

An interesting pattern of primes

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If you observe below there is a correlation between x and y . x will always be a positive even number and y will always be a positive odd number and its subtraction will give 7 until a certain prime number and there after it will be a different correlation where the result is 8 and after a while it will be 9 and so on. Later i will repost its new correlation, for now it is enough to see that this pattern holds until the 1062 nd prime.

mathematica

(Defining the ordered pairs)

```
pairs = {{8, 1}, {10, 3}, {12, 5}, {14, 7}, {16, 9}, {18, 11}, {20, 13}, {22, 15}, {24, 17}, {26, 19}, {28, 21}, {30, 23}};
```

(Function to verify if a is prime)

```
isPrimeZ[x_, y_] := Module[{z},  
  z = 7000 + 914 + y;  
  z == 7907 + x && PrimeQ[z]  
];
```

(Filttering the pairs that satisfy the condition)

```
results = Select[pairs, isPrimeZ[#[[1]], #[[2]]] &];
```

(Exhibiting the results)

```
results
```

```
{{12,5}, {20,13}, {26,19}, {30,23}}
```

mathematica

(Defining the ordered pairs)

```
pairs =  
{{10,2},{12,4},{14,6},{16,8},{18,10},{20,12},{22,14},{24,16},{26,18},{28,20},{30,22},  
{32,24},{34,26},{36,28},{38,30},{40,32},{42,34},{44,36},{46,38},{48,40},{50,42},{  
52,44},{54,46},{56,48},{58,50},{60,52},{62,54},{64,56},{66,58},{68,60},{70,62},{72,64},  
{74,66},{76,68},{78,70},{80,72},{82,74},{84,76},{86,78},{88,80},{90,82}};
```

(Function to verify if a is prime)

```
isPrimeZ[x_, y_] := Module[{z},  
  z = 16000 + 1395 + y;  
  z == 17387 + x && PrimeQ[z]  
];
```

(Filttering the pairs that satisfy the condition)

```
results = Select[pairs, isPrimeZ[#[[1]], #[[2]]] &];
```

(Exhibiting the results)
Results

RULE 1

{{14,6},{30,22},{32,24},{44,36},{56,48},{62,54},{80,72},{84,76},{90,82}}

mathematica

```
AS=Cases[Tuples[Range[190],2],{p_,i_}/;EvenQ@p && OddQ@i && p-i==7]
```

(Defining the ordered pairs)

```
pairs = AS;
```

(Function to verify if a is prime)

```
isPrimeZ[x_, y_] := Module[{z},
```

```
z = 7000 + 914 + y;
```

```
z == 7907 + x && PrimeQ[z]
```

```
];
```

(Filtering the pairs that satisfy the condition)

```
results = Select[pairs, isPrimeZ#[[1]], #[[2]] &];
```

(Exhibiting the results)

results

```
po = results[[All, 1]]
```

```
Differences[%]
```

```
pp=results[[All, 2]]
```

```
pc=pairs[[All,1]]
```

```
ListLinePlot[results]
```

```
a=ListLinePlot[po,PlotStyle->Red]
```

```
b=ListLinePlot[pp,PlotStyle->Green]
```

```
d=ListLinePlot[pc,PlotStyle->Blue]
```

```
c=Show[a,b,d]
```

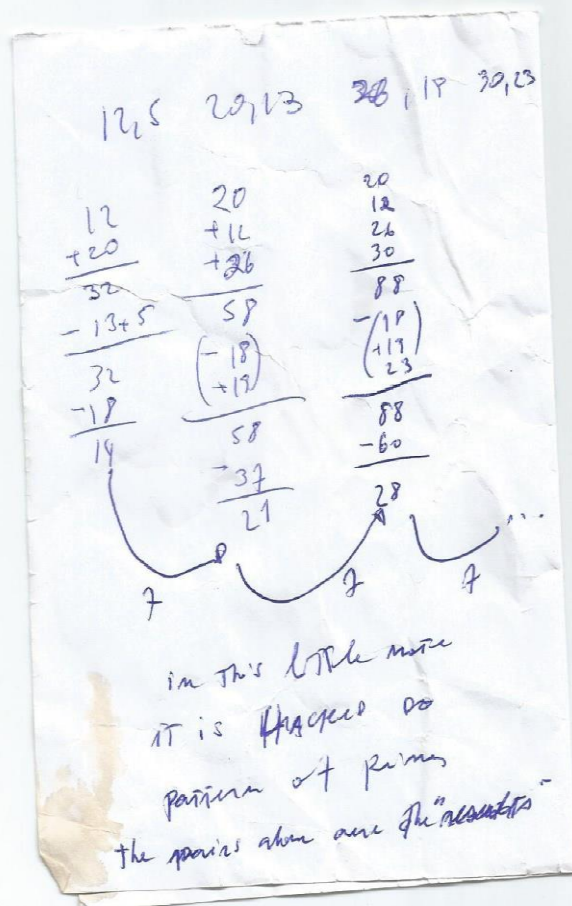
{{12,5},{20,13},{26,19},{30,23},{42,35},{44,37},{56,49},{86,79},{102,95},{104,97},
{110,103},{132,125},{146,139},{152,145},{162,155},{174,167},{180,173},{182,175},
{186,179}}

