta, \phi; k, t) = \sum_{L=0}^{2l_{max}} \sum_{M=-L}^L \beta_{LM}(k, t) Y_{LM}(\theta, \phi)$$

Anisotropy parameters

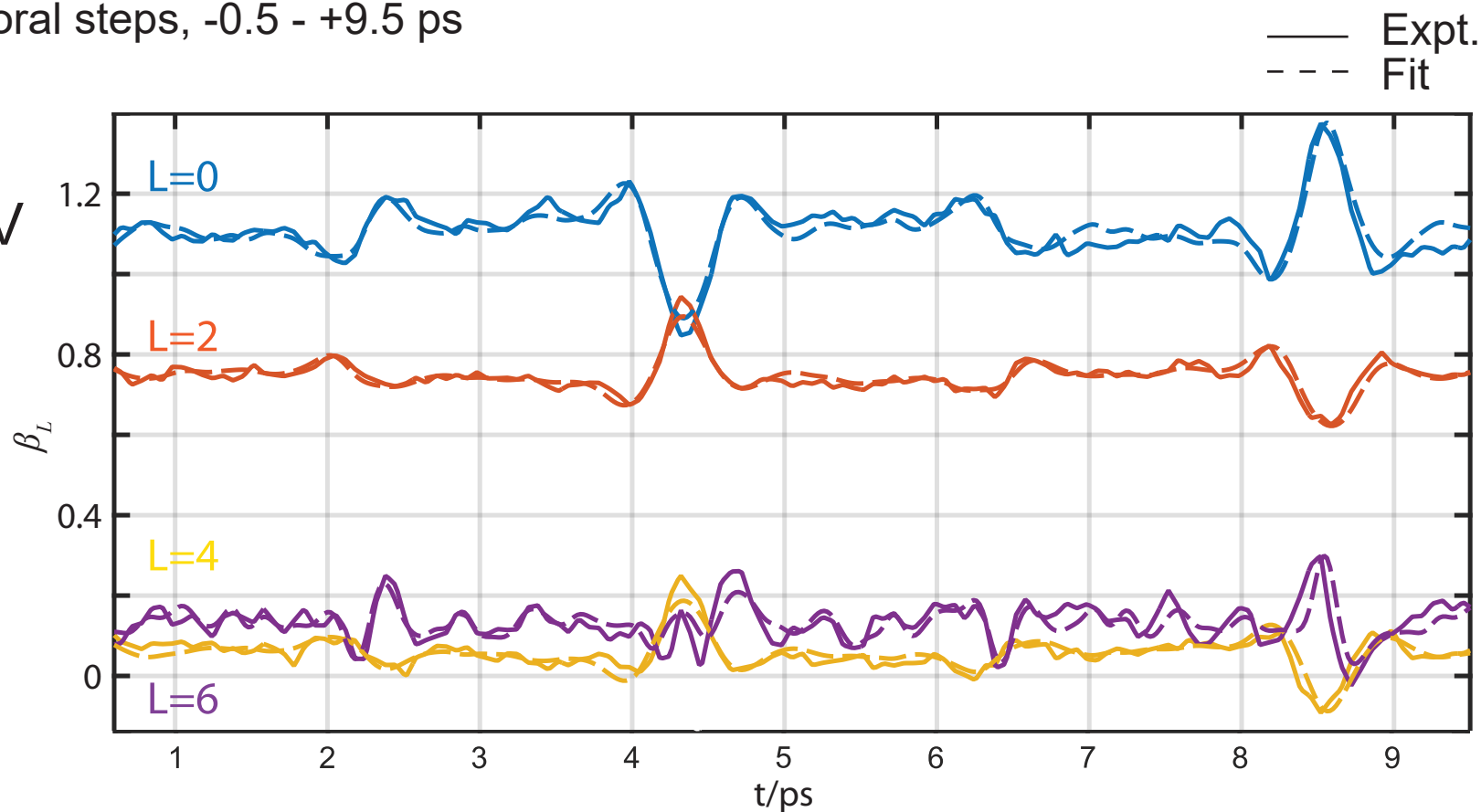
Spherical harmonics



# (1) N<sub>2</sub> dataset

- 267nm driving field
- Two-pulse IR rotational wavepacket preparation
- 150 temporal steps, -0.5 - +9.5 ps

X-state  
@7.7eV



Feature-averaged parameters:

$$\bar{\beta}_{L,M}^{\Gamma}(t) = \bar{\beta}_{L,M}^{\Gamma}(\Delta \bar{k}, t)$$



