

Appendix B: semi-discrete model notation and description

Combining the continuous system (1) with the discrete disturbances (2) from the main text leads to the semi-discrete model

$$\begin{aligned}
 \frac{dR}{dt} &= r_A A (1 - R - A - M) - aR - r_M R M - d_R R & t \neq \tau \\
 \frac{dA}{dt} &= aR + gA (1 - R - A - M) - \beta A M - d_A A & t \neq \tau \\
 \frac{dM}{dt} &= r_M M (1 - R - A - M) + r_M R M + \beta A M - h_b M - h_s M \frac{\omega A}{1 + \omega A} & t \neq \tau \\
 R(\tau^+) &= (1 - \gamma(\tau)) R(\tau) \\
 A(\tau^+) &= (1 - \gamma(\tau)) A(\tau) \\
 M(\tau^+) &= M(\tau).
 \end{aligned} \tag{B.1}$$

where τ are time steps with bleaching events and τ^+ are the instants following bleaching events.