{12,20,26,30,42,44,56,86,102,104,110,132,146,152,162,174,180,182,186}
{8,6,4,12,2,12,30,16,2,6,22,14,6,10,12,6,2,4} THE DISTANCE BETWEEN
EVERY ORDERED PAIR THAT GIVES A PRIME GIVES BY SUM THE NEXT
ODD NUMBER IN THE PAIRS
{5,13,19,23,35,37,49,79,95,97,103,125,139,145,155,167,173,175,179}

8+5=13 ,13+6=19,19+4=23,23+12=35 AND SO ON

AND FINALLY WRITTEN IN PORTUGUESE AND FOR THE SAKE OF
IDENTITY THE CONJECTURE THAT SEEMS TO HOLD TRUE :

$\{\{12,5\},\{20,13\},\{26,19\},\{30,23\},\{42,35\},\{44,37\},\{56,49\},\{86,79\},\{102,95\},\{104,97\},$
 $\{110,103\},\{132,125\},\{146,139\},\{152,145\},\{162,155\},\{174,167\},\{180,173\},\{182,17$
 $5\},\{186,179\}\}$ a Soma consecutiva dos pares dos pares ordenados menos a
soma consecutiva dos impares progressivamente dá múltiplos consecutivos de
7....



pairs={ {12,5}, {20,13}, {26,19}, {30,23}, {42,35}, {44,37}, {56,49}, {86,79}, {102,95}, {104,97}, {110,103}, {132,125}, {146,139}, {152,145}, {162,155}, {174,167}, {180,173}, {182,175}, {186,179}, {194,187}, {

```
204,197},{210,203},{216,209},{240,233},{254,247},{260,253},{264,257},{272,265},{284,277},{30
2,295},{312,305},{314,307},{324,317},{326,319},{330,323},{336,329},{356,349},{362,355},{366,
359},{380,373},{384,377},{386,379},{390,383},{404,397},{410,403},{422,415},{446,439},{456,44
9},{462,455},{470,463},{480,473},{482,475}}
```

```
list = pairs[[All, 1]]
```

```
list2=pairs[[All,2]]
```

```
list3=Drop[list2,2]
```

```
pairs = Table[{list[[i]], list[[i + 2]]}, {i, 1, Length[list] - 2}];
```

```
sums = Map[Total, pairs];
```

```
sums
```

```
division=sums/2
```

```
list3-division
```

```
PrimeQ[list2]
```

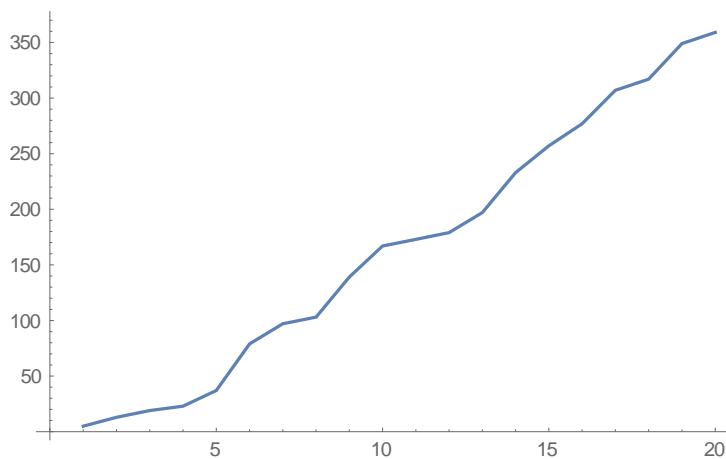
```
a=Select[list2,PrimeQ,(20)]
```

```
ListLinePlot[a]
```