## (2): rotational wavepacket retrieval

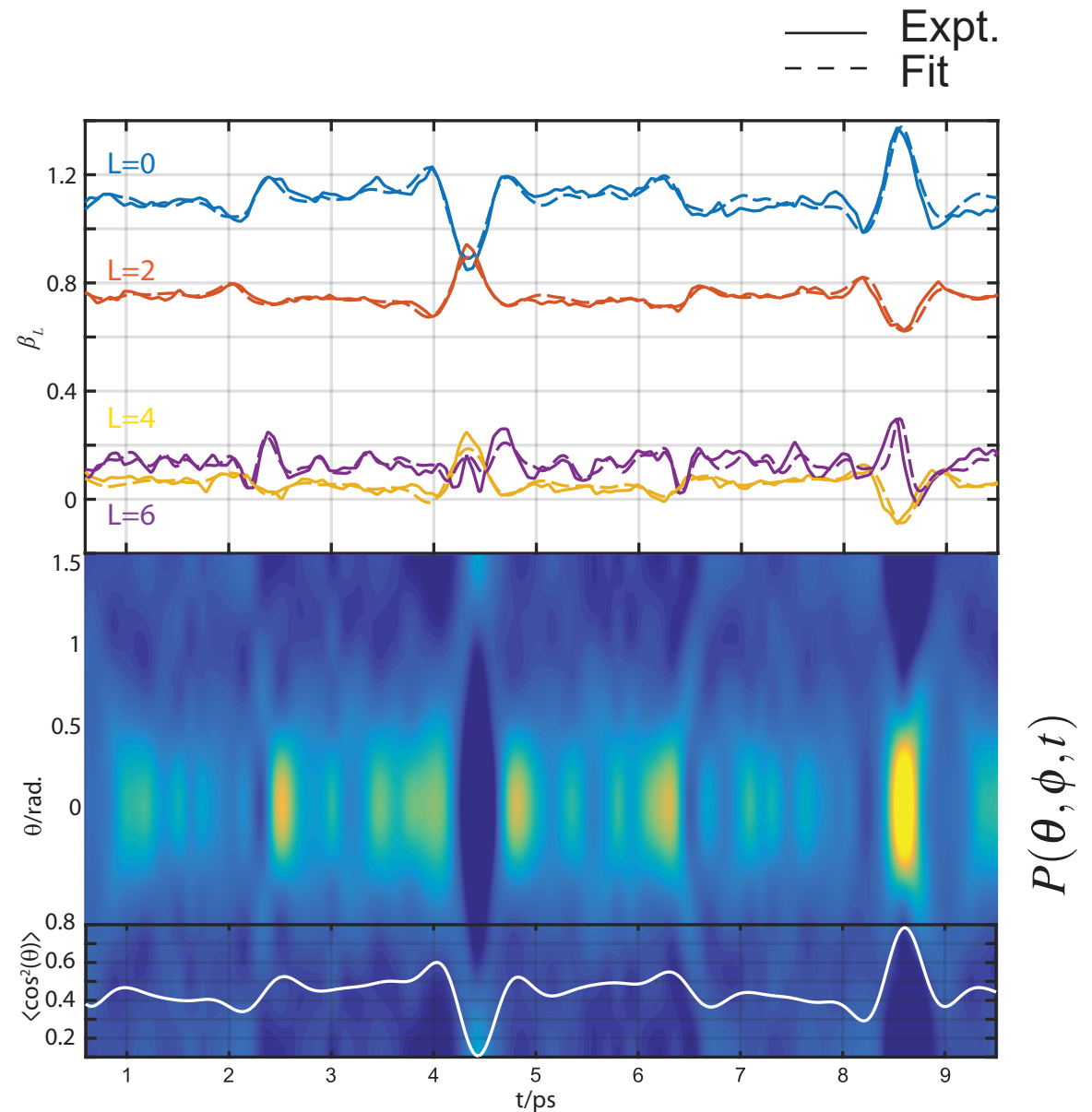
$$\bar{\beta}_{L,M}^{\Gamma}(t) = \sum_{K,Q} C_{K,Q}^{L,M}(\Gamma) A_{K,-Q}(t)$$

Fit data using simplified form (linear) to determine the rotational wavepacket.

- TDSE calculations of the rotational wavepacket, determines  $A_{K,Q}(t)$ .
- Best fit to data provides approximation of the wavepacket and conditions ( $T_{\text{rot}}$ , laser intensity, pulse structure).

↓

$$T_{\text{rot}} = 15\text{K}, I = 20 \text{ TWcm}^{-2}$$

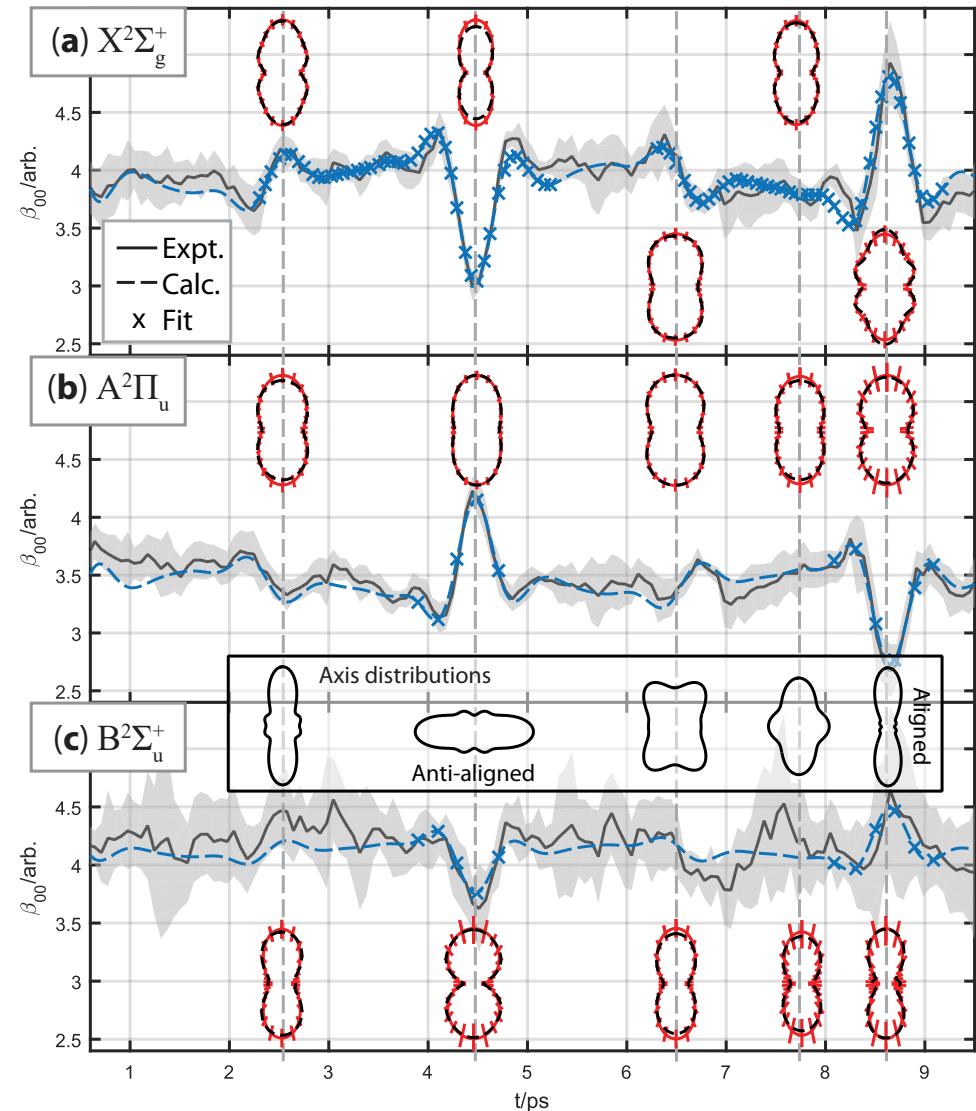


# (3a): photoionization dynamics

$$\bar{\beta}_{L,M}^{\Gamma}(t) = \sum_{K,Q} \left( \sum_{\alpha,\alpha'} \gamma_{K,Q}^{\Gamma,\alpha,\alpha'} \bar{D}_{\Gamma,\alpha}^*(\Delta k) \bar{D}_{\Gamma,\alpha'}(\Delta k) \right) A_{K,-Q}(t)$$

Fit data using full form (non-linear) to determine the photoionization dynamics.

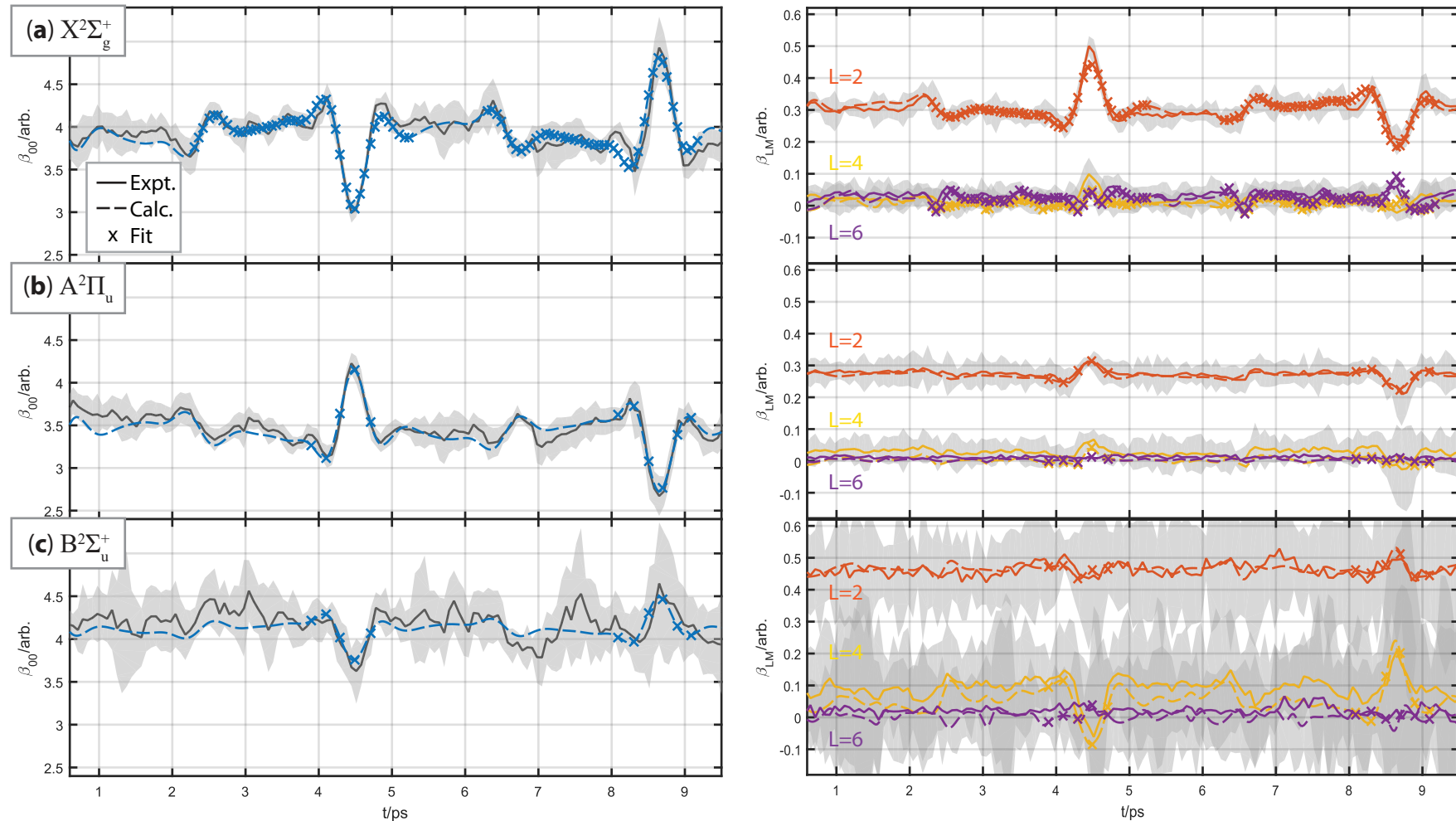
- $A_{K,Q}(t)$  from step (2).
- Calculate ang. mom. couplings  $\gamma$ .
- Fit determines (complex) matrix elements  $\mathbf{D}_{\alpha}$ .