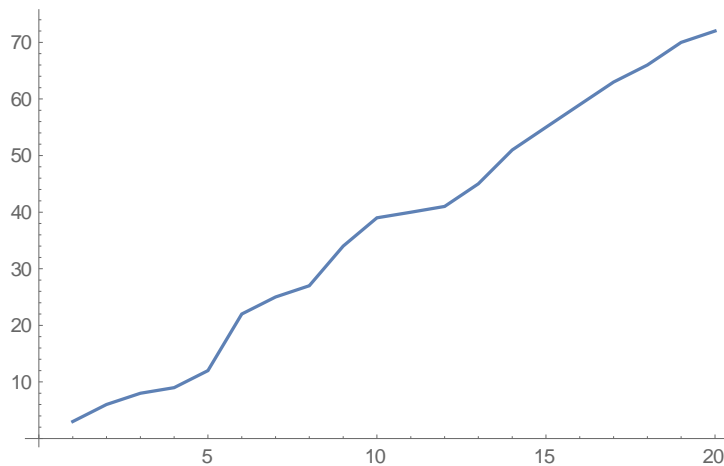
```
PrimePi[a]
```

```
ListLinePlot[%]
```

```
{5,13,19,23,37,79,97,103,139,167,173,179,197,233,257,277,307,317,349,359}
```



```
{3,6,8,9,12,22,25,27,34,39,40,41,45,51,55,59,63,66,70,72}
```



```
pairs={{12,5},{20,13},{26,19},{30,23},{42,35},{44,37},{56,49},{86,79},{102,95},{104,97},{110,103},
{132,125},{146,139},{152,145},{162,155},{174,167},{180,173},{182,175},{186,179},{194,187},{
204,197},{210,203},{216,209},{240,233},{254,247},{260,253},{264,257},{272,265},{284,277},{30
2,295},{312,305},{314,307},{324,317},{326,319},{330,323},{336,329},{356,349},{362,355},{366,
359},{380,373},{384,377},{386,379},{390,383},{404,397},{410,403},{422,415},{446,439},{456,44
9},{462,455},{470,463},{480,473},{482,475},{512,505},{516,509},{522,515},{524,517},{536,529},
{540,533},{554,547},{560,553},{594,587}}
```

```
list = pairs[[All, 1]]
```

```
list2=pairs[[All,2]]
```

```
list3=Drop[list2,2]
```

```
pairs = Table[{list[[i]], list[[i + 2]]}, {i, 1, Length[list] - 2}];
```

```
sums = Map[Total, pairs];
```

```
sums
```

```
division=sums/2
```

```
list3-division
```

```
PrimeQ[list2]
```

```
a=Select[list2,PrimeQ,(60)]
```

```
ListLinePlot[a] 1)
```

```
PrimePi[a]
```

```
ListLinePlot[%] 2)
```

```
series =
```

```
{3,6,8,9,12,22,25,27,34,39,40,41,45,51,55,59,63,66,70,72,74,75,76,78,85,87,90,97,101,107}
```

```
pairs = Table[series[[i]] + series[[Length[series] - i + 1]], {i, 1, Floor[Length[series]/2]]
```

```
ListLinePlot[pairs]
```

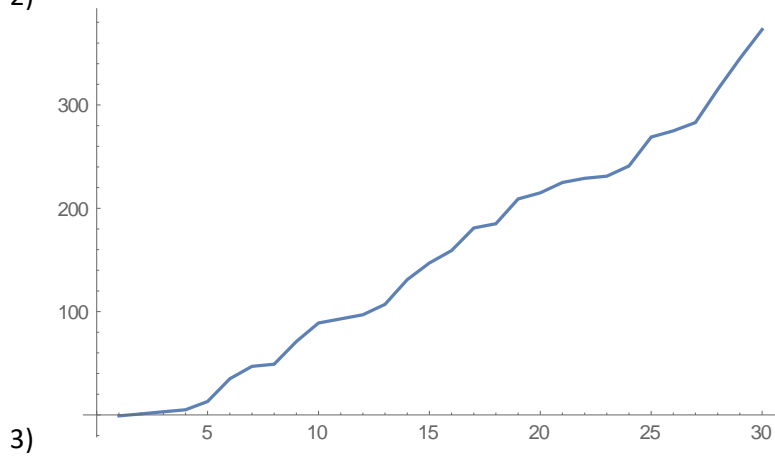
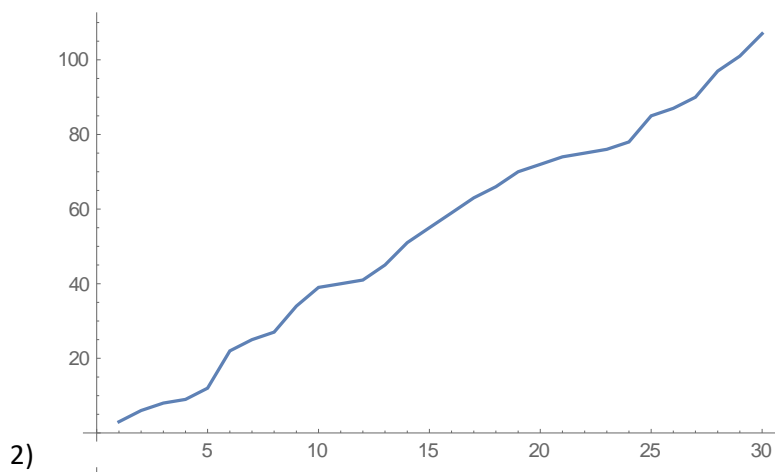
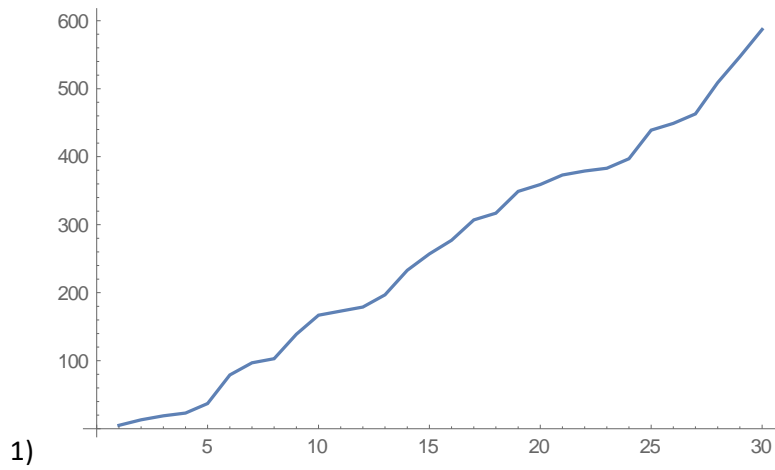
```
po = Table[pairs[[i]] + pairs[[Length[pairs] - i + 1]], {i, 1, Floor[Length[pairs]/2]]
```

```
ListLinePlot[pairs]
```

```
de=a-(series*2)
```

```
PrimeQ[de]
```

```
ListLinePlot[de] 3)
```



The following program algorithm checks if there is other forms of pairs that satisfy a certain pattern: Please use a translator to convert the texts in to english as it was originally formulated in portuguese.

```
(* Definindo os pares ordenados *)
```

```
pairs = {{12, 5}, {20, 13}, {26, 19}, {30, 23}, {42, 35}, {44, 37}, {56, 49}, {86, 79}, {102, 95}, {104, 97}};
```

```
(* Função para verificar a propriedade *)verificarPropriedade[pairs_List] := Module[{n, i, par1, impar1, par2, impar2, soma1, soma2, resultado}, n = Length[pairs];
```

```
resultado = True; For[i = 1, i <= Floor[n/2], i++, par1 = pairs[[i, 1]]; impar1 = pairs[[i, 2]]; par2 = pairs[[n - i + 1, 1]];
```

```
impar2 = pairs[[n - i + 1, 2]];
```

```
soma1 = par1 + impar2;
```

```
soma2 = impar1 + par2;
```

```
If[soma1 != soma2, resultado = False; Break[ ]; ]; resultado]
```

```
(* Verificando a propriedade *)verificarPropriedade[pairs]
```

```
True
```