# (3b): photoionization dynamics

Test fit results for uniqueness & cross-check via

- Statistical sampling
- Additional data



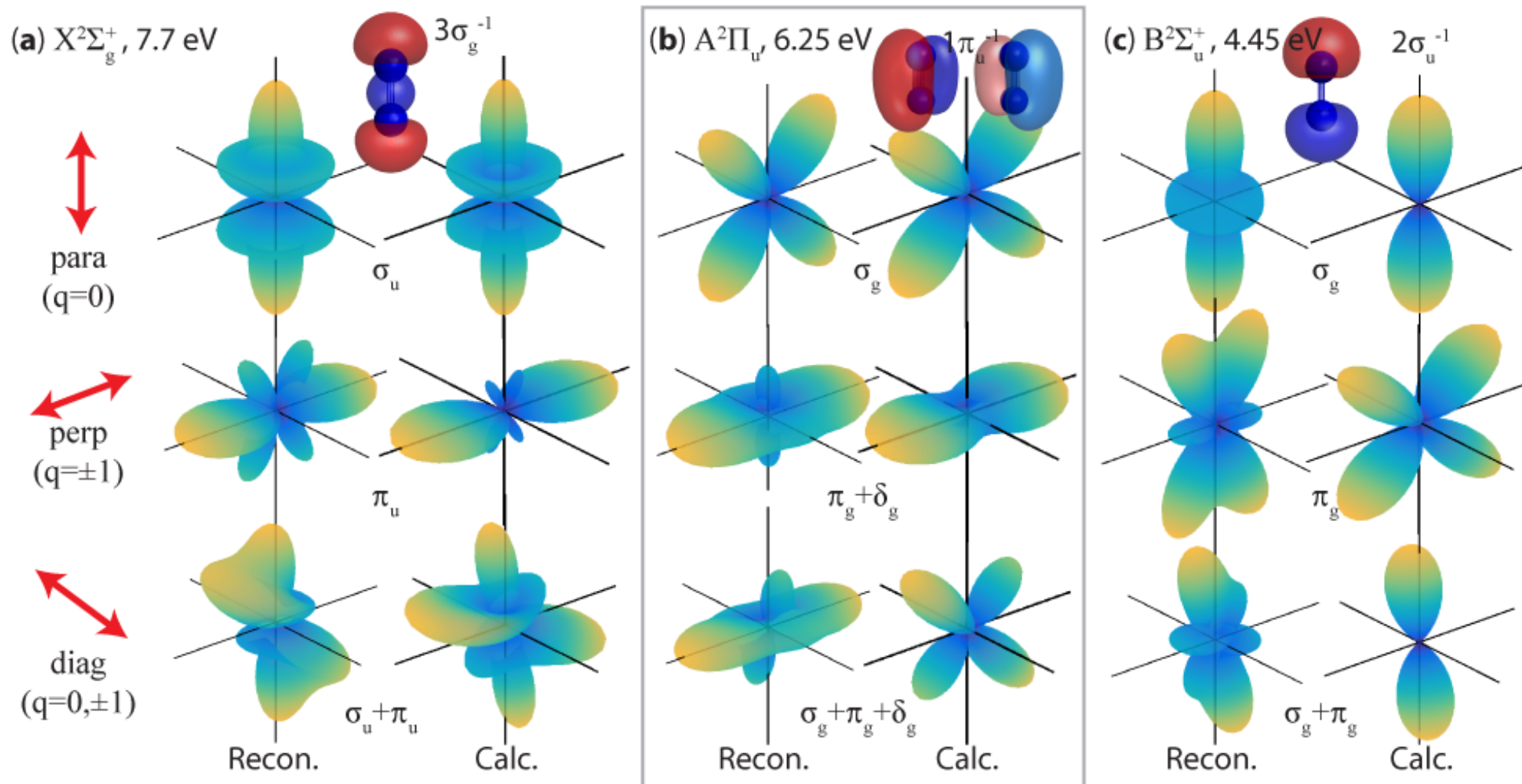
For details see online materials:

<https://dx.doi.org/10.6084/m9.figshare.4480349>

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# molecular frame reconstruction



Calculations use bound-free matrix elements from ePolyScat.

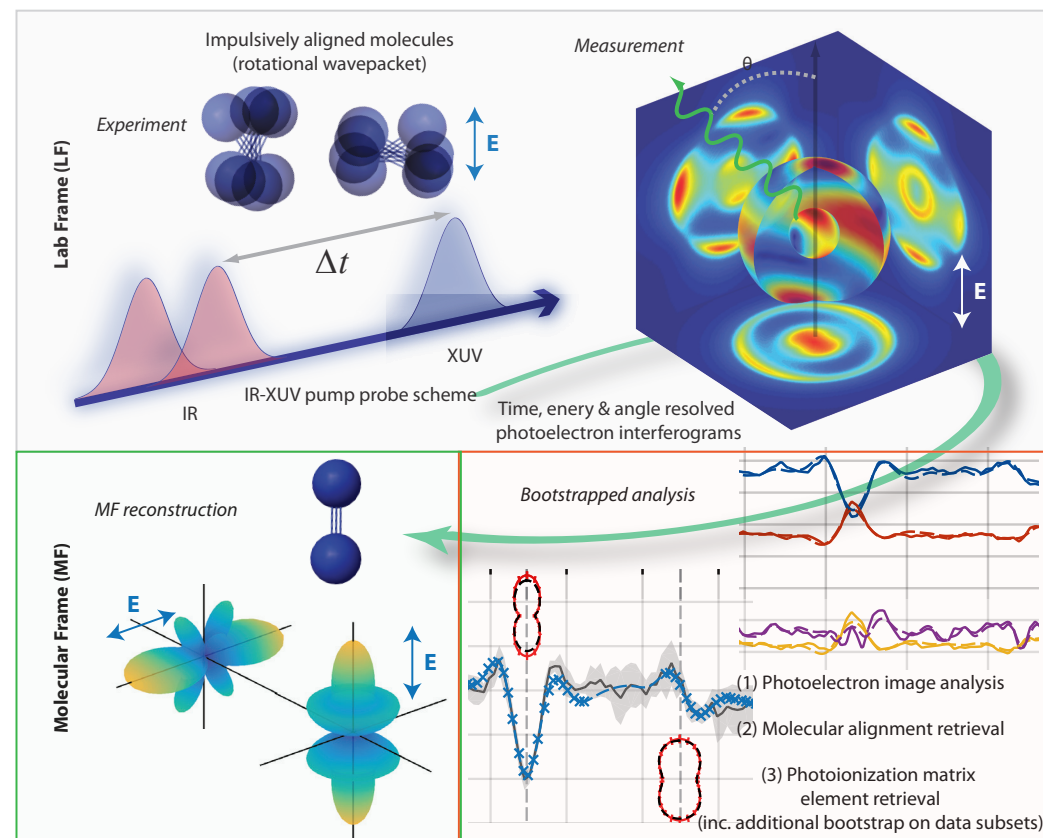
<http://www.chem.tamu.edu/rgroup/lucchese/ePolyScat.E3.manual/manual.html>





# summary

- Photoelectron metrology
- High information content measurements with rotational wavepacket.
- Bootstrapping analysis protocol:
  - Rotational wavepacket reconstruction.
  - Photoionization dynamics retrieval.
- Demonstrated for  $N_2$ , three different energies/final states.
- Molecular frame retrieval from laboratory frame measurements.