PROGRAM 2

```
pairs = {{12, 5}, {20, 13}, {26, 19}, {30, 23}, {42, 35}, {44, 37}, {56, 49}, {86, 79}, {102, 95}, {104, 97}};
```

```
(* Função para verificar a propriedade *)verificarPropriedade[pairs_List] := Module[{n, i, par1, impar1, par2, impar2, soma1, soma2, resultado}, n = Length[pairs];
```

```
resultado = True;
```

```
For[i = 1, i <= Floor[n/2], i++, par1 = pairs[[i, 1]]; impar1 = pairs[[i, 2]]; par2 = pairs[[n - i + 1, 1]];
```

```
impar2 = pairs[[n - i + 1, 2]];
```

```
soma1 = par1 + impar2;
```

```
soma2 = impar1 + par2;
```

```
If[soma1 != soma2, resultado = False; Break[ ]; ]; resultado]
```

```
(* Verificando a propriedade *)verificarPropriedade[pairs]
```



```
(* Modificando os pares para garantir somas únicas *)modificarPares[pairs_List] := Module[{n,
i, novoPar}, n = Length[pairs]; Table[ novoPar = {pairs[[i, 1]], pairs[[i, 2]]};
While[MemberQ[Table[pairs[[j, 1]] + pairs[[n - j + 1, 2]], {j, 1, Floor[n/2]}], novoPar[[1]] +
novoPar[[2]]], novoPar = {novoPar[[1]] + 2, novoPar[[2]] + 2}; ]; novoPar, {i, 1, n} ]]
```

```
(* Modificando os pares *)paresModificados = modificarPares[pairs];
```

```
(* Verificando a propriedade nos pares modificados *)
```

```
verificarPropriedade(paresModificados)
```

```
(* Exibindo os pares modificados *)paresModificados
```

```
True
```

```
{{12 verificarPropriedade,5 verificarPropriedade},{20 verificarPropriedade,13
verificarPropriedade},{26 verificarPropriedade,19 verificarPropriedade},{30
verificarPropriedade,23 verificarPropriedade},{42 verificarPropriedade,35
verificarPropriedade},{44 verificarPropriedade,37 verificarPropriedade},{60
verificarPropriedade,53 verificarPropriedade},{86 verificarPropriedade,79
verificarPropriedade},{102 verificarPropriedade,95 verificarPropriedade},{104
verificarPropriedade,97 verificarPropriedade}}

{{12,5},{20,13},{26,19},{30,23},{42,35},{44,37},{60,53},{86,79},{102,95},{104,97}}
```

```
nn = Range[1, 10000000];n = Select[nn, PrimeQ, {1000}];
```

```
k = (n^2) - 1 + n + (2 - 4 n);d = n^4 - 1 + n^2;c = n^3 + 2;e = Mod[c, 3];
```

```
f = Mod[d, 3];
```

```
g = Mod[k, 3];
```

```
h = Mod[c, 7];
```

```
i = Mod[d, 7];
```

```
j = Mod[k, 7];
```

```
l = Mod[c, 4];
```

```
m = Mod[d, 4];
```

```
o = Mod[k, 4];
```

```
r = Mod[c, 5];
```

```
s = Mod[d, 5];
```

```
t = Mod[k, 5];
```

```
QQ = Transpose[{e, f, g, h, i, j, l, m, o, r, s, t}];
```

```
validNumbers = Select[Range[7963, 8050], Module[{n2 = #, k1, d1, c1, e1, f1, g1, h1, i1, j1, l1,
m1, o1, r1, s1, t1, pp1}, k1 = (n2^2) - 1 + n2 + (2 - 4 n2);
```

```
d1 = n2^4 - 1 + n2^2;
```

```

c1 = n2^3 + 2;
e1 = Mod[c1, 3];
f1 = Mod[d1, 3];
g1 = Mod[k1, 3];
h1 = Mod[c1, 7];
i1 = Mod[d1, 7];
j1 = Mod[k1, 7];
l1 = Mod[c1, 4];
m1 = Mod[d1, 4];
o1 = Mod[k1, 4];
r1 = Mod[c1, 5];
s1 = Mod[d1, 5];
t1 = Mod[k1, 5];
pp1 = {e1, f1, g1, h1, i1, j1, l1, m1, o1, r1, s1, t1};
MemberQ[QQ, pp1] ] &];
validNumbers

```

```

oddNumbers = Select[validNumbers, OddQ];
validNumbers = Select[oddNumbers, Mod[2^#, #] == 2 &];

```

```

validNumbers

```

```

{7963,7967,7969,7979,7981,7982,7983,7985,7987,7991,7993,7997,7999,8003,8009,8011,801
7,8021,8023,8027,8033,8039,8041,8047}
{7963,7993,8009,8011,8017,8039}

```

```

nn = Range[1, 10000000];ng=Select[nn,OddQ,(5000)];n = Select[ng, CompositeQ, (1000)];
k = (n^2) - 1 + n + (2 - 4 n);d = n^4 - 1 + n^2;c = n^3 + 2;e = Mod[c, 3];
f = Mod[d, 3];
g = Mod[k, 3];

```

```

h = Mod[c, 7];
i = Mod[d, 7];
j = Mod[k, 7];
l = Mod[c, 4];
m = Mod[d, 4];
o = Mod[k, 4];
r = Mod[c, 5];
s = Mod[d, 5];
t = Mod[k, 5];

QQ = Transpose[{e, f, g, h, i, j, l, m, o, r, s, t}];

validNumbers = Select[Range[7963, 8050], Module[{n2 = #, k1, d1, c1, e1, f1, g1, h1, i1, j1, l1,
m1, o1, r1, s1, t1, pp1}, k1 = (n2^2) - 1 + n2 + (2 - 4 n2);

d1 = n2^4 - 1 + n2^2;
c1 = n2^3 + 2;
e1 = Mod[c1, 3];
f1 = Mod[d1, 3];
g1 = Mod[k1, 3];
h1 = Mod[c1, 7];
i1 = Mod[d1, 7];
j1 = Mod[k1, 7];
l1 = Mod[c1, 4];
m1 = Mod[d1, 4];
o1 = Mod[k1, 4];
r1 = Mod[c1, 5];
s1 = Mod[d1, 5];
t1 = Mod[k1, 5];

pp1 = {e1, f1, g1, h1, i1, j1, l1, m1, o1, r1, s1, t1};

MemberQ[QQ, pp1] ] &];

validNumbers

oddNumbers1 = Select[validNumbers, OddQ];

```

```
validNumbers = Select[oddNumbers1, Mod[2^#, #] == 2 &];
```

```
validNumbers
```

```
nn = Range[1, 10000000]; n = Select[nn, PrimeQ, {1000}];
```

```
k = (n^2) - 1 + n + (2 - 4 n); d = n^4 - 1 + n^2; c = n^3 + 2; e = Mod[c, 3];
```

```
f = Mod[d, 3];
```

```
g = Mod[k, 3];
```

```
h = Mod[c, 7];
```

```
i = Mod[d, 7];
```

```
j = Mod[k, 7];
```

```
l = Mod[c, 4];
```

```
m = Mod[d, 4];
```

```
o = Mod[k, 4];
```

```
r = Mod[c, 5];
```

```
s = Mod[d, 5];
```

```
t = Mod[k, 5];
```

```
QQ = Transpose[{e, f, g, h, i, j, l, m, o, r, s, t}];
```

```
validNumbers = Select[Range[7963, 8050], Module[{n2 = #, k1, d1, c1, e1, f1, g1, h1, i1, j1, l1, m1, o1, r1, s1, t1, pp1}, k1 = (n2^2) - 1 + n2 + (2 - 4 n2);
```

```
d1 = n2^4 - 1 + n2^2;
```

```
c1 = n2^3 + 2;
```

```
e1 = Mod[c1, 3];
```

```
f1 = Mod[d1, 3];
```

```
g1 = Mod[k1, 3];
```

```
h1 = Mod[c1, 7];
```

```
i1 = Mod[d1, 7];
```

```
j1 = Mod[k1, 7];
```

```
l1 = Mod[c1, 4];
```

```
m1 = Mod[d1, 4];
```

```
o1 = Mod[k1, 4];
```

```
r1 = Mod[c1, 5];
```

```

s1 = Mod[d1, 5];
t1 = Mod[k1, 5];
pp1 = {e1, f1, g1, h1, i1, j1, l1, m1, o1, r1, s1, t1};
MemberQ[QQ, pp1] ] &];
validNumbers

```

```

oddNumbers = Select[validNumbers, OddQ];
validNumbers = Select[oddNumbers, Mod[2^#, #] == 2 &];

```

```

validNumbers
validNumbers2=Intersection[oddNumbers,oddNumbers1]
validNumbers = Select[validNumbers2, Mod[2^#, #] == 2 &]
validNumbers

```

```

{7963,7965,7967,7969,7971,7973,7975,7977,7979,7981,7983,7985,7987,7989,7991,7993,799
5,7997,7999,8001,8003,8005,8007,8009,8011,8013,8015,8017,8019,8021,8023,8025,8027,80
29,8031,8033,8035,8037,8039,8041,8043,8045,8047,8049}