Quantitative photoelectron state reconstruction for “general” molecular photoionization is feasible with rotational wavepacket measurements and bootstrapping protocol...?

OK for symmetric tops... for asymmetric tops much work still to do!

For further discussion, see refs in abstract.

**[1] Molecular Frame Reconstruction Using Time-Domain Photoionization Interferometry.**

Marceau, C., Makhija, V., Platzer, D., Naumov, A. Y., Corkum, P. B., Stolow, A., Villeneuve, D. M., Hockett, P. (2017). Physical Review Letters, 119(8), 83401. <http://doi.org/10.1103/PhysRevLett.119.083401>

**[2] Coherent control of photoelectron wavepacket angular interferograms.**

Hockett, P., Wollenhaupt, M., & Baumert, T. (2015). Journal of Physics B: Atomic, Molecular and Optical Physics, 48(21), 214004. <http://doi.org/10.1088/0953-4075/48/21/214004>

**[3] Complete Photoionization Experiments via Ultrafast Coherent Control with Polarization Multiplexing.**

Hockett, P., Wollenhaupt, M., Lux, C., & Baumert, T. (2014). Physical Review Letters, 112(22), 223001. <http://doi.org/10.1103/PhysRevLett.112.223001>

**[4] Coherent imaging of an attosecond electron wave packet. (RABBIT based)**

Villeneuve, D. M., Hockett, P., Vrakking, M. J. J., & Niikura, H. (2017). Science, 356(6343), 1150–1153. <http://doi.org/10.1126/science.aam8393>



# acknowledgements

## NRC

Claude Marceau

Varun Makhija

Ruaridh Forbes

Rune Lausten

Albert Stolow

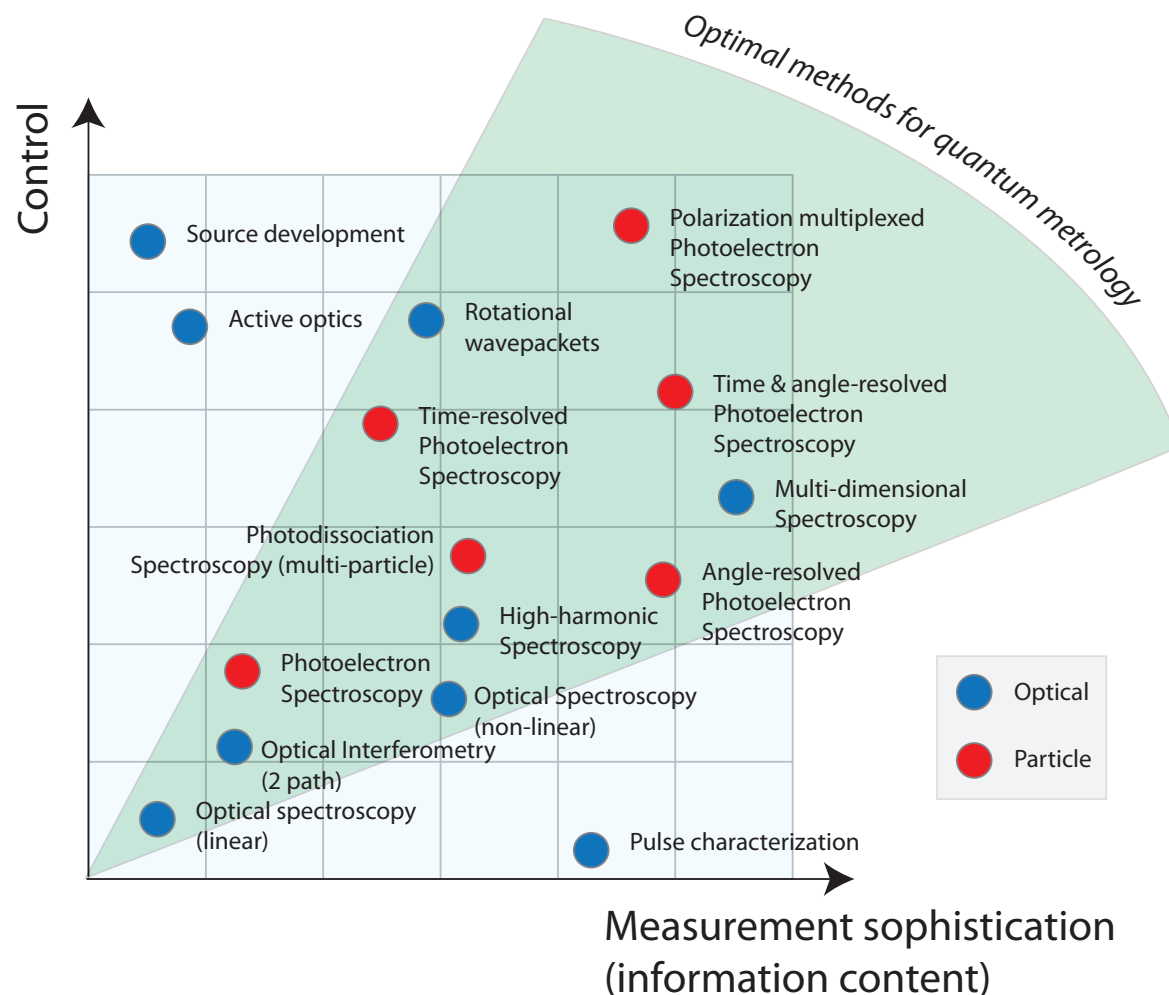
David Villeneuve

Paul Corkum

& everyone else at NRC!

## Texas A&M/LBNL

Robert R. Lucchese (ePolyScat)



# for more information...

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**Slides available via Figshare, DOI: [10.6084/m9.figshare.5645509](https://doi.org/10.6084/m9.figshare.5645509)**

arXiv: [http://arxiv.org/a/hockett\\_p\\_1.html](http://arxiv.org/a/hockett_p_1.html)

Figshare: [http://figshare.com/authors/Paul\\_Hockett/100955](http://figshare.com/authors/Paul_Hockett/100955)

Orcid: <http://orcid.org/0000-0001-9561-8433>

Scholar: <https://scholar.google.ca/citations?user=e4FgTYMAAAAJ>

Web: [www.femtolab.ca](http://www.femtolab.ca)

***Coming soon:***

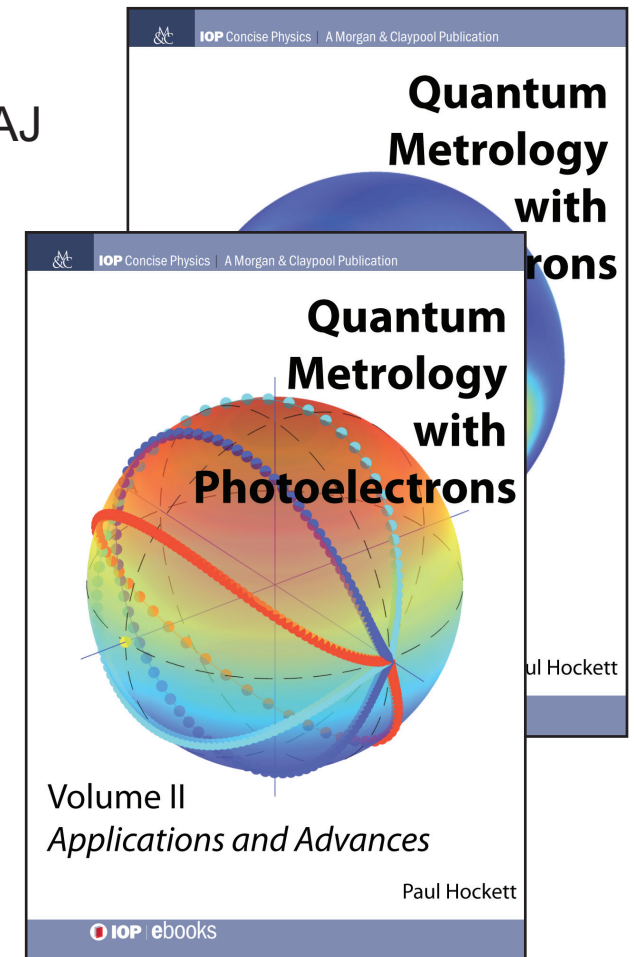
**Quantum Metrology with Photoelectrons**

*New book for the IOP Concise series, due 2018*

**<https://osf.io/q2v3g/>**



[paul.hockett@nrc.ca](mailto:paul.hockett@nrc.ca)



***femtolab.ca***



# where are we



*NRC, 100 Sussex Drive,  
Ottawa, ON, Canada*

*Web: femtolab.ca*

We're always interested in new  
collaborations and new directions...

If you have an idea, or work that  
could benefit from our expertise and  
facilities...