```

```

{7963,7993,8009,8011,8017,8039}

```

```

{7963,7967,7969,7979,7981,7982,7983,7985,7987,7991,7993,7997,7999,8003,8009,8011,801
7,8021,8023,8027,8033,8039,8041,8047}

```

```

{7963,7993,8009,8011,8017,8039}

```

```

{7963,7967,7969,7979,7981,7983,7985,7987,7991,7993,7997,7999,8003,8009,8011,8017,802
1,8023,8027,8033,8039,8041,8047}

```

```

{7963,7993,8009,8011,8017,8039}

```

Now observe the following sequence of pairs that satisfy the rule established in **RULE 1**

```

pairs = {{12, 5}, {20, 13}, {26, 19}, {30, 23}, {42, 35}, {44, 37}, {56, 49}, {86, 79}, {102, 95}, {104,
97}, {110, 103}, {132, 125}, {146, 139}, {152, 145}, {162, 155}, {174, 167}, {180, 173}, {182, 175},
{186, 179}, {194, 187}, {204, 197}, {210, 203}, {216, 209}, {240, 233}, {254, 247}, {260, 253},
{264, 257}, {272, 265}, {284, 277}, {302, 295}, {312, 305}, {314, 307}, {324, 317}, {326, 319},
{330, 323}, {336, 329}, {356, 349}, {362, 355}, {366, 359}, {380, 373}, {384, 377}, {386, 379},
{390, 383}, {404, 397}, {410, 403}, {422, 415}, {446, 439}, {456, 449}, {462, 455}, {470, 463},
{480, 473}, {482, 475}, {512, 505}, {516, 509}, {522, 515}, {524, 517}, {536, 529}, {540, 533},
{554, 547}, {560, 553}, {594, 587}};

```

```
result = FoldList[#2 - 12 &, Last[pairs][[1]], Reverse[Most[pairs]]][[All, 1]]
```

```
a=Differences[result]
```

```
b=a*-1
```

```
c=Reverse[b]
```

```
numbers = c
```

```
result = FoldList[Plus, 12, numbers]
```

and then check for the results...

```
{594,548,542,528,524,512,510,504,500,470,468,458,450,444,434,410,398,392,378,374,372,368,354,350,344,324,318,314,312,302,300,290,272,260,252,248,242,228,204,198,192,182,174,170,168,162,150,140,134,120,98,92,90,74,44,32,30,18,14,8,0}
```

```
{-46,-6,-14,-4,-12,-2,-6,-4,-30,-2,-10,-8,-6,-10,-24,-12,-6,-14,-4,-2,-4,-14,-4,-6,-20,-6,-4,-2,-10,-2,-10,-18,-12,-8,-4,-6,-14,-24,-6,-6,-10,-8,-4,-2,-6,-12,-10,-6,-14,-22,-6,-2,-16,-30,-12,-2,-12,-4,-6,-8}
```

```
{46,6,14,4,12,2,6,4,30,2,10,8,6,10,24,12,6,14,4,2,4,14,4,6,20,6,4,2,10,2,10,18,12,8,4,6,14,24,6,6,10,8,4,2,6,12,10,6,14,22,6,2,16,30,12,2,12,4,6,8}
```

```
{8,6,4,12,2,12,30,16,2,6,22,14,6,10,12,6,2,4,8,10,6,6,24,14,6,4,8,12,18,10,2,10,2,4,6,20,6,4,14,4,2,4,14,6,12,24,10,6,8,10,2,30,4,6,2,12,4,14,6,46}
```

```
{8,6,4,12,2,12,30,16,2,6,22,14,6,10,12,6,2,4,8,10,6,6,24,14,6,4,8,12,18,10,2,10,2,4,6,20,6,4,14,4,2,4,14,6,12,24,10,6,8,10,2,30,4,6,2,12,4,14,6,46}
```

```
{12,20,26,30,42,44,56,86,102,104,110,132,146,152,162,174,180,182,186,194,204,210,216,240,254,260,264,272,284,302,312,314,324,326,330,336,356,362,366,380,384,386,390,404,410,422,446,456,462,470,480,482,512,516,522,524,536,540,554,560,606}
```

these are the even parts of the pairs that satisfy RULE 1. Subtract 7 from the even numbers and you get the odd parts of the ordered pairs.

Now just to clarify the number 914 used in the equation of z in RULE 1 comes from subtracting the 999th prime number from the multiplication of 7*999, which is 7907-(7*999)=914