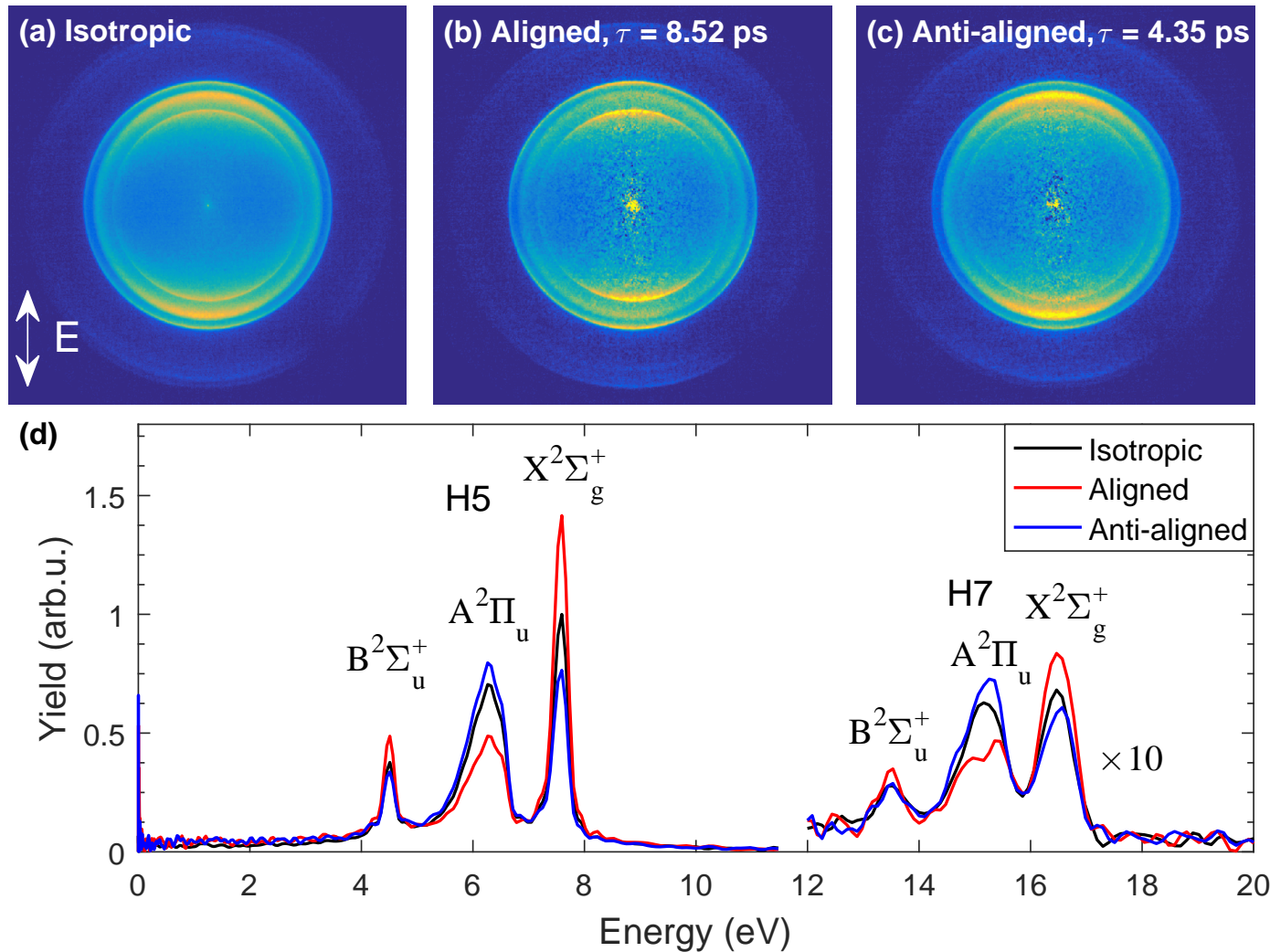
*...please get in touch!*



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# N<sub>2</sub> measurements summary

- 267nm driving field
- Two-pulse IR rotational wavepacket preparation
- 150 temporal steps, -0.5 - +9.5 ps



H5 = 23.3 eV

H7 = 32.6 eV





# details: alignment

## Notes from Varun's thesis

Laser-induced rotational dynamics as a route to molecular frame measurements

<http://krex.k-state.edu/dspace/handle/2097/18522>

where  $\chi$  becomes the azimuthal angle of the laser polarization vector. Since the Wigner functions  $D_{m,k}^j(\theta, \phi, \chi)$  are an irreducible representation on the rotation group  $SO(3)$ <sup>52</sup> the angle dependent ion yield can be expanded as

$$S(\theta, \chi) = \sum_{j,k} C_{j,k} D_{0,k}^j(\theta, \chi), \quad (5.1)$$

$$S(\theta, \chi) = \frac{dW}{d\hat{\Omega}} = \sum_{j,k} C_{j,k} D_{0,k}^j(\theta, \chi),$$

$$C_{j,k} = \sum_{l,m,\lambda,\lambda'} \langle l, -m; l, m | j, 0 \rangle \langle l, -\lambda; l, \lambda' | j, k \rangle A_{l,\lambda} A_{l,\lambda'} d_{l,m}, \quad (5.5)$$

$$S(t) = \int \rho(\theta, \chi, t) S(\theta, \chi) \sin \theta d\theta d\chi = \sum_{jk} C_{j,k} \int \rho(\theta, \chi, t) D_{0,k}^j \sin \theta d\theta d\chi = \sum_{jk} C_{j,k} \langle D_{0,k}^j \rangle(t). \quad (5.7)$$

Measured time-dependent signal

Fitted

Calculated from rotational wavepacket simulations  
Function of laser parameters & rotational temperature

**Determining the alignment  
Analysis by Varun Makhija**



<https://dx.doi.org/10.6084/m9.figshare.4480349>.

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# details: photoionization

Use known ADMs to determine the unknown dipole matrix elements. Everything else is angular momentum coupling and symmetry parameters; complicated, but analytical.

ADMs from Varun's fit

$$\begin{aligned}
 \beta_{L,M}(t) &= (2L + 1)^{1/2} \sum_P (-1)^P \begin{pmatrix} 1 & 1 & P \\ p & -p & R \end{pmatrix} e_{-p} e_{-p}^* \\
 &\times \sum_K \sum_Q (2K + 1)^{1/2} \begin{pmatrix} P & K & L \\ Q - M & -Q & M \end{pmatrix} A_{K,-Q}(t) \\
 &\times \sum_{q,q'} (-1)_{q'} \begin{pmatrix} 1 & 1 & P \\ q & -q' & q' - q \end{pmatrix} \begin{pmatrix} P & K & L \\ q - q' & q' - q & 0 \end{pmatrix} \\
 &\times \sum_{l,l'} \sum_{\lambda,\lambda'} (-1)^{\lambda'} (2l + 1)^{1/2} (2l' + 1)^{1/2} \begin{pmatrix} l & l' & L \\ \lambda & -\lambda' & M \end{pmatrix} \begin{pmatrix} l & l' & L \\ 0 & 0 & 0 \end{pmatrix} \\
 &\times (-i)^{l'-l} \sum_{\Gamma,\Gamma'} \sum_{\mu,\mu'} \sum_{h,h'} b_{hl\lambda}^{\Gamma\mu*} b_{h'l'\lambda'}^{\Gamma'\mu'} \mathbf{D}_{hl}^{\Gamma\mu*}(q) \mathbf{D}_{h'l'}^{\Gamma'\mu'}(q').
 \end{aligned}$$

Measured angular parameters

Matrix elements to determine

See *General phenomenology of ionization from aligned molecular ensembles* (Hockett, NJP, 17 023069 2015) for details.



<https://dx.doi.org/10.6084/m9.figshare.4480349>.

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# details: matrix elements

| $\Gamma$   | $q$     | $h$ | $\mu$ | $l$ | $m$     | $ D_{hl}^{\Gamma\mu}(q) $ | $\arg(D_{hl}^{\Gamma\mu}(q))$ | $b_{hl\lambda}^{\Gamma\mu}$ | Relations   |
|------------|---------|-----|-------|-----|---------|---------------------------|-------------------------------|-----------------------------|---|
| $\sigma_u$ | 0       | 1   | 1     | 1   | 0       | 0.53(2)                   | 0*                            | 1                           | -   |
|            |         |     |       | 3   | 0       | 0.41(2)                   | 1.1(1)                        | 1                           | -   |
|            |         |     |       | 5   | 0       | 0.49(2)                   | 1.3(4)                        | 1                           | -   |
| $\pi_u$    | $\pm 1$ | 1   | 1     | 1   | $\pm 1$ | 0.19(3)                   | -1.4(1)                       | $1/\sqrt{2}$                | $q : D_{hl}^{\pi_u\mu}(+1) = D_{hl}^{\pi_u\mu}(-1)$ |
|            |         |     |       | 3   | $\pm 1$ | 0.17(3)                   | 0(1)                          | $1/\sqrt{2}$                |   |
|            |         |     |       | 5   | $\pm 1$ | 0.30(2)                   | -1.6(9)                       | $1/\sqrt{2}$                |   |

Table 11.1: Symmetrized matrix elements,  $X^2\Sigma_g^+$ . The sum over all moduli squared are normalized to unity,  $\sum |D_{hl}^{\Gamma\mu}(q)/b_{hl\lambda}^{\Gamma\mu}|^2 = 1$ . \* reference phase, set to zero. Values in parentheses indicate the uncertainty in the final digit.

| $\Gamma$   | $q$     | $h$ | $\mu$ | $l$ | $m$     | $ D_{hl}^{\Gamma\mu}(q) $ | $\arg(D_{hl}^{\Gamma\mu}(q))$ | $b_{hl\lambda}^{\Gamma\mu}$ | Relations   |
|------------|---------|-----|-------|-----|---------|---------------------------|-------------------------------|-----------------------------|---|
| $\sigma_g$ | $\pm 1$ | 1   | 1,2   | 0   | 0       | 0.58(3)                   | 0*                            | $1/\sqrt{2}$                | $q(\mu=1) : D_{hl}^{\sigma_g^1}(+1) = D_{hl}^{\sigma_g^1}(-1)$                                  |
|            |         |     |       |     |         |                           |                               |                             | $q(\mu=2) : D_{hl}^{\sigma_g^2}(+1) = -D_{hl}^{\sigma_g^2}(-1)$                                 |
|            |         |     |       |     |         |                           |                               |                             | $\mu : D_{hl}^{\sigma_g^2}(+1) = \Im[D_{hl}^{\sigma_g^1}(+1)] - i\Re[D_{hl}^{\sigma_g^1}(+1)]$  |
|            |         |     |       | 2   | 0       | 0.23(6)                   | 0.3(12)                       | $1/\sqrt{2}$                |   |
|            |         |     |       | 4   | 0       | 0.15(7)                   | -0.5(9)                       | $1/\sqrt{2}$                |   |
| $\delta_g$ | $\pm 1$ | 1   | 1,2   | 2   | $\mp 2$ | 0.15(7)                   | -0.5(2)                       | $1/\sqrt{2}$                | $q(\mu=1) : D_{hl}^{\delta_g^1}(+1) = D_{hl}^{\delta_g^1}(-1)$                                  |
|            |         |     |       |     |         |                           |                               |                             | $q(\mu=2) : D_{hl}^{\delta_g^2}(+1) = -D_{hl}^{\delta_g^2}(-1)$                                 |
|            |         |     |       |     |         |                           |                               |                             | $\mu : D_{hl}^{\delta_g^2}(+1) = -\Im[D_{hl}^{\delta_g^1}(+1)] + i\Re[D_{hl}^{\delta_g^1}(+1)]$ |
|            |         |     |       | 4   | $\mp 2$ | 0.22(6)                   | -0.6(8)                       | $1/\sqrt{2}$                |   |
|            |         |     |       |     |         |                           |                               |                             |   |
| $\pi_g$    | 0       | 1,2 | 1,2   | 2   | $\pm 1$ | 0.15(5)                   | -0.3(30)                      | $1/\sqrt{2}$                | $h(\mu=1) : D_{1l}^{\pi_g^1}(0) = D_{2l}^{\pi_g^1}(0)$  |
|            |         |     |       |     |         |                           |                               |                             | $h(\mu=2) : D_{1l}^{\pi_g^2}(0) = -D_{2l}^{\pi_g^2}(0)$   |
|            |         |     |       |     |         |                           |                               |                             | $\mu : D_{hl}^{\pi_g^2}(0) = \Im[D_{hl}^{\pi_g^1}(0)] - i\Re[D_{hl}^{\pi_g^1}(0)]$              |
|            |         |     |       | 4   | $\pm 1$ | 0.05(9)                   | 0.6(30)                       | $1/\sqrt{2}$                |   |
|            |         |     |       |     |         |                           |                               |                             |   |

Table 11.2: Symmetrized matrix elements,  $A^2\Pi_u$ . The sum over all moduli squared are normalized to unity,  $\sum |D_{hl}^{\Gamma\mu}(q)/b_{hl\lambda}^{\Gamma\mu}|^2 = 1$ . \* reference phase, set to zero. Values in parentheses indicate the uncertainty in the final digit.

| $\Gamma$   | $q$     | $h$ | $\mu$ | $l$ | $m$     | $ D_{hl}^{\Gamma\mu}(q) $ | $\arg(D_{hl}^{\Gamma\mu}(q))$ | $b_{hl\lambda}^{\Gamma\mu}$ | Relations   |
|------------|---------|-----|-------|-----|---------|---------------------------|-------------------------------|-----------------------------|---|
| $\sigma_g$ | 0       | 1   | 1     | 0   | 0       | 0.08(21)                  | 0*                            | 1                           | -   |
|            |         |     |       | 2   | 0       | 0.19(9)                   | -1.0(13)                      | 1                           | -   |
|            |         |     |       | 4   | 0       | 0.65(4)                   | -1.6(19)                      | 1                           | -   |
| $\pi_g$    | $\pm 1$ | 1   | 1     | 2   | $\mp 1$ | 0.01(12)                  | -3.5(35)                      | $1/\sqrt{2}$                | $q : D_{hl}^{\pi_u\mu}(+1) = D_{hl}^{\pi_u\mu}(-1)$ |
|            |         |     |       | 4   | $\mp 1$ | 0.52(3)                   | 0.4(13)                       |                             |   |

Table 11.3: Symmetrized matrix elements,  $B^2\Sigma_u^+$ . The sum over all moduli squared are normalized to unity,  $\sum |D_{hl}^{\Gamma\mu}(q)/b_{hl\lambda}^{\Gamma\mu}|^2 = 1$ . \* reference phase, set to zero. Values in parentheses indicate the uncertainty in the final digit.

